

DETECTION AND ELIMINATION OF DISCREPANCIES IN BIG DATA AT TRANSPORT APPLYING STATISTICAL METHODS

AZAT TASHEV¹, JANNA KUANDYKOVA¹, DINARA KASSYMOVA^{1,2},
AINUR AKHMEDIYAROVA¹

¹ Institute of Information and Computational Technologies CS MES RK, Kazakhstan

² Doctoral student of Kazakh National Research Technical University named after K.I. Satbayev,
Kazakhstan

E-mail: ¹dikakassymova@gmail.com, ²dika.cat@mail.ru

ABSTRACT

An article herein considers the problems of discrepancies detection and elimination upon processing the big data at transport. Tasks of detecting and eliminating the discrepancies in the data has been solved by means of Grabbs method. To obtain trip time design characteristics values there have been applied statistical methods, which allow correct their prescheduled values. The given methodology is used the big data processing at transport in real time mode.

Keywords: *Smart transport system, discrepancies, big data*

1. INTRODUCTION

Using the information and communication technologies for urban management with the aim to upgrade quality of services to the urban residents is one of the main tasks upon constructing a smart city. Applying the technologies thereof reduces infrastructure and operation costs, upgrades efficiency of available resources usage, as well, improves urban residents interrelations with city transport [1]. Nowadays, such technologies are widely employed in contemporary cities transport service sphere. Today, public transport is a role-defining category in the city infrastructure formation for maintaining citizens mobility [2]. In particular, it is felt in heavily populated areas. At present transport systems do not completely meet the passengers ever-growing requirements. To solve such problems it is indispensable to have the knowledge of overall situation and information, concerning the city transport [3]. Unfortunately, the solution of city transport problems is usually based on unreliable information. Therefore, the decision taking process in reference to the transport situation is not optimal.

Rapid development of Kazakhstan economy and automobile industry has resulted in sharp increase of transportation load. As of December 1, 2019, in the Republic of Kazakhstan number of registered passenger cars constituted 3768,7 thousand units,

thereat, over millions of them are in Almaty. Thus, less, than for 5 years amount of automobiles, Almaty citizens own, almost doubled. Such great automobiles possession has quickly brought to the rise of social costs – including traffic jams on the roads and road accidents in Almaty city.

Usage of intelligent transport system plays an important role in smart cities transport systems. Intelligent transport systems include: synergic, synergetic technologies, artificial intellect, engineering principles, applied to transport systems for increasing the traffic capacity, maintaining security, etc. [4]. Intelligent transport systems allow collect large-scale data on transport and means of its movement [5], and fulfill processing the obtained information to optimize traffic current and citizens transportation.

Kazakhstan, in the frame of transport and logistic spheres digitization programs, creates intelligent transportation systems (IITS). One of ITS components is special automated measuring means, being installed at vehicles and automobile transport corridors. It secures monitoring and account of traffic intensity, excluding groundless stops. The system consists of road media boards networks, providing the road traffic participants with useful information: guidance to the nearest streets and objects with estimated time en-route to them, traffic stream speed limitation on the way, information on traffic jams and bypass roads, messages about

emergency situations, messages about oncoming emergency ambulance, operational messages from city administration, etc. The network is managed from a single center, able to process big data. It allows predict road situations and plan changes in road traffic, dependent on various situations, such as, weather, roads under repair, striping change, change of traffic lights working mode, etc.

In the work [6] a large-scale task is broken down into plenty of small subproblems, which are solved in parallel at different computational elements, which increases processing speed. For the recent 10 years there have been elaborated various systems for the big data analysis, using distributed computations, based on cloud technologies, inclusive [7].

Previously, the authors have developed the algorithm of specifying the maximum flow upon distributing in the network [8] and considered the problem of locating minimal number of chambers in the given transportation network [9]. The scientific work herein is a logic continuation of the work on the research topic.

At present, in Transport Holding of Almaty city, mainly, the data on routes drive and by card Onai are stored in archive without processing. The first step to upgrading the performance of the city transport is big data processing, using the new information technologies. In the result there will be improved:

- i. public transport operation quality, based on the analysis of buses location history;
- ii. passengers mobility applying the analysis of tickets purchase with transport cards.

One of the basic tasks upon big transport data processing is detection and elimination of discrepancies.

The article herein presents an approach to analysis and treatment of public transport big data, based on applying the statistical methods with elimination of contradictory information.

