

A NOVEL TWO-DIMENSIONAL SPECTRAL/SPATIAL HYBRID CODE FOR OPTICAL CODE DIVISION MULTIPLE ACCESS SYSTEM

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ABSTRACT

A newly two-dimensional hybrid code based on Zero Cross Correlation (ZCC) and Multi Diagonal (MD) codes (2D ZCC/MD) has been proposed for incoherent spectral/ spatial OCDMA system in this paper in order to suppress MAI and mitigate PIIN. The 2D ZCC/MD keep the zero cross correlation property since the both of Zero Cross Correlation (ZCC) and Multi Diagonal (MD) codes have zero cross correlation property. Using the direct detection technique the proposed code is analysed where the performance of 2D ZCC/MD code is compared with existing 2D FCC/MDW and 2D DPDC. The analytical results prove that at low BER and high data 2D ZCC/MD can support more simultaneous user.

Keywords: *Optical Code Division Multiple Access (OCDMA), Multiple Access Interference (MAI), Zero Cross-Correlation Code (ZCC), Multi-Diagonal code (MD), Phase Induced Intensity Noise.*

1. INTRODUCTION

OCDMA (Optical Code Division Multiple Access) is a huge research area where it attracts many interesting research for decades. The importance of the system lies in the acquisition of certain characteristics that allow it to be interesting technique such as flexibility in high speed access network, high security, dynamic bandwidth assignment, large and effective bandwidth utilization [1]. OCDMA can be divided into five important schemes: frequency hopping [2], [3], time spreading [4], [5], spectral amplitude coding (SAC) [6], [7] and spatial coding [8], [9]. Due to the ability of suppression of Multiple Access Interference (MAI) completely by the spectral coding and mitigation Phase Induced Intensity Noise (PIIN), the spectral amplitude coding (SAC-OCDMA) has attracted a more interest recently [10], [11].

OCDMA can be classified into coherent and incoherent categories. A coherent OCDMA system is costly due to the high cost of the light source as a mode-locked laser while an incoherent OCDMA is cheaper and more suitable in optical network [12].

OCDMA can be implemented in one-dimensional (1D) [13], [14], two-dimensional (2D) [15], [16] or three-dimensional (3D) [17] for the main purpose to suppress Multiple Access Interference (MAI) and mitigation of Phase Induced Intensity Noise (PIIN) [18]. Many codes are introduced in two dimensional in order to overcome the obstacle of one dimensional as: 2-D diluted perfect difference (2-D DPD) spectral/spatial code provided by Yeh et al., based on the 1-D PD code and the dilution method [19], [20], 2-D spectral/spatial code based on modified quadratic congruence (MQC) code developed by Yin, et al. [21], 2-D spectral/spatial modified double weight code optical code division multi-access system (2D MDW) developed by Arief, A. R. and Aljunid, S. A [22], 2D wavelength/time hybrid Flexible Cross Correlation/Modified Double Weight (FCC/MDW) provided by Nui [23], [24].

In the present paper we propose a new two-dimensional hybrid ZCC/MD code established from the combination of 1D ZCC (Zero Cross Correlation) and 1D MD (Multi Diagonal) to recover the performance of the OCDMA system where the paper is arranged as follow: section 2 focused on the 2D hybrid ZCC/MD code

construction. Section 3 presents system description. Section 4 presents the system performance where the numerical results and discussion are exhibited on the section 5. the last section gives the conclusion.

2. 2D HYBRID ZCC/MD CODE CONSTRUCTION

Based on the combination of 1D MD code [7] and 1D ZCC code [25], the 2D-ZCC/MD code can be constructed. Let $X = \{x_0, x_1, x_2, \dots, x_{M-1}\}$, $Y = \{y_0, y_1, y_2, \dots, y_{N-1}\}$ With k_1 code weight of 1D-ZCC code and k_2 code weight of 1D-MD code. Denoted that w_1 is the code size of 1D-ZCC code and w_2 is the code size of 1D-MD code, so the code length of X, Y are $M = k_1 w_1, N = k_2 w_2$ respectively. $W = w_1 w_2$ represents the code size of 2D-ZCC/MD.

