

# GLOBAL MODELING OF A NEW THREE PHASE HV POWER SUPPLY FOR MICROWAVES GENERATORS WITH N MAGNETRONS BY PHASE (TREATED CASE N=1) UNDER MATLAB SIMULINK CODE

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## ABSTRACT

In the industrial installations of microwave generators, the current single phase power supply uses a single-phase HV power transformer with magnetic shunts for each magnetron. Based on the encouraging results obtained from the modeling of a new generation of single-phase HV power supplies for industrial microwaves generators with N magnetrons, we performed a feasibility study for a new three-phase HV power supply with N magnetrons per phase. In this paper, we present an original conception of a new three-phase of HV power supply for microwaves generators with N magnetrons per phase (treated case N = 1). The modeling of this new generation of power supply for magnetrons passes obligatorily by modeling and dimensioning of its own new three-phase HV power transformer with shunts. This modeling of the new three-phase HV power supply of one magnetron by phase, consists to exploiting the model of new three-phase HV power transformer with shunts by MATLAB-SIMULINK code. This model, resulting from the diagram of the armored magnetic circuit tetrahedron type equivalent of this transformer with magnetic shunts, is a  $\pi$  quadruple model with saturable inductances able to translating the saturation phenomena. The electrical signals obtained (currents and voltages) are variable magnitude curves, periodic and non-sinusoidal dephased  $2\pi / 3$  between them. These signals have the same form as those of experimental of a classical power supply containing one transformer by magnetron. That presents multiple advantages in terms of reducing weight, volume, electrical wiring and cost during the implementation and maintenance of such a new device.

**Keywords:-** High Voltage (HV), Generators, Magnetrons, Matlab, Microwaves, New Modeling,- Power Supply, SIMULINK, Three Phase Transformer

## NOMENCLATURE

The upper and lower case letters represent respectively the primary and secondary quantities.

$r_A, r_B, r_C, r_a, r_b, r_c$  : are respectively the primary and secondary resistances of phases A, B, C.

$i_A, i_B, i_C, i_a, i_b, i_c$  : are respectively the currents traversing the primary and secondary windings of phases A, B, C.

$u_A, u_B, u_C, u_a, u_b, u_c$ : are the primary and secondary windings voltages of phases A, B, C.

$\Phi_A, \Phi_B, \Phi_C, \Phi_a, \Phi_b, \Phi_c, \Phi_{Sh}$ : are respectively the primary, secondary and shunts fluxes by turn in each phase.

$n_1, n_2$ : the number of primary and secondary turns for each phase.

$R_A, R_B, R_C, R_a, R_b, R_c, R_{Sh}$ : magnetic circuit reluctances of primary, secondary and shunts of each phase, traversed respectively by the fluxes  $\Phi_A, \Phi_B, \Phi_C, \Phi_a, \Phi_b, \Phi_c, \Phi_{Sh}$ .

$R_{COM}, R_{com}$ : the common reluctances between the three phases traversed by the common fluxes  $\Phi_{COM}, \Phi_{com}$ .

## 1. INTRODUCTION

This paper treats the modeling of a new three phase HV power supply of industrial microwaves

generators with N magnetrons (type 800 Watts at 2450 MHz) by phase (treat case of N=1). Currently to supply only one magnetron, the industrial installations of single phase HV power supply for microwaves generators use a HV power transformer with magnetic shunts by magnetron [2]-[3]- [10]-[11]. To contribute to the development of technological innovation in industry of manufacturing of power supplies of magnetrons for microwave ovens for domestic or industrial use, this work is part of the development of a new type of three-phase HV power supply for generators microwave with several magnetrons. The new power supply device considered will be thus a different version of the single phase model currently manufactured by the constructors of microwave ovens. It may comprise either a single phase transformer [6]-[8]-[9] or three-phase (Fig.1), or six-phase supplying several magnetrons by phase and not as the current case of a single-phase transformer by magnetron. The modeling of this new generation of power supply of magnetrons passes necessarily by the modeling and dimensioning of its own new three-phase HV power transformer with shunts.

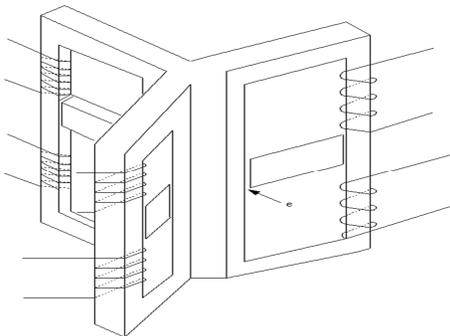


Figure.1. Form Of Magnetic Circuit Diagram Tetrahedron Type Of The New Three Phase HV Transformer With Magnetic Shunts