2. REVIEW OF WORKS ON RELATED TOPICS

Some approaches to detecting discrepancies and big data processing and their advantages are given in the Table 1, 2.

Table 1: Examples of techniques for transport data processing

Method	Advantage	Employment
k- nearest neighbors[10]	Prediction precision,	Traffic state forecasting

	efficiency and sustainability	
Random forest, Bayesian inference [11]	Traffic improvement and safety, active traffic control	Security maintenance at urban freeways
Bayesian classifier, support vector regression (SVR)[12]	Experiment outcomes have shown, that an approach, using evaluation, based on SVR, has higher precision, than linear regression	Traffic flow prediction in real time
k- nearest neighbors, Gaussian process[13]	Processing time cut for 69%, an offered method can accurately predict traffic stream speed with a mean error, less than 2 miles per hour	Traffic speed prediction
k- nearest neighbors [14]	Upgrade of performance and scaling of transport streams short-term scaling, comparing to existing approaches	Traffic speed prediction
k- nearest neighbors, Bayesian inference, algorithm MOCcell[15]	Employed multicriteria honeycomb genetic algorithm MOCcell for optimizing the bus depot schedules with various busload	For improving the system of public transport

Table 2: Examples of training methods, used in anomalies identification

Method	Usage
Training method: controlled	
Hidden Markov Model, HMM	Controlled statistic Markov model, in which the system under simulation is considered to be Markov process with hidden states: employed for anomalies detection [16].
Support Vector Machine (SVM)	Presentation of data points in space, displayed in such a way, that separate categories are divided, forming close-cut separation between them: special class SVM, namely, one class of SVM (OCSVM) is

	widely used for anomalies detection [17].
Gaussian regression (GR)	General controlled training technique, designated for solving the regression and probabilistic classification of the problem: used for anomalies detection from video [18],[19].
Convolutional Neural Networks (CNN)	Class of in-depth neural networks, applied conventionally for visual images analysis: owing to its applicability to retrieval of semantic level functions from the input, it has become popular in plenty of applications, including the anomalies detection [20].
Training technique: uncontrolled	
Latent Dirichlet Allocation (LDA)	Thematic model, using statistic analysis for obtaining the topics main distribution in documents: used to model video vivid words for anomalies detection [21]
Probabilistic Latent Semantic Analysis (pLSA)	Model for presenting the information about concurrent incoming in probability structure: used in [22] for anomalies detection.
Hierarchical Dirichlet process (HDP)	Nonparameteric Bayesian approach, designed, based on LDA, for data clustering: used at modeling data to detect anomalies [23].
Gaussian Mixture Model (GMM)	Probabilistic model, assuming, that all data points are generated from finite numbers mixture of Gaussian distributions with unknown parameters: used for anomalies detection [24].
Principal component analysis (PCA)	Orthogonal transformation statistic procedure for observations set transforming, possible, for correlated variables into values set of linearly uncorrelated variables: used for dimensionality cutoff [25].
Training technique: Hybrid	
HDP + HMM	Hybrid model: used for presenting the sub-trajectories in [26] for detecting anomalies, using MIL
CNN-LSTM	Hybrid model: detecting anomalies based on forecast, by means of CNN-LSTM [27]

There is following initial data:

- Aggregate of random magnitudes actual values, representing headways, public transport running time, etc.

- Mathematical expectation a priori values and random magnitudes mean-square deviation. For instance, there prescribed public transport headways and their permissible deviations.

The task consists in tentative detecting and eliminating the discrepancies in the aggregate of random magnitudes actual values, as well, in estimation of mathematical expectation and random magnitude mean square deviation and adjustment of their a priori values.

4. THEORETICAL PART

4.1. General algorithm discrepancies detection and elimination.

Considerable role in the research plays the information quality, which is affected with contradictions, missings, bad values, ejections, etc. They might be defined and eliminated with various methods [28], computer-aided learning, inclusively. Fig.1 shows the general process of data pre-processing.