2.1. 1D Zero Cross Correlation (ZCC) code

The Zero Cross Correlation (ZCC) code for SAC OCDMA was developed by Anuar et al (2009).[25] ZCC is designed with zero cross correlation property between its code words to improve the performance of SAC OCDMA system. ZCC is characterized by a matrix of $K \times L$ where K represents number of active users and L represents the minimum code length. The number of active user K and code length L are given as:

$$K = w + 1 \tag{1}$$

$$L = w(w + 1) \tag{2}$$

The construction of the code is designed from the modified double weight (MDW) code [26] where the matrix is generated as follow with the basic ZCC code ($w=1$):

$$ZCC(w = 1) = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \tag{3}$$

According to the following map, the increase of the number of users is occurred:

$$ZCC(w = 2) = \begin{bmatrix} 0 & Z_1 \\ Z_1 & 0 \end{bmatrix} \tag{4}$$

$$ZCC(w = 3) = \begin{bmatrix} 0 & Z_2 \\ Z_2 & 0 \end{bmatrix} \tag{5}$$

The number of code weight can be increased by the general transformation below:

$$ZCC_w = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \tag{6}$$

Where:

A : is $[1, w(w - 1)]$ matrix of zeros.

B : represents w replication of the matrix $\sum_{j=1}^w j[0,1]$.

C : contain of the duplication of the matrix from $w - 1$.

D : is the diagonal pattern of $[m \times n]$ with exchange column of zeros matrix $[m \times n]$.

An example for the transformation code from $w = 1 \rightarrow w = 2 \rightarrow w = 3$ as follow:

$$ZCC_{w=1} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \tag{7}$$

$$ZCC_{w=2} = \begin{bmatrix} \overset{A}{\downarrow} & \overset{B}{\downarrow} \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 \\ \underset{C}{\uparrow} & \underset{D}{\uparrow} \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \tag{8}$$

$$ZCC_{w=3} = \begin{bmatrix} \overset{A}{\downarrow} & \overset{B}{\downarrow} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ \underset{C}{\uparrow} & \underset{D}{\uparrow} \\ & & & & & & & & & & & & & \end{bmatrix} \tag{9}$$

2.2. 1D Multi Diagonal (MD) code

One-dimensional Multi Diagonal (1D MD) was been developed by [7]. It is characterized by N (code length), w (code weight) and λ_c (in phase cross correlation)

For the code sequence $X = \{x_1, x_2, \dots, x_N\}$, $Y = \{y_1, y_2, \dots, y_N\}$. The cross correlation expression can be expressed by $\lambda_c = \sum_i^N x_i y_i$

1D MD (Multi Diagonal) possesses zero cross correlation $\lambda_c = 0$.

The matrix of 1D MD code consists of $K \times N$ where K is the number of user, N is the code length. The choice of the weight value is free and $N = Kw$. The 1D MD code can be designed as below:

Step1:

A sequence of diagonal matrix can be constructed using the value of the weight (w) and number of user (K), according to these value the i ($i = 1, 2, 3, \dots, K$) is the index of rows in each matrix and j ($j = 1, 2, 3, \dots, w$) where j is the number of diagonal matrix.

Step2:

The MD sequences can be computed for each diagonal matrix using the equation below:

$$S_{i,j_w} = \begin{cases} (i_n + 1 - i), j_w = \text{even} \\ i \quad \text{for } j_w = \text{odd} \end{cases} \quad (10)$$

$$S_{i,1} = \begin{bmatrix} 1 \\ 2 \\ 3 \\ \vdots \\ \vdots \\ K \end{bmatrix}, S_{i,2} = \begin{bmatrix} \cdot \\ \cdot \\ \cdot \\ \cdot \\ 3 \\ 2 \\ \cdot \\ 1 \end{bmatrix}, S_{i,3} = \begin{bmatrix} 1 \\ 2 \\ 3 \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ K \end{bmatrix}, \dots \quad (11)$$

Each element of the $S_{i,j}$ matrices represents the position of one in $T_{i,j}$ matrices with $K \times K$ dimensions.