Moreover, in our previous work, we have made a preliminary study, with EMTF code, dealing with the feasibility [19] at the nominal operation of a new HV power (3x800 Watts at 2450 MHz) three-phase character with one magnetron by phase. In this new HV power supply with three phase character system, we have connected in star three identical  $\pi$  quadruple models of three identical single phase HV transformers with magnetic shunts. These models are supplied by a three-phase system. Encouraged by conclusive results obtained we have undertaken the study of a real and original three-phase transformer newly conceived. It will be dimensioning in this paper and modeled as an equivalent electrical circuit. The new conception of

the new three-phase HV power transformer with magnetic shunts uses an armored structure tetrahedron type (Fig.1) to represent its equivalent magnetic circuit. That will undoubtedly allow to reducing the size, volume and makes this new device more economical while ensuring the regulation process of each magnetron current. For this reason, the new design is more advantageous than the combination of three identical single-phase models connected in star [19]. We have exploited the model of the new three phase HV power supply system of one magnetron by phase with MATLAB-SIMULINK code. It is a  $\pi$  quadruple model derived from diagram of the armored structure magnetic circuit tetrahedron type equivalent of the three phase HV power transformer with magnetic shunts. This model is composed of saturable inductances capable to translating the nonlinear saturation phenomena. Each inductance of this model is characterized its analytical expression, which reflects its non-linear relationship "flux-current". The principle of determination of this relationship has the advantage to be simple and directly obtained from the geometrical parameters of construction of the new three phase transformer.

## 2. PRINCIPLE OF MODELING

The conception of this new HV power transformer with magnetic shunts was based on the diagram of the armored structure of its magnetic circuit tetrahedron type Fig.1. A magnetic shunt serves to divert an important part of flux circulating between the primary and secondary windings of each of three phases. The primary and secondary fluxes of the three phases respectively, are added together to cross the Common reluctances  $R_{COM}$  and  $R_{com}$  (Fig. 2). The sum of these fluxes is zero if the three-phase system is equilibrated. Other hand, taking into account the air-gaps dimension and the magnetic state of saturation, the magnetic fluxes of air dispersion are negligible compared to one through the shunts. Hereafter, we consider the new three-phase transformer without iron losses (hysteresis loss and eddy current). And to simplify the study, we consider the Star Star (Yy) coupling between the primary and secondary windings.

### 2.1 Mathematical Equations and Dimensioning

#### • Electrical Equations

Once the new three-phase transformer with shunts is supplied, the turns of primary and secondary windings of each phase, which are respectively traversed by fluxes  $\Phi_A$ ,  $\Phi_B$ ,  $\Phi_C$ ,  $\Phi_a$ ,  $\Phi_b$ ,  $\Phi_c$ , are thus the seat each one of an electromotive force of auto-induction. Applying of Ohm's law provides the six electrical equations of

the new three-phase transformer with shunts, and considering the general case where the three phase system is not necessarily equilibrated:

$$u_A = r_A \cdot i_A + n_1 \cdot \frac{d\psi_A}{dt} \quad (1)$$

Or  $\psi_A = \Phi_A + \Phi_{COM}$

$\Phi_A$ : is the own flux of phase A and  $\Phi_{COM}$  the common flux of primary side of this phase.

$$u_B = r_B \cdot i_B + n_1 \cdot \frac{d\psi_B}{dt} \quad (2)$$

$$u_C = r_C \cdot i_C + n_1 \cdot \frac{d\psi_C}{dt} \quad (3)$$

$$u_a = -r_a \cdot i_a + n_2 \cdot \frac{d\psi_a}{dt} \quad (4)$$

Or  $\psi_a = \Phi_a + \Phi_{com}$

$$u_b = -r_b \cdot i_b + n_2 \cdot \frac{d\psi_b}{dt} \quad (5)$$

$$u_c = -r_c \cdot i_c + n_2 \cdot \frac{d\psi_c}{dt} \quad (6)$$

Such as the leakage fluxes in the air are negligible, and by writing each total flux in the form:  $n\Phi = Li$ , and considering the currents in the inductances and  $L_{COM}$   $L_{com}$  corresponding to the common reluctances between phases  $R_{COM}$  and  $R_{com}$ , the previous equations become:

$$u_A = r_A \cdot i_A + \frac{d}{dt}(L_A \cdot i_A) + \frac{d}{dt}(L_{COM} \cdot i_{COM}) \quad (7)$$

Or  $i_{COM} = i_A + i_B + i_C$

$$u_B = r_B \cdot i_B + \frac{d}{dt}(L_B \cdot i_B) + \frac{d}{dt}(L_{COM} \cdot i_{COM}) \quad (8)$$

$$u_C = r_C \cdot i_C + \frac{d}{dt}(L_C \cdot i_C) + \frac{d}{dt}(L_{COM} \cdot i_{COM}) \quad (9)$$

$$u_a = -r_a \cdot i_a + \frac{d}{dt}(L_a \cdot i_a) + \frac{d}{dt}(L_{com} \cdot i_{com}) \quad (10)$$

Or  $i_{com} = i_a + i_b + i_c$

$$u_b = -r_b \cdot i_b + \frac{d}{dt}(L_b \cdot i_b) + \frac{d}{dt}(L_{com} \cdot i_{com}) \quad (11)$$

$$u_c = -r_c \cdot i_c + \frac{d}{dt}(L_c \cdot i_c) + \frac{d}{dt}(L_{com} \cdot i_{com}) \quad (12)$$

• **Magnetic Equations**

From the diagram of the equivalent magnetic circuit of the new three-phase transformer with shunts Fig.2 (see Appendix a), and applying the magnetic circuit formulas, we can write the magnetic equations for each phase of the new three-phase transformer for new three-phase HV power supply for microwaves generators. The dimensions of the magnetic circuit of the Fig.2 are identified by the letters A, B, C, D, E, F which are relative to the average line of magnetic flux of various magnetic circuit portions.