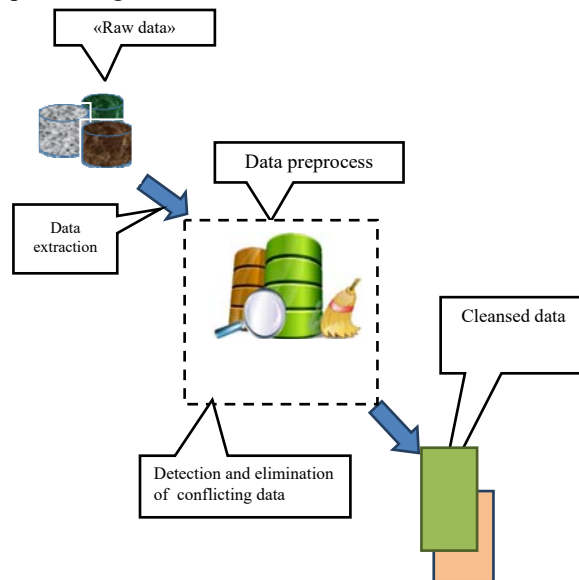


Figure 1: General process of data pre-processing

Figure 1 demonstrates, that the incoming data is subject to pre-processing (classified, cleaned, transformed, checked) and transmitted to subsequent analysis.

Figure 2 shows general block-scheme of detecting and eliminating the conflicting data in real time scale.

3. PROBLEM STATEMENT

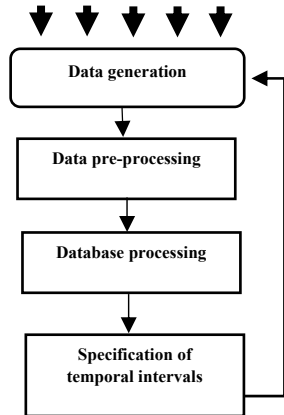


Figure 2: General block-scheme of detecting and eliminating the conflicting data (extra-bold arrows denote entering the new information into the base to form the database)

It follows from the Figure, that the data enters the system uninterruptedly and it is processed as and when it is received. The next step is the big data pre-processing. Hereby, we consider merely temporal contradictions, linked with public transport running in Almaty city.

Conflicting data processing consists of the following stages:

- 1) identifying conflicting data;
- 2) conflicting data processing

Conflicting data definition in the article herein is fulfilled by means of Grabb's method, and processing might be executed with one of the following techniques:

- 1) detected conflicting data is eliminated;
- 2) detected conflicting data is corrected

(for example, replaced with mathematical expectation estimation).

In the result of the process thereof, the data is reduced to the normalized form, which is applied the statistical methods of analysis and big data processing.

Grabb's method for detecting conflicting data consists in the following.

At first there is assessed the sampling's arithmetic mean \hat{y} and mean square deviation $\hat{\sigma}$:

$$\hat{y} = \frac{\sum_{i=1}^n y_i}{n} \tag{1}$$

$$\sigma_y = \sqrt{\frac{\sum_{i=1}^n (y_i - \hat{y})^2}{n - 1}} \tag{2}$$

To specify abnormality y_i there is computed the parameter

$$\lambda_i = \frac{|y_i - \hat{y}|}{\sigma_y} \tag{3}$$

and compared with permissible λ_{per} [29].

If $\lambda_i > \lambda_{per}$, then y_i is considered to be contradictory.

Figure shows 3 the block-scheme of discrepancies detection and elimination, using Grabb's criterion.

