MODELING AND QUERYING SPATIOTEMPORAL MULTIDIMENSIONAL DATA ON SEMANTIC WEB: A SURVEY

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ABSTRACT
The usage of “web of data” for decision making has increased with the presence of On-Line Analytical Processing (OLAP), Data Warehouse (DW), Multidimensional (MD) data, and Semantic Web (SW) technologies. These technologies are converging into technology that utilizes data on the web to obtain important information as the basis of crucial decision making. The implementation of these technologies continues to grow along with data published on the web using vocabularies like SDMX, QB, and QB4OLAP for linked cube data. Along with increasing analysis complexity, spatiotemporal OLAP emerges as a tool to obtain sophisticated, better, and more intuitive analysis results than OLAP. Vocabulary for spatial OLAP on the Semantic Web has been constructed, namely QB4SOLAP, and successfully implemented. Query language extension for SW was built significantly, but the fundamental model of more dynamic spatial (spatiotemporal) multidimensional data for OLAP on the SW still lacks to exhibit and implemented, even Spatiotemporal DW has been widely studied. This paper presents state-of-the-art research results and outlines future research challenges in Spatiotemporal multidimensional data on the semantic web. This paper organized into three parts, the first part (1) discusses the convergence of OLAP / DW and SW, the second part (2) discusses DW, and spatiotemporal DW on the SW based on the model and the query, and (3) discusses future research opportunities.

Keywords: Spatiotemporal, Multidimensional Data, Semantic Web, Modeling, Querying

1 INTRODUCTION
Business Intelligence (BI) is a technology for collecting, transforming, and presenting data for analysis as a tool for supporting decision making. BI uses Data Warehouse (DW), Multidimensional (MD) data, and Online Analytical Processing (OLAP) that has proven to be useful for obtaining information and knowledge relevant to the business [1]. A Data Warehouse (DW) is a tool that gathers, transforms, and loads data from transactional databases and external sources to provide information to decision-makers. DW has to be maintained in a consistent and consolidated method. The technologies related to DW is OLAP multidimensional (MD) data processing. MD models defined observation as a fact and dimension in a star or snowflake scheme table and queried using de facto standard language Multi-Dimensional Expression (MDX). BI technology has been widely adopted by proprietary or open-source software and massively used by organizations.

At the same time, Semantic Web (SW), as a concept of sharing data on the web, attracts many scientists more than a decade. SW has a visioner method to represent data on the web in a machine recognizable way and could add semantic annotation so that information on the web could be retrieved and processed by computer or human effectively. SW technologies create a new paradigm of integration data, transparency data, semantically linked data using description logic for inference tasks, and in the end, may boost economic growth [2]. SW creates a large-scale Web of Data in the form of semi-structured data and information in the Web[3]. SW accurately exploit data published on the web. SW sets shared vocabularies, semantically expresses metadata, and provides data annotations over web data with semantic through RDF and ontology,
which then generates Semantic Linked Data (e.g.: Linked Data, Linked Open Data, and Government Linked Open Data). The availability of the web of data can be access using query language named SPARQL with its endpoint.

Business and Government have published their data in SW with an open concept, which produces large amounts of valuable data in the form of semi-structured data, flexible and machine-readable. Impressive examples are Dbpedia [4], data.gov, geonames, and data.gov.uk. The field of health and life science is also massively utilizes linked data, namely: UMLS [5], SNOMED-CT, GALEN, GO, Bio2RDF, Linked Life Data, and Linking Open Drug Data. They launch an open data portal to provide data access as statistical data [6]. The statistical data have multidimensional characteristics.

In the modern and competing environment, there is an urgent requirement of tools that able to exploit, analyze, and summarize all statistical data from “web of data” resources. The exploitation of a statistical web of data became popular in the last few years. The government institutions has published their statistical data using cube vocabulary, and has reach 61.75% of their domain. Consequently, many developments focused on using, validating, and visualizing this statistical datasets [7]. Many researchers have been work intensively to implement the concept of BI on the SW. Implementation BI on the SW has many issues, the first issue is OLAP modeling on the SW, the second is the integration process from disperse data source to the DW, and the last issue is data access using query language. Moreover, some researchers worked with system architecture and implementation, user interface design, dataset, and applications of the SW for BI.