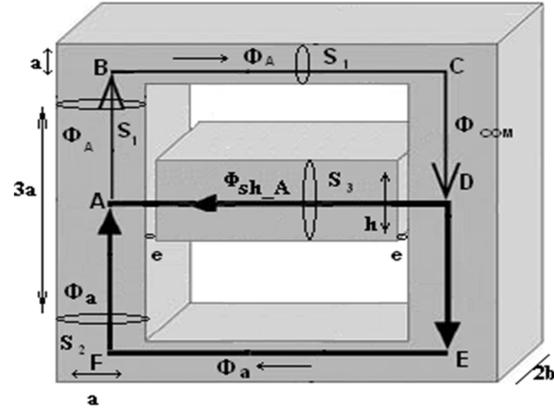


Figure.2: Diagram Of The Equivalent Magnetic Circuit Of One Phase (Phase A As Example) Of The New Three-Phase Transformer With Magnetic Shunts

We take the phase A as example:

1. For the path ABCDA :

$$R_A \cdot \Phi_A + R_{COM} \cdot \Phi_{COM} + R_{sh\_A} \cdot \Phi_{sh\_A} = n_1 \cdot i_A \quad (13)$$

2. For the path ADEFA

$$-R_{sh\_A} \cdot \Phi_{sh\_A} + R_{com} \cdot \Phi_{com} + R_a \cdot \Phi_a = -n_2 \cdot i_a \quad (14)$$

With,  $\Phi_{com}$  and  $\Phi_{COM}$  are the sum respectively of fluxes  $\Phi_a, \Phi_b, \Phi_c$  and  $\Phi_A, \Phi_B, \Phi_C$  traversing the common reluctances  $R_{com}$  and  $R_{COM}$ .

3. For the path BCEFB :

$$R_A \cdot \Phi_A + R_{COM} \cdot \Phi_{COM} + R_{com} \cdot \Phi_{com} + R_a \cdot \Phi_a = n_1 \cdot i_A - n_2 \cdot i_a \quad (15)$$

The equations (13) to (15), are complemented by the additional relations translating the fluxes conservation law for each phase:

$$\Phi_A = \Phi_a + \Phi_{sh\_A} \quad (16)$$

$$\Phi_B = \Phi_b + \Phi_{sh\_B} \quad (17)$$

$$\Phi_C = \Phi_c + \Phi_{sh\_C} \quad (18)$$

Such as:  $\Phi_{sh\_A}, \Phi_{sh\_B}$  and  $\Phi_{sh\_C}$  are respectively, total fluxes traversing the shunts of phases, A, B and C. We obtain thus, the complete system of electric and magnetic equations representing the operation of the new three-phase HV transformer with magnetic shunts of the new three phase HV power of magnetrons.

**2.2 Equivalent electrical circuit of the new three-phase transformer with shunts**

- **$\pi$  quadruple model by phase referred to secondary**

We take always the phase A as example:

$$u_A = r_A \cdot i_A + n_1 \cdot \frac{d\Phi_A}{dt} + n_1 \cdot \frac{d\Phi_{COM}}{dt} \quad (19)$$

$$u_a = -r_a \cdot i_a + n_2 \cdot \frac{d\Phi_a}{dt} + n_2 \cdot \frac{d\Phi_{com}}{dt} \quad (20)$$

Multiplying equation (19) by  $(n_2/n_1)$  and writing the quantities  $(n_1\Phi_A)$  and  $n_1\Phi_{COM}$  in the form:

$$n_1 \cdot \left(\frac{n_2}{R_A}\right) \left(\frac{R_A}{n_2}\right) \Phi_A$$

We obtain:

$$\begin{aligned} u'_A &= r'_A \cdot i'_A + n_2 \cdot \frac{d\Phi_A}{dt} + n_2 \cdot \frac{d\Phi_{COM}}{dt} \\ &= r'_A \cdot i'_A + \frac{d}{dt} \left( \frac{n_2^2 R_A}{R_A n_2} \Phi_A \right) \\ &\quad + \frac{d}{dt} \left( \frac{n_2^2 R_{COM}}{R_{COM} n_2} \Phi_{COM} \right) \end{aligned}$$

With:  $r'_A = \left(\frac{n_2}{n_1}\right)^2 r_a$ ,  $i'_A = \left(\frac{n_1}{n_2}\right) i_a$ ,  $u'_A = \left(\frac{n_2}{n_1}\right) u_a$   
 By posing the inductance  $(n_2^2/R_A)=L'_{p-A}$  and the electric current  $(R_A\Phi_A/n_2) = i'_{p-A}$ , the above equation become:

$$\begin{aligned} u'_A &= r'_A \cdot i'_A + \frac{d}{dt} (L'_{p-A} \cdot i'_{p-A}) \\ &\quad + \frac{d}{dt} (L'_{COM} \cdot i'_{COM}) \quad (21) \end{aligned}$$

We replace  $n_2\Phi_a$  and  $n_2\Phi_{com}$  in the equation (20) by  $n_2\Phi_a = \left(\frac{n_2^2}{R_a}\right) \left(\frac{R_a}{n_2}\right) \Phi_a$  and by posing the inductance  $(n_2^2/R_a)=L_{s-a}$  and the electric current  $(R_a\Phi_a/n_2) = i_{s-a}$ , we obtain:  $u_a = \frac{d}{dt} (L_{s-a} \cdot i_{s-a}) + \frac{d}{dt} (L_{com} \cdot i_{com}) - r_a \cdot i_a$  (22)