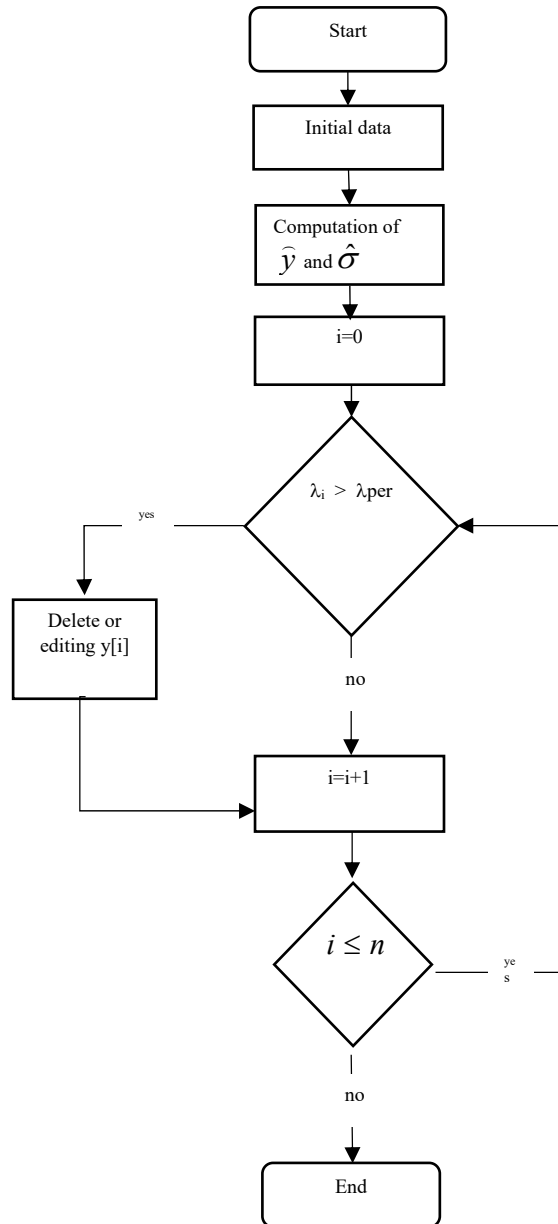


Figure 3: Block-scheme of discrepancies detection and elimination, using Grabb's method

Grubb’s test is applied to assessing cross errors (parasitic errors) of sampling doubtful values from a random magnitude, having normal distribution. The most known and often applied criterion variety is the case, when the parameters of normal distribution – mathematical expectation and general dispersion – are unknown and assessed according to sample mean and sample variance, and for parasitic error there is assessed only one sample value – maximum or minimal. Grubb’s test specifies one outlier per one iteration. That outlier is excluded from the data set and the test is repeated until there are detected all outliers.

Table 3 shows the results of a comparison of the criteria for the detection of gross errors.

Table 3: Gross Error Detection Results

Name of criterion	Error detection in small samples	Error detection in large samples
1. Irwin Method	+	-
2. Student criterion	+	-
3. The criterion of the largest absolute deviation	-	+
4. Maximum relative deviation criterion	-	-
5. Romanovsky criterion	+	-
6. Variational range method	-	+
7. 3 Sigma Criterion	-	+
8. Wright criterion	-	+
9. Grubbs criterion.	-	+
10. Q-test (Dixon)	+	-
11. Lvovsky criterion	+	-
12. Chauvinet criterion	+	-
13. David criterion.	-	+
14. Hoglin-Iglevich criterion	+	+
15. L-test (Titien-Moore test)	+	-
16. Smolyak-Titarenko criterion	-	+
17. Brodsky-Batsan-Vlasenko criterion	-	+
18. Kimber criterion	-	+

4.2. Apriori information adjustment, using statistical methods

Preliminary disambiguation leads to mathematical expectation change and mean square deviation. Therefore, there happens deviation of those values from a priori ones. Accordingly, there occurs the task of mathematical expectation estimation and mean square deviation, as well, of empiric distribution function determination. Solution of the tasks thereof consists of the following basic stages:

- 1) Computation of expectation estimation and mean square deviation;
- 2) Determination of the interval length;
- 3) Detecting of distribution empiric functions;
- 4) Computation of theoretical hitting frequency into the interval;
- 5) Checking the correspondence hypothesis to distribution empiric and theoretical functions, employing the selected criterion (Pearson χ^2).
- 6) Calculating the class marks and hitting frequency into the interval;

Computation of expectation estimation and mean square deviation is executed according to a formula:

$$\hat{m} = \frac{\sum_{i=1}^n x_i}{n} \tag{4}$$

$$\hat{\sigma} = \sqrt{\frac{\sum_{i=1}^n (x_i - \hat{m})^2}{n - 1}} \tag{5}$$

Let’s find the interval value:

$$\Delta x = \frac{x_{\max} - x_{\min}}{1 + 3,322 * \lg n} \tag{6}$$

Let’s hypothesize the random magnitude distribution function with probability distribution density $p(x)$ with mathematical expectation \hat{m} and MSD $\hat{\sigma}$.

Formula of empiric and theoretical distribution functions [30].

$$F_n^*(y) = \frac{1}{n} \sum_{i=1}^n I(x_i < y) \tag{7}$$

$$I(x_i < y) = \begin{cases} 1, & \text{if } x_i < y, \\ 0 & \text{otherwise} \end{cases} \tag{8}$$

$$p(x) = \frac{1}{\sqrt{2\pi} * \hat{\sigma}} * e^{-\frac{(x-\hat{m})^2}{2\hat{\sigma}^2}} \tag{9}$$

In the work herein, to compare empiric and theoretical distribution functions, we use a criterion χ^2 :

$$\chi^2 = \sum_{i=1}^k \frac{(m_i - np_i)^2}{np_i} \quad (10)$$

where $k = \frac{x_{\max} - x_{\min}}{\Delta x}$ - intervals number; m_i -

experimental hitting frequency of variate value into i - interval; np_i - theoretical frequencies.