Along with increasing analysis complexity, spatiotemporal OLAP emerges as a tool to obtain better and more intuitive analysis results than OLAP. Spatiotemporal OLAP is a combination of GIS and OLAP that could handle spatial data objects, temporal data objects, temporal-spatial types or moving objects and evolving data warehouse dimensions. An enormous volume of geographic/spatial data has been published using SW, yielding the need for Spatial OLAP for analysis spatial or non-spatial data. Spatial OLAP has been modeled on SW by QB4SOLAP vocabulary, which supports spatial operators and algorithms for spatial aggregate SPARQL querying [8].

Although, the research on spatiotemporal OLAP/DW or moving objects have been attracted to many researchers in the last decade because of the wide availability of devices that track the position of moving objects, modeling and querying spatiotemporal OLAP on the SW still lack the significant foundation of treatment. Deep analytic support for spatiotemporal OLAP on SW data is very valuable, it needs modeling and querying that consist of function, methods, manipulation techniques, and vocabulary representing spatiotemporal data warehouse, that is still not available today.

1.1 Paper Contribution

Firstly, the paper presents the background of the importance of modeling and querying spatiotemporal multidimensional data on SW. Secondly, the paper presents the survey strategy and then describes the characteristics of DW/OLAP and SW, the convergence of DW and SW, and the approach of combining DW and SW. Then, the paper describes modeling and querying multidimensional data, both from the conventional OLAP DW to the Semantic Linked Cube Data, and makes a comparison of modeling and querying features of DW that have been implemented on the SW. The next section will be discussed the conceptual model of spatiotemporal DW, and findings from the modeling and querying spatiotemporal multidimensional data on the SW. Finally, all the discoveries are discussed and several guidelines for prospect research are defined.

2 SURVEY STRATEGY

Survey strategy is important in the survey to guarantee the breadth and depth of the studies. The survey strategy consists of three steps:

a) Identification of Research Questions (RQ)
b) Digital library selection
c) Search string identification

2.1 Identification of Research Questions

This survey objectives to review the novel concept and implementation of the spatiotemporal DW model and to query on SW comprehensively for further investigation. Three research questions were
identified to support this survey, as presented in table 1.

Table 1: Research Question

<table>
<thead>
<tr>
<th>RQ</th>
<th>RQ Statement</th>
<th>Motivation</th>
</tr>
</thead>
<tbody>
<tr>
<td>RQ1</td>
<td>What is the concept and technology behind the combination of the DW and SW? What are the approaches? What are the benefits and drawbacks of the approaches?</td>
<td>To find the concept and technology behind the combination of DW and SW and find the best approach to combine DW and SW.</td>
</tr>
<tr>
<td>RQ2</td>
<td>What are the existing multidimensional data semantic models and analytical queries have been proposed for multidimensional on the SW?</td>
<td>To find an existing multidimensional model and analytical query on SW that have been formulated and implemented.</td>
</tr>
<tr>
<td>RQ3</td>
<td>What are the existing semantic model and analytical query have been proposed for spatiotemporal multidimensional data on the SW?</td>
<td>To find existing spatiotemporal multidimensional model and analytical query on SW that have been formulated and implemented.</td>
</tr>
<tr>
<td>RQ4</td>
<td>What are the existing gap in the current research in the modeling and querying spatiotemporal multidimensional data on SW?</td>
<td>To find area of spatiotemporal multidimensional data on SW that have not have been modeled and queried.</td>
</tr>
</tbody>
</table>

2.2 Digital Library Collection

The selection process is started with entering ‘Data Warehouses’ and ‘Semantic Web’ between 2010 – 2019 as search strings on Google Scholar repository. This query results from 4.010 of papers and filtered from several popular databases research area to collect the primary papers originated from recognized databases. The popular databases are:

a) Springer
b) Science Direct
c) IEEE Xplore
d) Emerald Insight
e) Taylor & Francis
f) ACM Digital Library
g) Wiley Online Library

2.3 Search String Identification

The authors search papers from the digital library collection with search string ‘Data Warehouses’ and ‘Semantic Web’ between the year 2010 until 2019 with the language exclusion not in English. The results of the query are depicted in figure 1.

Figure 1. Search string query and the results

Table 2. Inclusion dan Exclusion Criteria

<table>
<thead>
<tr>
<th>Inclusion Criteria</th>
<th>Exclusion Criteria</th>
</tr>
</thead>
<tbody>
<tr>
<td>Using the English Language</td>
<td>Not Using the English Language</td>
</tr>
<tr>
<td>Paper related to Modeling and Querying Multidimensional data on SW</td>
<td>Identical papers</td>
</tr>
<tr>
<td>Paper is related to at least one research question</td>
<td>Paper does not relate to research questions</td>
</tr>
<tr>
<td>Paper is peer-reviewed in journals, conferences, or workshops</td>
<td>Paper is not peer-reviewed, presentations</td>
</tr>
</tbody>
</table>

The result of applying inclusion, exclusion, and snowball technique are 80 papers are fit to answer all the research question defined earlier.