Where

$$T_{i,1} = [S_{i,1}]_{K \times K}, T_{i,2} = [S_{i,2}]_{K \times K}, \dots, T_{i,w} = [S_{i,w}]_{K \times K} \quad (12)$$

$$T_{i,1} = \begin{bmatrix} 1 & 0 & \dots & 0 \\ 0 & 1 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \dots & \dots & 1 \end{bmatrix}_{K \times K}, T_{i,2} = \begin{bmatrix} 0 & \dots & 0 & 1 \\ 0 & \dots & 1 & 0 \\ \dots & \dots & \ddots & \vdots \\ 1 & \dots & \dots & 0 \end{bmatrix}_{K \times K}, \dots, T_{i,w} = \begin{bmatrix} 1 & 0 & \dots & 0 \\ 0 & 1 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \dots & \dots & 1 \end{bmatrix}_{K \times K} \quad (13)$$

Step3:

The construction of the matrix of MD code of power $K \times N$ is based on the combination of diagonals matrices. In a matrix each row is a single code sequence.

$$MD = [T_{i,1} : T_{i,2} : \dots : T_{i,w}]_{K \times N} \quad (14)$$

$$MD = \begin{bmatrix} a_{1,1} & a_{1,2} & \dots & a_{1,N} \\ a_{2,1} & a_{2,2} & \dots & a_{2,N} \\ a_{3,1} & a_{3,2} & \dots & a_{3,N} \\ \vdots & \vdots & \dots & \vdots \\ a_{i_n,1} & a_{i_n,2} & \dots & a_{i_n,N} \end{bmatrix} \quad (15)$$

The following table give an example of MD code with $K = 4$, $w = 3$

Table1: The MD Code With $K = 4$, $w = 3$

i	Code sequence
1	1 0 0 0 0 0 0 1 1 0 0 0
2	0 1 0 0 0 0 1 0 0 1 0 0
3	0 0 1 0 0 1 0 0 0 0 1 0
4	0 0 0 1 1 0 0 0 0 0 0 1

The cross correlation of newly code can be obtained using four characteristics are given as follow:

$$A^0 = Y^T X \quad (16)$$

$$A^1 = Y^T \bar{X} \quad (17)$$

$$A^2 = \bar{Y}^T X \quad (18)$$

$$A^3 = \bar{Y}^T \bar{X} \quad (19)$$

Where $A(d)$, $d \in (0, 1, 2, 3)$ has been given in [9] represents the characteristic matrices. Where parameters \bar{X} and \bar{Y} are the complementary of X

and Y respectively. The cross correlation of hybrid 2D ZCC/MD code $A^{(d)}$ and $A_{g,h}$ is formulated as:

$$R^{(d)}(g, h) = \sum_{M=1}^{M-1} \sum_{N=1}^{N-1} a_{ij}^{(d)} a_{(i+g)(j+h)} \quad (20)$$

Where $a_{ij}^{(d)}$ depicts the $(i, j)_{th}$ of $A^{(d)}$ and $a_{(i+g)(j+h)}$ is the $(i, j)_{th}$ of $A_{g,h}$. TableII shows the cross correlation between any two codes $A^{(d)}$ and $A_{g,h}$ of 2D Hybrid ZCC/MD code produced from the equation (20).

Tableii: Cross Correlation Of 2D ZCC/MD Hybrid Code

	$R^{(0)}$	$R^{(1)}$	$R^{(2)}$	$R^{(3)}$
$g = 0, h = 0$	$k_1 k_2$	0	0	0
$g = 0, h \neq 0$	0	$k_1 k_2$	0	0
$g \neq 0, h = 0$	0	0	$k_1 k_2$	0
$g \neq 0, h \neq 0$	0	0	0	$k_1 k_2$

The cross correlation of $A_{0,0}^0$ and $A_{g,h}$ can be calculated as follows:

$$R^{(0)}(g, h) = \sum_{i=1}^{M-1} \sum_{j=1}^{N-1} a_{i,j}^{(0)} a_{i,j}(g, h) = \begin{cases} k_1 k_2 & \text{for } g = 0, h = 0 \\ 0 & \text{otherwise} \end{cases} \quad (21)$$