5. PRACTICAL PART

Every five seconds the employees of Central dispatcher service of Almaty city Transport Holding receive the information about buses location and driving speed. Moreover, the public transport is watched by means of video cameras, installed at every street. Dispatchers trace the situations at roads 24-four hours. All data on traffic congestion, intervals of bus running, dead time at bus stops are analyzed in real mode. That data allows adjust routes and bus number in compliance with citizens' needs.

We have received the data archive for the big data analysis and processing from Almaty city Transport Holding. The latter manages about 114 city buses. All buses and trolleybuses are equipped with GPS-trackers for transport tracing and information receiving in real time mode (Figure 4).

The installed GPS-tracker is directly connected with the terminal ONAI. The data enters the transport holding dispatcher section via satellite GLONASS every second and it is renewed with minimal delay.



Figure 4: GPS-tracker frotcom gv65

If a bus is delayed in the jam, or it has fallen out from the route due to any other reason, the changes will be displayed on the map within several seconds. Application CityBus (Figure 5) in Almaty city is connected to the Holding's base system and it shows the location and routes of the buses at the moment. Complete daily information about buses and routes is recorded and transmitted to the data archive. Figure 5 presents a map of watching over public transport on-line, obtained by means of application CityBus of Almaty city.



Figure 5: Almaty city public transport routes map

Figure 6 shows the architecture of data collection, transmission, analysis and visualization process. Arrows direction denotes the data and information flows.

The data thereof have been collected, united into CSV files, using protocol OPC (one CSV file per day), then it is transmitted to the file server. The

data, being stored in the database, is obtained by the software for high level analysis

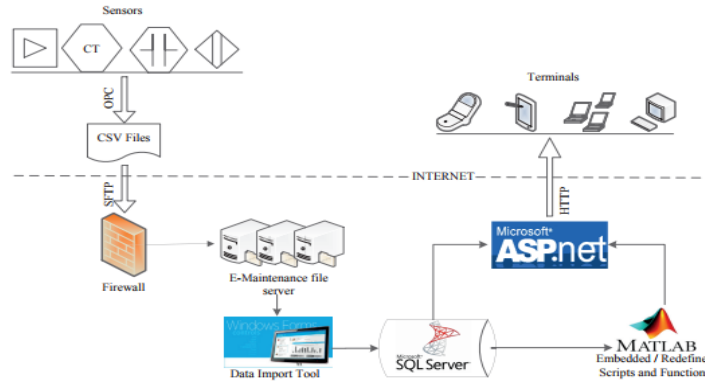


Figure 6: Process of data collection, transmission, analysis and visualization

Obtained from the sensors data is stored in the form of a file csv. The given database encloses complete information on the buses state number plates, bus stops names on a certain route, actual time of arrival to a stop and idle time at a stop.

Total volume of data achieves, obtained from Almaty city Transport Holding is 3 TB.

Figure 7 presents an example of the report on actual and scheduled route traffic in time, denoting stops and idle time (A-starting stop, B-end stop).

Gov.number	A-B	Microdistrict No. 6			Altynsarin / Abay				
	B-A	Railway station "Almaty-1"			Seyfullina / Sholokhov				
		plan	fact	deviation	plan	plan	fact	deviation	plain
582DS02	A-B		06:15 (S)		0:07:01		06:21 (S)		0:02:49
	B-A		07:20 (S)		0:12:43		07:23 (S)		0:01:17
	A-B		08:30 (S)		0:06:39		08:34 (S)		0:00:21
	B-A		09:48 (S)		0:01:10		09:50 (S)		0:00:28
	A-B		10:46 (S)		0:10:03		10:48 (S)		0:00:35
	B-A		12:31 (S)		0:44:58		12:36 (S)		0:02:34
	A-B		13:42 (S)		0:08:12		13:45 (S)		0:00:42
	B-A		15:12 (S)		0:31:35		15:15 (S)		0:01:24
	A-B		16:22 (S)		0:06:53		16:28 (S)		0:01:59
	B-A		17:30 (S)		0:02:34		17:32 (S)		0:01:17
	A-B		18:54 (S)		0:02:06		18:56 (S)		0:00:28
	B-A		19:49 (S)		0:05:14		19:51 (S)		0:00:42

Figure 7: Actual and scheduled route traffic in time, denoting stops and idle time

As an example, let's take the travel time from the starting stop to an end stop of the route 72 (Table

4). Table 4 presents an actual daily trip time of the bus route 72.