3 BUSINESS INTELLIGENCE AND SEMANTIC WEB

BI architecture consists of a data source layer, integration layer, storage layer, and analysis layer. The data source layer is a layer where data is collected from an internal or external data source. The integration layer is a layer for the data integration process in the form of Extract, Transform, and Loading (ETL) which produces multidimensional data. Multidimensional data will be saved at the storage layer called Data Warehouse (DW) and is ready to be analyzed using OLAP that creates an analysis layer. The multidimensional data, which represented by DW, have fact and dimension tables. Conventional BI relies on a controlled internal environment for data sources. The data source must have a structure and will be applied by heavy extract mechanisms, transformation, and loading data based batch mode. BI requires high
quality and complete data, but the completeness might not be obtained only from internal databases, so that BI has to link to external data, such as competitor data, markets, potential buyers, government rules, and politics [9].

BI grows with the capability to adapt to external data sources that have an unstructured, semi-structured, and flexible format. BI grows its scope that extends to not only strategic decision support but also the tactical decision that makes new terms like BI 2.0 [10], on-demand BI, Self Service BI [11], and fusion cube [12].

Furthermore, the exploratory OLAP concept emerges as a BI that has the ability to explore and access new data sources with new data structures, to store new data, and to query these new data [13], [14]. One of the technologies behind the Exploratory OLAP is the Semantic Web. This technology becomes mature. SW allows data sharing in a dynamic way, publishing data and linking semi-structured data on the web using standards, besides SW also has the ability to support inferencing and active reasoning. In order to support the data sharing process, SW has accurate and rich data declarations through ontology and vocabulary. SW also supports efficient data acquisition with SPARQL. Data integration with SW is supported by the ability to provide data meaning that it is indispensable for the process of cleansing, merge, and combining data from a variety of sources to become multidimensional data. The process of analyzing data through queries is also equipped with the ability to give meaning to data not only for results but also where the data comes from.

Over several years, the direction of BI and SW research has been different, but in the last decade research in these two domains shows us the convergence and the mutually beneficial. BI proposed sophisticated tools for analyzing the huge amount of data with an outstanding performance, whereas SW linked data proposes an exploratory opportunity of valuable information that could be used for enriching business analytics with inferencing capability [12], [15]–[19]. The convergence of the BI and SW showed in figure 1.

Developing OLAP using SW categorized into three types of approaches, the first approach is an integration-based approach that focuses on data source integration, the second is an analysis-based approach that focuses on analytical processing and the third is a combination of these two approaches. A detailed discussion of the three approaches is as follows:

3.1 The integration-based approach

An integration-based approach is an approach that focuses on the process of extracting, transforming, and loading (ETL), from RDF data sources to DW. The integration-based approach has been proposed because RDF data does not have a data structure that allows OLAP operations to be imposed on it, such as: drill down, roll up, slice, dice, etc. The ETL results are stored in a multidimensional cube that can be easily accessed using MDX query language for analysis. This approach is also known as a schema-on-write approach where requires a multi-dimensional schema to be designed and the ETL process to be set as a write process before the query is executed. The illustration of this concept is shown in figure 2. The ETL process input is coming from the data source that may have a different format, semantic or non-semantic data. ETL process will build DW and Cube that OLAP operations could be used to support analysis.