The development of the auto-induction force expression  $n_2 \cdot \frac{d\psi_A}{dt}$  can lead to the following relation:

$$\begin{aligned} n_2 \cdot \frac{d\psi_A}{dt} &= \frac{d}{dt} \left( \frac{n_2^2}{R_a} \right) \left( \frac{R_a}{n_2} \right) \psi_a \\ &\quad + \frac{d}{dt} \left( \frac{n_2^2}{R_{sh-A}} \right) \left( \frac{R_{sh}}{n_2} \right) \Phi_{sh-A} \end{aligned}$$

By posing  $(n_2^2/R_{sh-A})=L'_{sh-A}$  and  $(R_{sh-A} \cdot \Phi_{sh-A}/n_2) = i'_{sh-A}$ :

$$n_2 \cdot \frac{d\psi_A}{dt} = \frac{d}{dt} (L_a \cdot i_a) + \frac{d}{dt} (L'_{sh-A} \cdot i'_{sh-A}) \quad (23)$$

The equations (21) to (23) respond to the single phase equivalent circuit reduced to secondary of three-phase transformer with shunts of Figure.2. All occurs as so for each phase of this new three-phase HV transformer with shunts tetrahedron type, was composed of three perfect transformers, each one supplies a  $\pi$  quadruple composed of the inductive elements  $L'p$  and  $L_{COM}$  on the primary side,  $L_S$  and  $L_{com}$  on the secondary one and  $L'_{HS}$  on the shunt side. These inductances are respectively traversed by currents  $i'p$ ,  $i_{COM}$ ,  $i_s$ ,  $i_{com}$  and  $i'_{sh}$ .

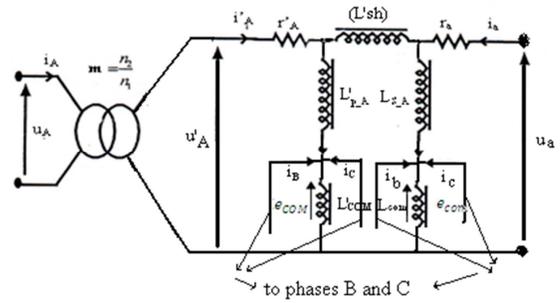


Fig. 3.  $\pi$  Quadruple Model Of Saturable Inductances Referred To Secondary Equivalent Of New Three-Phase HV Transformer With Magnetic Shunts

In perfect transformer input of phases A, B, C, we have the currents  $i_A$ ,  $i_B$ ,  $i_C$  and the voltages  $u_A$ ,  $u_B$ , and  $u_C$ . And in its outputs, we find the voltages  $u'_A = (n_2/n_1) u_A$ ,  $u'_B = (n_2/n_1) u_B$  and  $u'_C = (n_2/n_1) u_C$  and the currents  $i'_A = (n_1/n_2) i_A$ ,  $i'_B = (n_1/n_2) i_B$  and  $i'_C = (n_1/n_2) i_C$ . Finally we obtain to the output terminals of these quadruples the real voltage of output of three-phase transformer with shunt  $u_a$ ,  $u_b$ ,  $u_c$ .

### 2.3 Analysis of transformer model

The advantage of the armored type tetrahedron structure used for the new three-phase transformer with magnetic shunts, is that each phase is supplied by a simple voltage 220 volts.

The distribution of primary, secondary and shunts fluxes in each phase, is the same as that one of single-phase HV transformer with shunts, which ensures the stabilization of the current in the classical HV power for microwaves generators. This leads us to two important points:

- Deduce the geometry of the magnetic circuit of the new three phase HV transformer from that of single-phase transformer with magnetic shunts. Geometrical parameters are namely: the width of the core unwound  $a$ , sections of different cores  $S_1$ ,  $S_2$  and  $S_3$ , the thickness of the air-gaps  $e$ .
- Validate this model of the new three-phase HV transformer with magnetic shunts by the comparison between the curves from this model with those simulated and experimental of single-phase HV transformer with magnetic shunts presented in [8]-[11]-[12].

### 3. MODELING OF NONLINEAR INDUCTANCES OF NEW MODEL

Each inductance of the studied model is a function of the reluctance, of the portion of magnetic circuit supposed as fictively closed on which is wound  $n_2$  turns, and thus the magnetic permeability  $\mu$ . This one depends in a complex way

of state saturation, consequently of the variable current at every moment. Under these conditions, there is no proportionality between the voltage and current of each inductor, since the latter varies with these quantities.

To be able exploit with MATLAB-SIMULINK code, the study in the nonlinear regime of phenomena related to the saturation of each inductance, it is necessary to represent each nonlinear inductive element by its analytical expression deduced from fitting of magnetization curve of material used by constructors (SF<sub>19</sub>) [8]-[21]. The total flux  $n_2\Phi(i)$ , ( $\Phi(i)$  is the flux per turn) as a function of current  $i$  is given by the relation:

$$L = \frac{n_2 \cdot \Phi(i)}{i} = \frac{n_2^2 \cdot B \cdot S}{H \cdot l} = \frac{n_2^2 \cdot S}{l} \cdot \frac{B}{H(B)} \quad (24)$$

We therefore admit that any saturable part of the armored magnetic circuit investigated, has a characteristic form which is given in appendix Fig.2. And in the following, we consider only the effects of saturation; hysteresis effects and eddy currents are neglected. For determining the characteristic of each inductance from the geometrical parameters of construction of the considered magnetic circuit portion of this transformer, we use the fitting of the magnetization curve  $B(H)$  of the material used. We translate therefore the variation law of flux  $n_2\Phi(i)$  as a function of  $i$  for each inductance.