TABLE 4: Data on the route №72 per one day (N- route number, t_{att} - actual trip time).

N	t _{att}	№	t _{att}	№	t _{att}	№	t _{att}	№	t _{att}	№	t _{att}	№	t _{att}
1	56	21	70	41	49	61	69	81	58	101	62	121	59
2	59	22	58	42	30	62	77	82	62	102	58	122	37
3	58	23	62	43	60	63	49	83	63	103	60	123	55
4	69	24	61	44	63	64	52	84	63	104	68	124	62
5	59	25	70	45	53	65	49	85	68	105	61	125	45
6	55	26	52	46	58	66	59	86	75	106	61	126	63
7	61	27	62	47	64	67	66	87	49	107	62	127	65
8	59	28	77	48	69	68	60	88	60	108	76	128	78
9	61	29	47	49	64	69	63	89	62	109	67	129	55
10	63	30	60	50	57	70	50	90	68	110	50	130	55

11	69	31	62	51	53	71	55	91	62	111	59		
12	52	32	58	52	57	72	61	92	64	112	72		
13	49	33	62	53	51	73	63	93	62	113	49		
14	55	34	65	54	59	74	67	94	61	114	92		
15	61	35	83	55	76	75	62	95	64	115	59		
16	62	36	49	56	47	76	64	96	65	116	63		
17	61	37	58	57	60	77	58	97	74	117	57		
18	69	38	58	58	58	78	59	98	48	118	69		
19	60	39	62	59	79	79	72	99	62	119	63		
20	50	40	59	60	64	80	60	100	66	120	58		

The software part has been implemented in Python 3.8. Used scripts: sympy, numpy, matplotlib.pyplot as plt, math, tkinter, faker, time. The interface “Identification and elimination of contradictions methods” has been created, as shown

in Figure 8. Three methods are considered herein: k means, Grabbs criterion, and Statistical Processing for identifying and eliminating conflicting data.

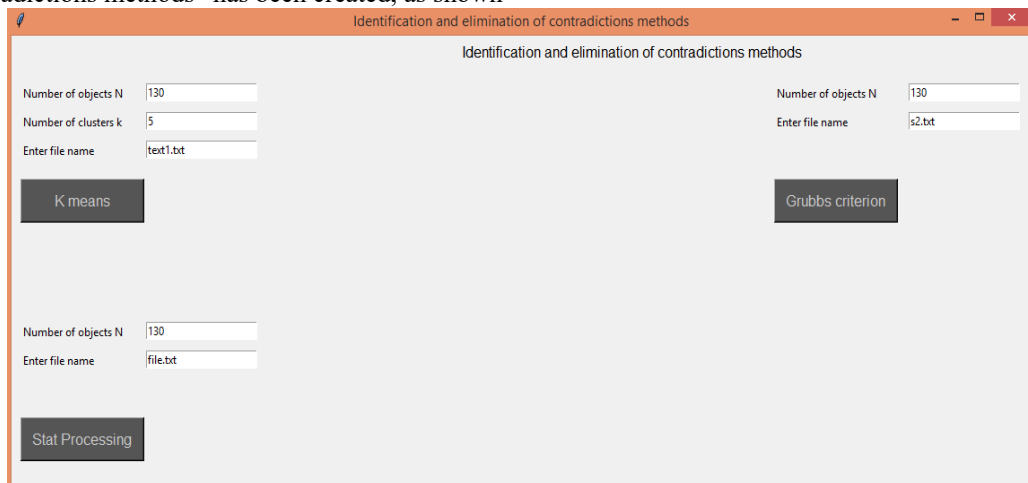


Figure 8: Interface «Identification and elimination of contradictions methods»

To apply the k means method [31], you need to enter the number of objects and clusters, as well as select a file and click the "k means" button.

The result of dividing the data into 5 classes is presented in Figure 9. In the figure an axle x denotes bus trip actual time from starting to an end stop, and an axle y - number of bus routes.