Many researchers have been successfully carried out with this approach. Firstly, the research of the creation of the multidimensional concept of
DW warehouses originating from single domain ontology representing multiple heterogeneous data sources from many business domains [20]. Furthermore, research by Niinimaki et al. developed a technique to practice ontology and mapping files that connect to the data sources from external sources with the ontology. Then, the ETL process is performed according to the ontology and mapping files. OLAP ontology defines measures and dimensions using Ontology Web Language (OWL) and Resource Description Framework (RDF). This research-validated by performance testing using 450,000 RDF statements and give outstanding performance [21]. Likewise, Nebot et al. suggest a solution to solve the problem of combining DW and SW technologies. They proposed a framework for designing a model of MD analysis with the semantic annotation stored in a Semantic DW (SDW) that stores web resources, domain ontologies and the semantic annotations using XML. Their finding claims has a new semi-automatic approach to defining multiple domain ontology, scalable, and well formalized [22]. Additionally, Jiang et al. proposed a method to handle data heterogeneity to build DW with the domain ontology in the integration process. Domain ontology has created using classes of Web Ontology Language and inserted in the metadata of the DW that could describe the logic of transforming data, discover the data sources, and remove the heterogeneity. The method has been implemented in a hospital DW, and medical domain ontology plays an important role [23]. Likewise, Bergamaschi et al. developed an ETL tool that could support semantic mappings from the data source with inter-attribute definition to support the extraction and transformation process to the DW schema. The tool has been implemented for developing DW in the case of the food and beverage logistics area and resulting effective method [24].

Moreover, Kampgen et al. proposed a concept of integrating multiple Linked Data sources of statistical data. Their research created a design to convert from Linked Data into the Cube model in DW, then execute the design using an ETL pipeline process, and thus load the conversion results into an open-source OLAP system. This research also shows how the infrastructure of OLAP could be used for querying and visualizing integrated statistical Linked Data [15]. Inoue et al. developed a general ETL framework for Linked Open Data (LOD) dataset. Their framework can execute the ETL process to the datasets regardless of the usage of the OLAP Cube vocabulary and could explore semantic hierarchies in the dataset even from external LOD such as geonames and DBpedia [25]. Further, An ETL-based approach is developed in the H-SPOOL framework that does extract OLAP-related information from SPARQL endpoints that have the advantage of reducing the number of downloaded triples [26].

The integration-based approach has the advantage of the usage of mature and proven OLAP technology, on the contrary, this method still has disadvantages that the refreshment process of LOD data to DW still performed in semi-automatically way, making it difficult to maintain consistency between data warehouse and online data for analysis purposes.

3.2 The analysis-based approach

This approach focuses on analytical processes that carried out directly on Semantic Web/RDF data without the ETL process. In this approach,
multidimensional data requires vocabulary to model data cubes, dimensions, and measures in RDF. This approach sometimes called a schema-on-read approach. The de facto standard of vocabulary for RDF Data Cube is QB. Many proposals have been successfully explored this approach. Firstly, Kampgen et al. define a proposal to model querying statistical Linked Data using common OLAP operations on RDF data cubes. This research also found a set of OLAP query functions and operators using SPARQL language. Both models and queries are executed directly on a triple repository without intermediate storage; therefore, if the RDF is changed, modifications are disseminated to OLAP clients. This research also improved the QB vocabulary for enhancing multidimensional statistical data representations [27].

Moreover, Etcheverry and Vaisman developed Open Cube (OC) vocabulary that using RDFS for publishing multidimensional cubes on the SW. Using Open Cube, traditional OLAP operations possibly executed using SPARQL 1.1., and web cube could be mapped to the multidimensional model in order to be able to operate with the local cubes. OC also developed to support model with dimensions with multiple hierarchies, but OC has a disadvantage that could not reuse QB vocabulary that has been used before [28].

Saad et al. create an efficient RDF constellation model by proposing a formalization of multidimensional structure. This model supports multiple facts, multiple dimensions, and multiple hierarchies. Based on this formalization, operators of OLAP can be interpreted into SPARQL queries that comply with the constellation model [29]. Furthermore, Ibragimov et al. developed a framework called Exploratory OLAP over RDF sources. This research proposes a system using RDF vocabularies to define OLAP cube with a multidimensional schema. The system is intelligently executing the query to extract and summarize data, and also build a cube based on the vocabularies. This project also creates a process for determining unidentified data sources and constructing a multidimensional schema of the cube. In this approach, vocabulary for multidimensional or statistical data is an important issue because OLAP in the semantic web requires complex models for the fact, dimension, level, hierarchy, etc. [18].

Moreover, the research conducted by Etcheverry develop an extension of QB that models multidimensional data with the new vocabulary; it is called QB4OLAP. QB4OLAP supports balanced hierarchy, recursive, ragged, and many-to-many relationships that most used on the multidimensional model.