3. SYSTEM DESCRIPTION

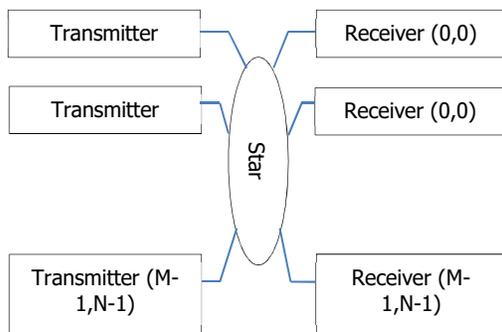


Figure1: Block Diagram Of A 2D Hybrid ZCC/MD Spectral/Spatial OCDMA System

Based on the direct detection technique, 2D ZCC/MD is designed as illustrated in Figure1. It consists of $w_1 w_2$ pairs of transmitters and receivers, the star coupler to connect the transmitter and the receiver. Using the assigned codeword, the incoming data will be encoded and transmitted to the receiver via star coupler. At the receiver, the encoded data will be decoded through up one combiner and all codewords from different users are correlated. Figure2 shows the construction of 2D ZCC/MD transmitter, it consists of incoherent light source (BLS), to send the data, an electrical to optical modulator (EOM) to modulate the signal coming from BLS, one splitter for the spectral encoding, two (2) Fiber Bragg Grating (FBG) with the same number of grating but opposite arrangement for the spatial encoding. The incoming data from BLS will be converted to the optical signal through EOM with ON-OFF Keying format; this modulated data will pass through the FBG1 for the spectral encoding purpose according to X_g the spectral code sequence. The spectral components of optical pulse either matched to 1s of a code are filtered back and the other are filtered out. FBG2 is designed to compensate the delay of the set of FBG1 matched spectral components. These matched spectral components transmit to optical splitter where these are split into k_2 equal parts to send it to the star coupler according to the code sequence of Y_h . At this phase, the optical signal is encoded in two dimensions.

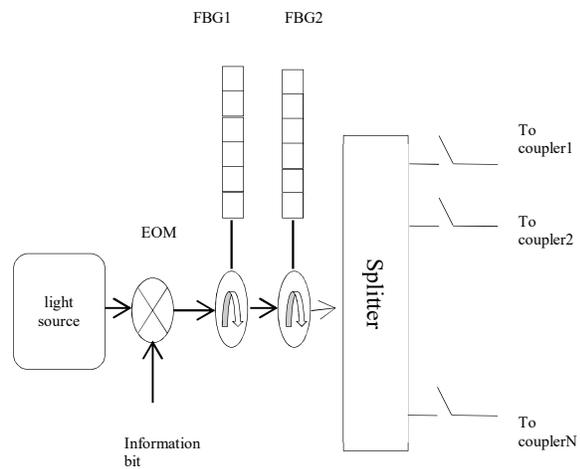


Figure 2: The Construction Of Transmitter

Figure3 depicts the construction of the receiver where it is designed in order to suppress MAI and used as information bit recovery. It consists of one

combiner, one direct detection technique part and one integrator. The direct detection technique part in turn consists of two sets of Fiber Bragg Grating (FBG1 and FBG2), two circulators and one Photo detector (PD). The incoming spatial code sequence Y_h from the star coupler are received and combined by the combiner. The spectral components which are matched to “1s” of the spectral code sequence X_g are reflected back by FBG1. FBG2 with the same grating but opposite arrangement used to compensate the run-trip delay. The photo detectors (PD) convert the optical signals to electronic signals and then pass them to the integrator.

$$\tau = \frac{\int_0^\infty S(v)^2 dv}{\left[\int_0^\infty S(v)\right]^2} \tag{22}$$

Where $S(v)$ consists the single sideband power spectral density. To simplify the analysis, four assumptions are made [9]:

We defined $U(v, i)$ as follows:

$$U(v, i) = \left\{ u \left[v - v_0 - \frac{\Delta v}{2M} (-M + 2i) \right] - u \left[v_0 - \frac{\Delta v}{2M} (-M + 2i + 2) \right] \right\} \tag{23}$$

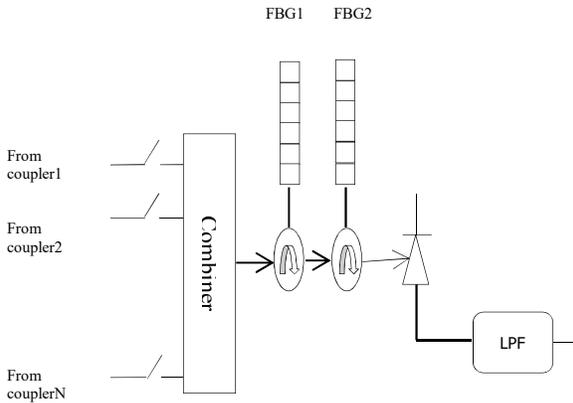


Figure3: The construction of the receiver.