### 3.1 Characteristic of each inductance

- **Characteristic  $n_2\Phi_p(i'p)$  of the primary inductance  $L'p$**

For the calculation and simulation, we remember that the nonlinear inductance of each branch is replaced by the analytical expression of the instantaneous current as a function of flux passing through this inductance. We mention also that the reluctance  $R$  of a homogeneous magnetic circuit portion has as length  $l$ , section  $S$  and permeability  $\mu$ , is given by the equation  $R = (l / \mu s)$ . From Figure 2 and the proposed model in paragraph 2.2, the primary inductance is the inductance of a ferromagnetic circuit supposed as fictively closed, corresponding to the path ABC (Fig.2) length  $l_p$  and section  $S_1$ . On this last path, we consider wound  $n_2$  turns traversed by the current  $i'p$ . From the fitting of the magnetization curve that gives the expression of the magnetic field  $H$  as a function of magnetic induction  $B$  [8] and the values of  $n_2$ ,  $S_1$ ,  $l_p$ , as recorded in Appendix c, we arrive at the  $n_2\Phi_p(i)$  law using the relationship:

$$i_p = \frac{l_p}{n_2} H(B) \quad (25)$$

And as we use the flux  $\Phi$  as input to this model

from a simple integration of the voltage (Appendix Fig.2), we must replace the induction  $B$  in equation (25) by the flux through the relationship:  $B = \Phi/S$

- **Characteristic  $n_2\Phi(i)$  of inductances commons  $L_{COM}$  and  $L_{com}$**

The common inductances between the three phases  $L_{COM}$  (primary side) and  $L_{com}$  (secondary side) are inductances of circuits ferromagnetic corresponding to CD and DE paths (Fig.2) its lengths respectively  $l_{COM}$  and  $l_{com}$  and section  $S_1$ . On these CD and DE paths, we consider wound  $n_2$  turns traversed by the currents  $i_{COM}$  and  $i_{com}$ . The characteristics of these inductances are therefore given by the relations:

$$i_{COM} = \frac{l_{COM}}{n_2} H(B) \text{ and } i_{com} = \frac{l_{com}}{n_2} H(B) \quad (26)$$

- **Characteristic  $n_2\Phi(i)$  of the secondary inductance  $L_s$**

Considering the symmetry of the magnetic circuit armored compared to the axis AD (Fig.2) and using relations similar to the preceding, we obtain, by posing  $l_s$  the average length corresponds to the path AFEA and the secondary section  $S_2$  ( $S_2 = S_1$ ), the equations of the form:

$$i_s = \frac{l_s}{n_2} H(B) \quad (27)$$

- **Characteristic  $n_2\Phi_{sh}(i'_{sh})$  of inductance  $L'_{sh}$**

$L_{sh}$  is the inductance of an assumed magnetic circuit supposed as fictively closed, corresponding to path DA (Fig.2) and of width  $l_{sh} - 2 \cdot e_{sh}$ , of section  $S_3$  ( $S_3 = h \cdot (2b)$ ), see Appendix .c).  $L_{sh}$  is in series with two narrow air gaps of length  $e$  each one ( $e_{sh} = 2e$  is the global length of a shunt), on which we consider wound  $n_2$  turns which is traversed by the current  $i'_{sh}$ .

Applying the magnetic circuit's law in this ferromagnetic field with air gaps, we obtain:

$$\left( \frac{1}{\mu} \cdot \frac{l_{sh} - e_{sh}}{S_3} + \frac{1}{\mu_0} \cdot \frac{e_{sh}}{S_3} \right) \Phi_{sh} = n_2 \cdot i'_{sh}$$

If  $R_{sh}$  designates the reluctance of this portion, it corresponds to the reluctance of the ferromagnetic part ( $R_{sh}^f$ ) and reluctance constant ( $R_{sh}^e$ ) caused by the air of the air gap, hence:

$$R_{sh} = R_{sh}^f + R_{sh}^e \quad (28)$$

$$\text{With: } R_{sh}^f = \frac{1}{\mu} \cdot \frac{l_{sh} - e_{sh}}{S_3} \text{ and } R_{sh}^e = \frac{1}{\mu_0} \cdot \frac{e_{sh}}{S_3}$$

We know that the inductance ( $L'_{sh} = n_2^2 / R_{sh}$ ) traversed by the current  $i'_{sh}$  obeys the law :

$$n_2 \Phi_{sh} = L'_{sh} i'_{sh}$$

By writing the expression of the  $L'_{sh}$  according to ( $R_{sh}^f$ ) and ( $R_{sh}^e$ ), it comes:

$$L'_{sh} = \frac{n_2^2}{R_{sh}^f + R_{sh}^e} = \frac{\frac{n_2^2}{R_{sh}^e} \cdot \frac{n_2^2}{R_{sh}^f}}{\frac{n_2^2}{R_{sh}^e} + \frac{n_2^2}{R_{sh}^f}}$$