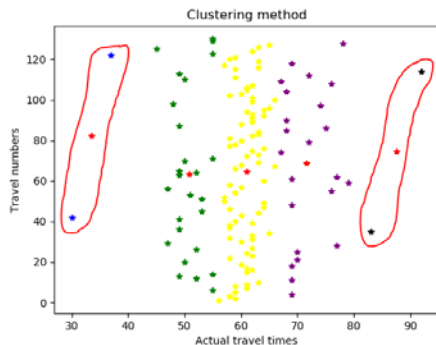


Figure 9: The result of splitting data into 5 classes

When the “Grabbs criterion” button is clicked, we get the mean square deviation, average value and outliers of the first and second iteration according to the Grabbs criterion in the results window (Figure 10).



Figure 10: Grubbs test results

At applying Grubbs method there has been adjusted the data 42 (with value 30), 114 (with value 92) and 122 (with value 37), 35 (with value 83).

The results of the first and second iteration using the Grubbs method are presented in Figures 11 and 12.

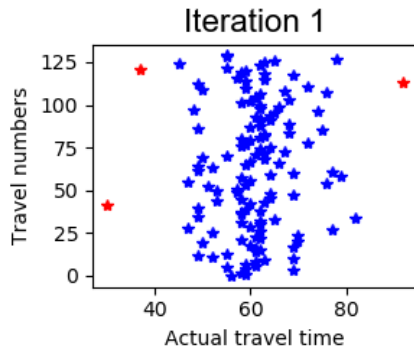


Figure 11: The result of the first iteration

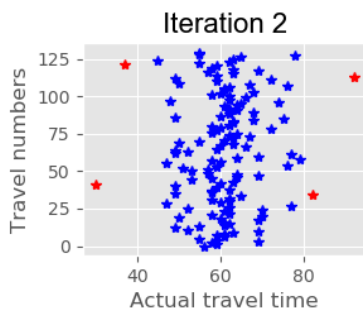


Figure 12: Result of the second iteration

The numbers of the conflicting data from the last iteration are consistent with the conflicting data, obtained by the k means method (Figure 9).

Subsequent to data adjustment according to the above described methodology, we obtain theoretical and experimental distributions of buses trip time (Fig.13).

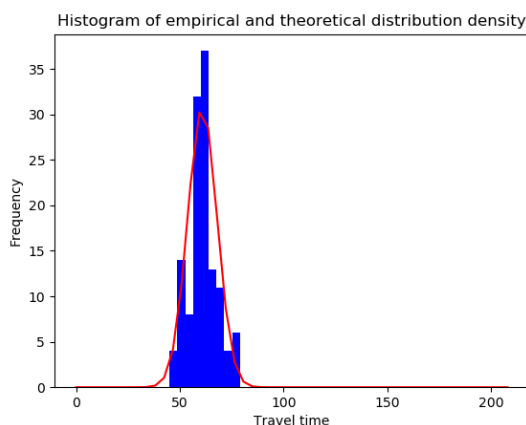


Figure 13: Column diagram of empiric and theoretical density distribution

In the Figure an axle x denotes the bus trip time, and an axle y - scale of events hitting frequency.

Computed value $\chi^2 = 6.63$, which is less, than 9.21 for significance level 0.1. It means, that with probability 0.9 it might be confirmed, that theoretical and experimental distribution functions coincide.

Thereat, estimation of expectation has constituted - 60, and mean square deviation - 7.28.

Trip passing time according to a priori data (per plan) amounts to 50 minutes, and computation results - 60. Therefore, it is necessary to correct the schedule for 10 minutes.

CONCLUSION

We have carried out analytical review of existing works on the thematic under study and demonstrated work's actuality.

In the work we have offered the methodology of discrepancies detection and elimination in large-scale transport data, as well, the statistical method for adjusting a priori information. For that aim there is first fulfilled preliminary detecting and eliminating of discrepancies, and further, cleaned data is used for adjusting the scheduled data.

Preliminary detection and elimination of discrepancies in big transport data has been executed employing Grubbs method and clustering (k-average method). Outcomes, obtained with those methods for the being considered example, coincide.

Received data subsequent to pre-processing has been used for getting the trip time statistical characteristics, which have been applied to their adjustment. At that, it has been shown, that the trip time distribution corresponds to normal law with a probability of 0.9. In the result of statistical processing the trip time of the selected route has come to 60 minutes, and scheduled time composes 50 minutes. It means, that there is required the schedule adjustment for 10 minutes.

Proposed methodology has been implemented in Python software medium.

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