4. SYSTEM PERFORMANCE

According to the zero cross correlation property of the code 2D ZCC/MD, there is no overlapping in a spectra of different users, thus the effect of MAI have been removed. The effects of thermal noise, PIIN, and shot noise in the photo-detector have been considered in the analysis. The Gaussian approximation is employed to calculate the BER. The total noise photocurrent variance can be expressed as follow:

$$\begin{aligned} \langle i_{noise}^2 \rangle &= \langle i_{PIIN}^2 \rangle + \langle i_{shot}^2 \rangle + \langle i_{therm}^2 \rangle \\ &= BI^2\tau + 2eBI + \frac{4K_b T_n B}{R_L} \end{aligned} \tag{21}$$

Where e is the electron charge, I is the average photocurrent. B is the electrical bandwidth, T_n is the absolute temperature, K_b is Boltzmann's constant, R_L is the load resistance and τ is the coherence time of the light which expressed as:

TableIII: The 2D ZCC/MD code with $(k_1 = 3, w_1 = 3, k_2 = 2, w_2 = 3)$

$A_{g,h}$	$X_1 = [1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0]$	$X_1 = [0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0]$	$X_2 = [0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1]$ X_h
$Y_1^T = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1 \end{bmatrix}$
$Y_2^T = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$
$Y_3^T = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0 \\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0 \\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$	$\begin{bmatrix} 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 1 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \end{bmatrix}$
Y_g			

$$I = R \int_0^\infty G(v)dv$$

Where $U(v, i)$ is a unit step function defined as:

$$u(v) = \begin{cases} 1 & v \geq 0 \\ 0 & v < 0 \end{cases} \quad (24)$$

$$\begin{aligned} &= \int_0^\infty \frac{P_{sr}}{k_2 \Delta v} \sum_1^W d(w) R^0(i, j) U(v, i) dv \\ &= \frac{P_{sr} \Delta v}{k_2 \Delta v M} [k_1 k_2 + \sum_1^W d(w) R^0(i, j)] \end{aligned}$$

The power spectral density (PSD) of the received signals can be written as

$$r(v) = \frac{P_{sr}}{k_2 \Delta v} \sum_1^K d(k) \sum_{j=0}^{P-1} \sum_{i=0}^{M-1} a_{(i,j)}(k) U(v, i) \quad (25)$$

Where k_1 and k_2 are the code weights of spectral and spatial respectively, P_{sr} is the effective source power at the receiver, N and M are the code lengths of spatial and spectral code sequences respectively, W is the number of active users, $d(k)$ is the data bit of W_{th} user which can be "1" or "0" and $a_{(i,j)}$ is an element of the k_{th} user's codeword. depending on the cross correlation between $A_{0,0}^{(0)}$ and $A_{g,h}$ obtain the output currents of PD at receiver $(0,0)$ is obtained as follows:

Where η is the quantum efficiency of the photo-diode, R is the responsivity of the photo-diode given by $R = \eta e / h \nu_0$ and h is Plank's constant. Since, $M = w_1 k_1$ and $W = w_1 w_2$, then:

$$I = \frac{R P_{sr} w_2}{W} \quad (27)$$

Phase Induced Intensity Noise (PIIN) can be calculated as:

$$\begin{aligned} \langle i_{PIIN}^2 \rangle &= B I^2 \frac{\int_0^\infty G_0^2(v) dv}{[\int_0^\infty G_0(v) dv]^2} \\ &= B R^2 \int_0^\infty [G^2(v)] dv \\ &= B R^2 \int_0^\infty \left[\frac{P_{sr}}{k_2 \Delta v} \sum_{k=1}^K d(k) R^0 U(i, j) \right]^2 dv \end{aligned}$$

$$= \frac{BP_{sr}^2 R^2}{k_2^2 \Delta v^2 M} \left[k_1 k_2 + \underbrace{\sum_{k=1}^K d(k) R^0(i, j)}_0 \right]^2$$

$$= B \frac{R^2 P_{sr}^2 w_2 k_1}{\Delta v W} \quad (28)$$

Consequently, the total noise where the probability of each user sending bit 1 is equal so:

$$\langle i_{noise}^2 \rangle = \langle i_{PIIN}^2 \rangle + \langle i_{shot}^2 \rangle + \langle i_{thermal}^2 \rangle \quad (29)$$

$$\langle i_{noise}^2 \rangle = BI^2 \tau + 2eBI + \frac{4K_b T_n B}{R_L} \quad (30)$$