That we can put in a more convenient form: by posing

$$(L'_{sh})^e = \frac{n_2^2}{R_{sh}^e} \text{ The air gap inductance and}$$

$$(L'_{sh})^f = \frac{n_2^2}{R_{sh}^f} \text{ Inductance of ferromagnetic part}$$

We obtain thus:

$$L'_{sh} = \frac{(L'_{sh})^e * (L'_{sh})^f}{(L'_{sh})^e + (L'_{sh})^f} \quad (29)$$

Other hand, the current expression  $i'_{sh}$  becomes:

$$i'_{sh} = \frac{R_{sh}}{n_2} \Phi_{sh} = \frac{R_{sh}^e}{n_2} \Phi_{sh} + \frac{R_{sh}^f}{n_2} \Phi_{sh}$$

by posing:  $(i'_{sh})^e = \frac{R_{sh}^e}{n_2} \Phi_{sh}$  and  $(i'_{sh})^f = \frac{R_{sh}^f}{n_2} \Phi_{sh}$

$$n_2 \Phi_{sh} = (L'_{sh})^e * (i'_{sh})^e + (L'_{sh})^f * (i'_{sh})^f \quad (30)$$

From equations (28) (29) (30), we find thus that the inductance  $L'_{sh}$  is equivalent to two inductances  $(L'_{sh})^e$  and  $(L'_{sh})^f$  in parallel. The inductance  $(L'_{sh})^e$  is supposed as fictive winding  $n_2$  turns wound in the air of section  $S_3$  traversed by the current  $i'_{sh}$ .

At the inductance  $(L'_{sh})^f$ , we associate a ferromagnetic circuit corresponding to the path AD of length  $l_{sh-e_{sh}}$ . The  $\pi$  quadruple model of the three phase transformer with shunts in figure 3 is slightly modified, it becomes equivalent to that of Fig.4.

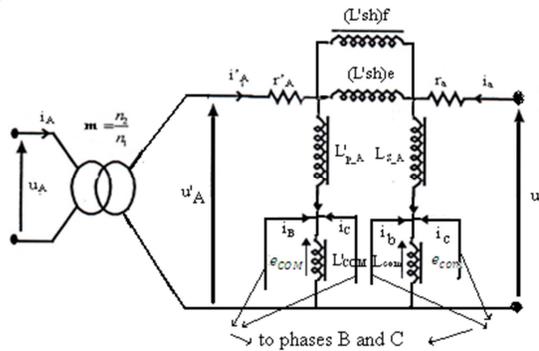


Figure.4: New  $\Pi$  Quadruple Model Of Three-Phase Transformer With Shunts

We see that to translate the relationship  $n_2 \Phi_{sh}$  ( $i$ ) of the inductance  $L'_{sh}$ , it is enough to find the relationship  $n_2 \Phi_{sh}$  ( $i'_{sh}^f$ ) of the inductance  $(L'_{sh})^f$ , because the inductance  $(L'_{sh})^e$  is constant. From the expression of the instantaneous current passing through this inductance derived from the B(H) curve fitting and the values of  $n_2$ ,  $L'_{sh}$ ,  $S_3$  and  $e_{sh}$ . We arrive at the  $n_2 \Phi_{sh}(i'_{sh}^f)$  law using the relations:

$$(i_{sh})^f = \frac{l_{sh-e_{sh}}}{n_2} H(B) \quad (31)$$

#### 4. SIMULATION RESULTS

The study of the operation under nominal state of this new system in Figure 5 was undertaken. The mounting of Fig.5 was simulated by MATLAB-SIMULINK code, to reflect the operation of the three-phase HV power for microwaves generator with one magnetron by phase able to delivering under 220 V its full power 800 Watts useful at 2450 MHz. All three identical models supplies normally at nominal state one magnetron type 800 Watts at 2450 MHz. Figure 5 shows the equivalent diagram of mounting of three-phase HV power supply of a new generation of microwaves generators with N magnetrons by phase (case treated N = 1 by magnetron phase). It is composed of three  $\pi$  quadruple models equivalent of phases. Every one supplies at its output a voltage doubler cell composed of a capacitor and a diode that in its output supplies only one magnetron.

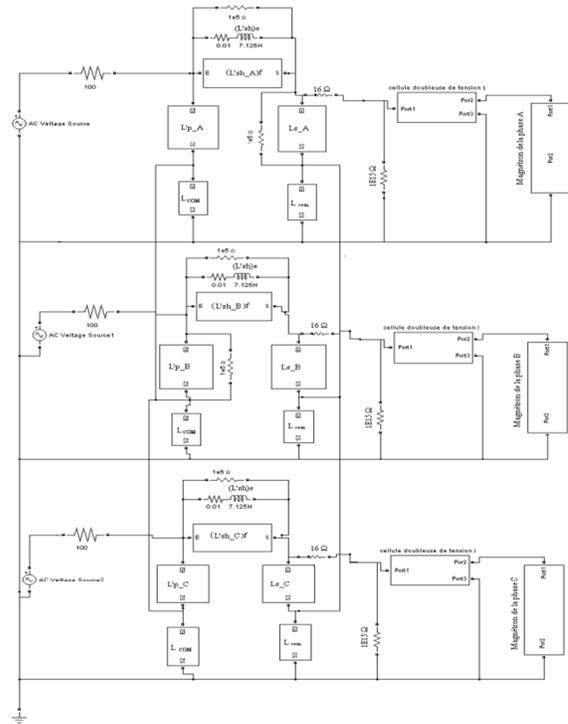


Figure.5. Equivalent Diagram Of The Mounting Of Three-Phase HV Power Supply For One Magnetron By Phase Simulated With The MATLAB-Code SIMULINK

This equivalent circuit reflects the behavior of the entire three-phase HV power supply including the magnetron and the three-phase transformer with shunts. The simultaneous solution of electric and magnetic equations of entire system is too complex.