From the previous equations I_{noise} can written as

$$\langle i_{noise}^2 \rangle = \langle i_{PIIN}^2 \rangle + \langle i_{shot}^2 \rangle + \langle i_{thermal}^2 \rangle$$

$$\langle i_{PIIN}^2 \rangle = B \frac{R^2 P_{sr}^2 w_2 k_1}{\Delta v W} \quad (31)$$

$$\langle i_{shot}^2 \rangle = 2eB \frac{RP_{sr} w_2}{W} \quad (32)$$

$$\langle i_{thermal}^2 \rangle = \frac{4K_b T_n B}{R_L} \quad (33)$$

$$\langle i_{noise}^2 \rangle = \frac{BR^2 P_{sr}^2 k_1^2}{\Delta v W} + 2eB \frac{RP_{sr} w_2}{W} + \frac{4K_b T_n B}{R_L} \quad (34)$$

Note that the probability of sending bit “1” at any time for each user is 1/2:

$$\langle i_{noise}^2 \rangle = \frac{BR^2 P_{sr}^2 k_1^2}{2\Delta v W} + \frac{eBRP_{sr} w_2}{W} + \frac{4K_b T_n B}{R_L} \quad (35)$$

Finally, the average signal to noise ratio (SNR) can be calculated as

$$SNR = \frac{I^2}{\langle i_{noise}^2 \rangle} = \frac{\left[\frac{RP_{sr} w_2}{W} \right]^2}{\frac{BR^2 P_{sr}^2 k_1^2}{2\Delta v W} + \frac{eBRP_{sr} w_2}{W} + \frac{4K_b T_n B}{R_L}} \quad (36)$$

from SNR, The BER can be expressed as follows:

$$BER = \frac{erfc\left(\sqrt{\frac{SNR}{8}}\right)}{2} \quad (37)$$

Where

$$erfc = \frac{2}{\sqrt{\pi}} \int_0^\infty \exp(-y^2) dy \quad (38)$$

Table IV : Link parameters

PD quantum efficiency	$R = 0.75$
Spectral width of broadband light source	$\Delta\lambda = 30nm$ ($\Delta\lambda = 3.75$)
Operating wavelength	$\lambda_0 = 1.55\mu m$
Electrical bandwidth	$B = 320MHz$
Data transmission rate	$R_b = 622Mbps$
Receiver noise temperature	$T_n = 300K$
Receiver load resistor	$R_L = 1030\Omega$
Boltzmann's constant	$K_b = 1.38 \times 10^{-23} W / K/Hz$
Electron charge	$e = 1.60217646 \times 10^{-19} coulombs$
Light velocity	$C = 3 \times 10^8 m/s$

5. RESULTS AND DISCUSSION

TableV exhibits the parameters used to analyze the performance of the 2D ZCC/MD code and obtain the numerical results.

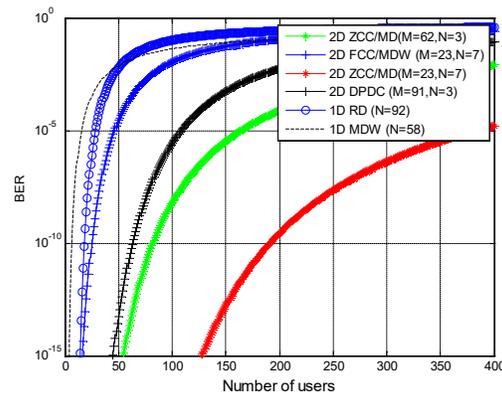


Figure4: BER Against Number Of Users Where Data Rate Is $R_b=1Gbps$ And Effective Power Is $P_{sr}=-10dbm$

Figure4 shows the variation of BER versus the number of users of the codes 2D ZCC/MD (M=63, N=3) compared to 2D DPDC (M=91, N=3), 2D

FCC/MDW (M=23, N=7), 2D ZCC/MD (M=23, N=7), 1D RD (N=92) and 1D MDW (N=58) where effective power P_{sr} equal to -10dBm and data rate $R_b=1$ Gbps. It can be seen that 2D ZCC/MD exhibit the better performance than other codes. At BER equal to 10^{-9} the 2D ZCC/MD (M=23, N=7) can support until 210 user.