The solution can be only numerical (MATLAB-SIMULINK or other code). Based on the nonlinear characteristics already calculated by the above formulas of each inductance and using developed programs around the MATLAB-SIMULINK code, we simulated the circuit behavior of the new three phase HV power of microwaves generator with one magnetron per phase. Figure 6 shows the oscillograms obtained from this simulation. As first remark, we note that the electrical signals obtained ( $I_{diode}$ ,  $I_{secondary}$ ,  $I_{magnetron}$ ,  $V_{magnetron}$ ,  $V_{secondary}$ ,  $V_{condensator}$ ) are curves periodic and non-sinusoidal dephasing  $2\pi/3$  between them (Fig.6). These signals have the same form as those of experimental and simulated of classic HV power supply having a single transformer by magnetron. The dephasing of  $2\pi/3$  confirms the absence of interaction between magnetrons.

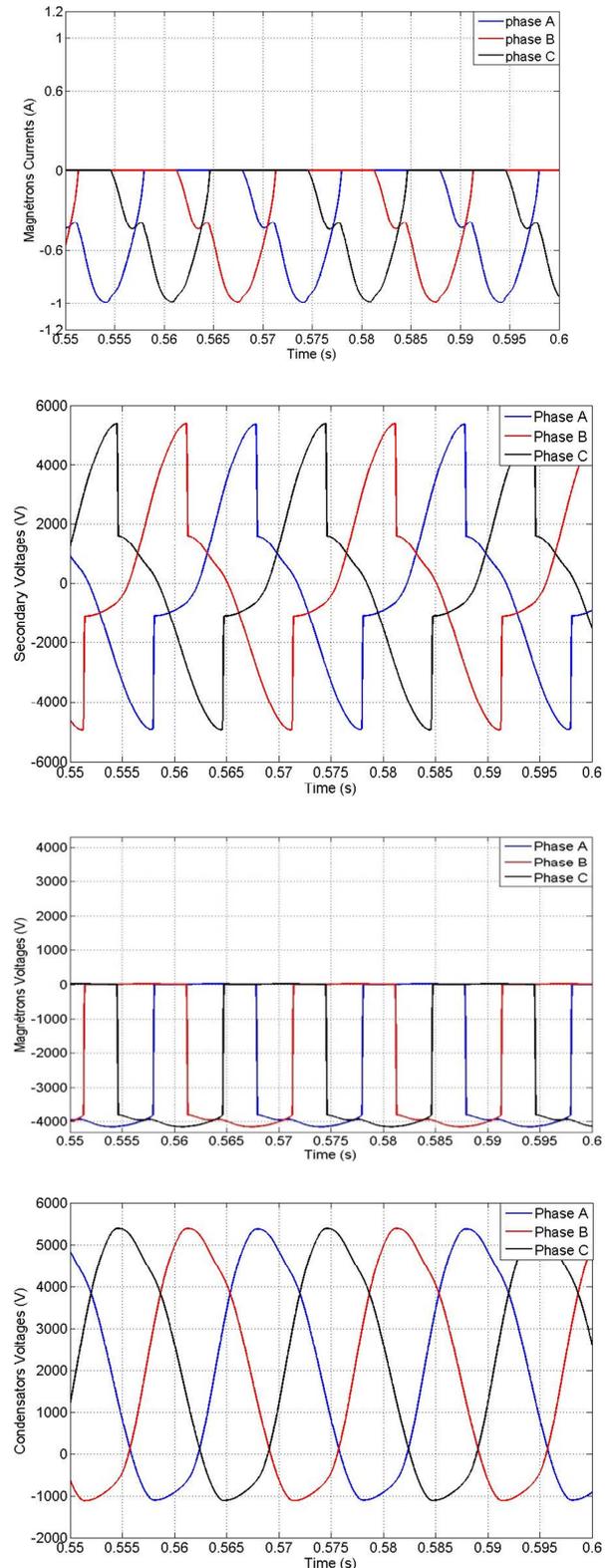
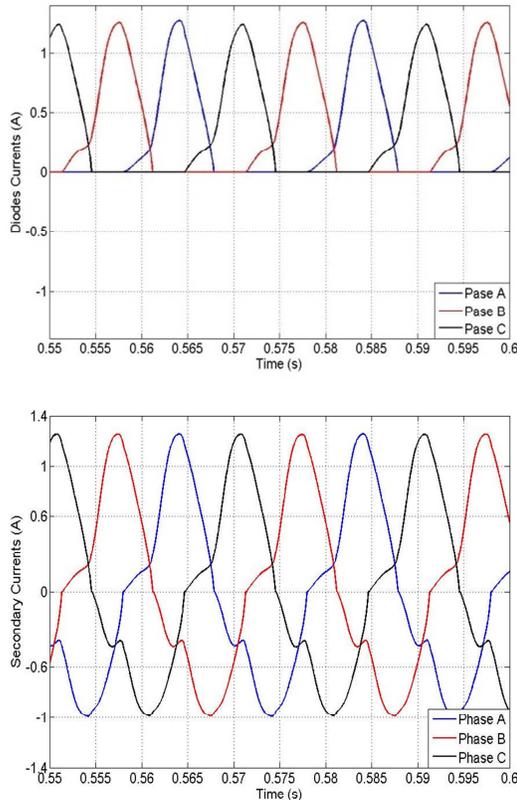


Figure.6. Waveforms Of Current And Voltage Of Simulation Of The New Three-Phase HV Power System For Magnetron.