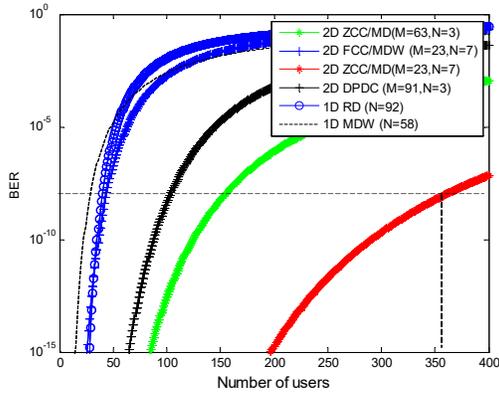


Figure5: BER Versus Number Of Users With Data Rate Is $R_b=2.5$ Gbps And Effective Power Is $P_{sr}=-10$ dbm

Figure5 illustrates also the variation of the BER versus number of user of the same codes but with $P_{sr}=-10$ dBm and data rate $R_b=2.5$ Gbps. This figure confirms the observations given by the previous figure. It can be clearly seen that number of user is increased where for the 2D ZCC/MD (M=23, N=7) code can reach 315 user at BER equal to 10^{-9} .

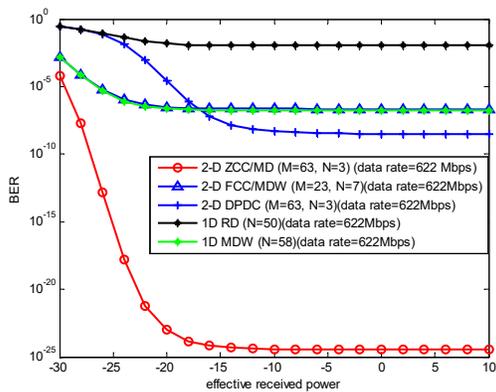


Figure6: BER Versus Effective Power P_{sr} When $K=100$ User And Data Rate Is $R_b=622$ Mbps

Figure6 shows the relation between the BER and the effective power in dBm when the number of user is equal to 100 and data rate equal to 622Mbps. The figure apparent that 2D ZCC/MD (M=23, N=7) is the best at high power and it has a minimum BER

-24 comparing to the other codes. 2D ZCC/MD indicates that the superior performance is coming from the ability of the code to fully to suppress the effect of the MAI and mitigate PIIN.

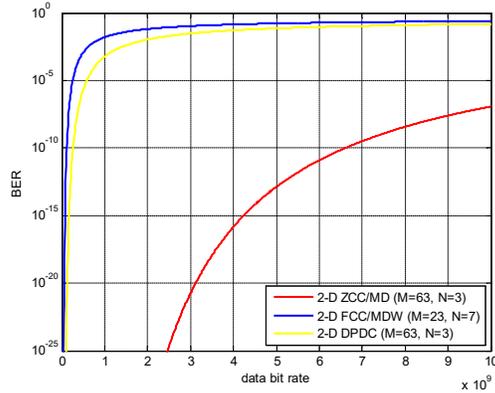


Figure7: BER Versus Data Rate When The Effective Power Is $P_{sr}=-10$ dbm And The Number Of User Is $K=100$ User.

Figure7 shows the variation of BER versus the data transmission rate of each user with similar code length when the number of user is 100 and the effective source power -10 dBm. At the BER equal to 10^{-9} , the figure demonstrates that 2D ZCC/MD can accommodate the higher data transmission rate for each user with a similar code length is used compared to the other codes.

6. CONCLUSION

The OCDMA is an interesting scheme due to characteristic such as: flexible bandwidth, asynchronous access, flexibility of implementation differential QOS and ability to support multimedia services. A newly two dimensional code has been proposed referred as 2D hybrid code for spectral/spatial OCDMA system. The construction of this code is based on the combination of 1D ZCC code and 1D MD code. The performance of this new code has been evaluated by using the analytical analysis. The proposed code has the MAI suppression property where the proposed system has a low BER. The proposed code represents the better performance compared to other codes so the system could robustly accommodate more users.

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