The operating points of these magnetrons are no longer disturbed, which is essential for a stabilized current power supply. Moreover, the tests of the breakdowns of the magnetrons, which we carried out, confirm that the breakdown of N magnetrons does not modify the operation of the remaining magnetrons. It suffices to replace the magnetron off by a new one.

**5. CONCLUSION**

The study of operating at nominal state of new system of three phase HV power supply with one magnetron by phase has been conclusive. It can be extended without any problem in case of power supply operation of magnetrons by N phase at the nominal state. In the other hand, the breakdown of one or more of N magnetrons supplied does not change the operation of remaining magnetrons. The modeling of the new three phase HV power supply with one magnetron by phase, based on an appropriate dimensioning by magnetic circuit tetrahedron type of its own three-phase HV transformer with shunts has been done. That will certainly help undoubtedly to reduce size, volume, weight and electrical cabling and therefore guarantee a lower cost of implementation and maintenance of microwaves generators. This study can be extended for modeling a three-phase transformer with magnetic shunt with a armored-magnetic circuit type of three or five columns, able to supplying in its secondary N magnetrons by phase. This work can also be similarly performed to the case of the same type of three phase or six-phase HV power supply for several magnetrons by phase with useful power 1000 Watts or 1200 Watts for each one at 2450 MHz. Thus contributing to the development of new modeling systems of three-phase or six-phase of power supply with several magnetrons (800 Watts, 1000 Watts or 1200 Watts at 2450 MHz) by phase for microwaves generators for industrial applications. An optimization strategy of the new three-phase HV power supply can also be defined using optimization programs developed around the MATLAB-SIMULINK code, to reduce the installation cost and without damage the magnetrons tubes. The results of this optimization, allow us to realize the new three-phase HV transformer with shunt for a new generation of industrial microwaves generators. And this will contributes to technological innovation.

**6. APPENDIX**

**a- Geometry of transformer with magnetic shunts**

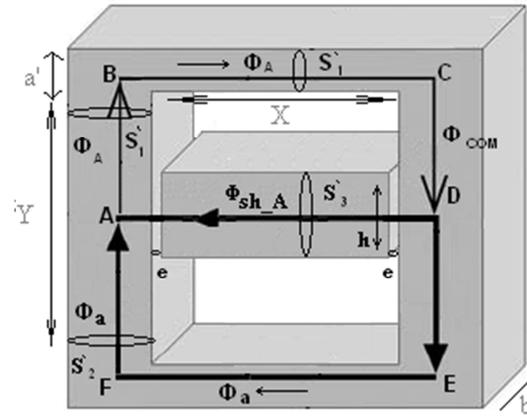


Fig.1

We have S'<sub>1</sub> that the section must be equal to the section of single-phase transformer with magnetic shunts S<sub>1</sub>:

$$S'_1 = a' * b'$$

$$S_1 = 2 * a * b$$

Thus, we have two solutions for the geometry of this new three phase transformer with shunts:

1. a' = a and b' = 2 \* b
2. a' = 2 \* a and b' = b

As the section S'<sub>3</sub> must be the double of the section S<sub>3</sub>.

$$S'_3 = h' * b'$$

$$S_3 = h * b$$

$$S'_3 = 2 * S_3$$

From the above solution 1: a' = a and b' = b \* 2 is more realizable

**X and Y calculated from the reluctances:**

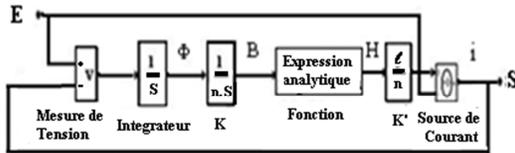
The primary and shunts reluctances that correspond to paths respectively ABCD and AD, must therefore be equal to those in case of single phase. That allows us to obtain the system of equations:

- 1)  $\frac{1}{2} Y + 0.5 * a + 0.5 * a + X + 0.5 * a + 0.5 * a + \frac{1}{2} Y = 6.5 * a$
- 2)  $0.5 * a + X + 0.5 * a - 2 * e = 2.5 * a - 2 * e$

From this system we have:

$$X=1.5*a ; Y=3*a$$

b- Fig.2



c- Parameters

- a' = a = 0.02 m ;
- b = 0.06 m
- b' = 0.12 m ;
- n2 = 2400 ;
- s1 = a' \* b' m<sup>2</sup> ;
- lp = 4.5 \* a ;
- l<sub>COM</sub> = 2 \* a ;
- ls = 4.5 \* a ;
- l<sub>com</sub> = 2 \* a ;
- e = 0.00055 mm ;
- s3 = 0.00068 \* b \* n3 m<sup>2</sup> ;
- lsh = (2.5 \* a - 2 \* e) ;

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