Varga et al. also developed QB2OLAPem, as a tool to transform the QB dataset into QB4OLAP dataset using enrichment semantic and using the high-level QL OLAP languages that automatically generate SPARQL statement [31]. Furthermore, Kalampokis et al. develop a new method to speed up query execution using a materialized view of the RDF graph. Their approach physically stores summarized triple in the system for faster processing.
SPARQL queries (MARVEL). Many application tools have been built using this approach and used by government and industries, e.g. http://opengovintelligence.eu, which continues to develop, expanding, and exploiting Statistical Linked Open Data, with the TARQL extension, and D2DQ, called the Linked Open Cube Analytics (LOCA) system [32]. On the other hand, Boumhidi et al. proposed a method for directly querying the cube data stored modeled by QB vocabulary with an interactive OLAP via MDX to SPARQL mapping without any materialization. This research also constructed a formal algebra of OLAP operations on data cubes published as Linked Data [33].

This analysis-based approach described earlier, actually overcomes the problems of the previous integration-based approach on the issue of ETL and data refreshment. The analysis-based approach provides multidimensional OLAP modeling that is suitable for Linked Data but the impressive materialization and pre-aggregation aspects of the cube on linked data still left a problem to be solved.

3.3 The combination approach

This approach is fully integrated SW in all layers of BI. It had been known, one of the drawbacks of the implementation of the integration-based approach is that the ETL process for the linked data source traditionally prioritizing data schema. This method is considered ineffective because Linked Data has a schema-dependent nature, or sometimes has a complex schema, or even only have an implicit schema. Data on SW may have a condition where different sources can explain the same data in different ways. The integration of data for heterogeneous data using semantic data is a necessity that cannot be avoided. This combination approach improves the weaknesses of traditional ETL that fully integrate the Semantic Web with the Data Warehouse, in this way the BI community benefits from the analysis process with semantically annotated data. Several researchers proposed this combination approach, among them, are Colazzo et al. proposed a bottom-up redesign of the core data analytics concepts and tools, on RDF data. This design is fitted with Linked Data with rich semantic and heterogeneous format. This design using a full RDF warehousing approach, where the data source and the DW are in RDF graph format. This research also defines analytical schema and queries and optimization techniques with schema materialization [34].

![Figure 5. The combination between integration-based and analysis-based Architecture OLAP on Semantic Web](image)

Moreover, Bansal and Kagemann researched to create ETL tools that are able to integrate data from various heterogeneous sources by utilizing semantic data to enrich the integration process [35]. Furthermore, Nath et al. proposed a programmable framework called Semantic ET (SETL) that could support the development of Semantic Data Warehouse. SETL using TBox and QB4OLAP schema to create Multidimensional data for Semantic and Non-Semantic Data Source [36]. Table 3 shows the summary of the OLAP development using the SW. The comparison, benefits, and drawbacks of the three approaches have described in this table.

<table>
<thead>
<tr>
<th>Integration-based</th>
<th>Analysis-based</th>
<th>Combination approach</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conventional Data Source</td>
<td>Semantic ETL</td>
<td>RDF Cube/Triple Store</td>
</tr>
<tr>
<td>RDF Data Source</td>
<td>Extract Transform Loading Process</td>
<td>SPARQL Query</td>
</tr>
<tr>
<td>RDF Cube/Triple Store</td>
<td>RDF</td>
<td>Users</td>
</tr>
</tbody>
</table>

Table 3. Summary of OLAP development using Semantic Web
4 MULTIDIMENSIONAL DATA MODEL

The multidimensional data model or a data cube was introduced as an infrastructure of OLAP and DW. The concept of OLAP popularized by Codd [39] as a method of executing complex analysis over information stored in a DW. A DW is a considerable data repository with subject-oriented, integrated, time-variant, and non-volatile data organized specifically for analytical purposes [40]. A DW is designed in the form of a star schema or snowflake that has a fact table and dimension table. A DW is designed to be performed well by drill-down, roll-up, slice, and dice operations. The fact table contained cells associated with numerical values called measures. The analysis process assesses many aspects of the business using these measures. For example, the cube of data in figure 6 shows a cell

![Figure 6. Data Cube for Agriculture Production](image)
that represents a measure of Quantity, indicating the numbers of agriculture production (in thousands ton) by-product(category), time(quarter), and farmer(province). A data cube usually has several measures. For example, another measure on the agricultural cube, not shown in the figure, could be the total sales amount from agriculture production. The dimension table is a representation of a dimensional perspective of analysis. Dimension has levels and descriptors. For example, the data cube in figure 6 can be used to analyze production figures. The cube has three dimensions: Product, Time, and Farmer. A dimension level represents the detail level of the data and often called granularity. A level has attributes that describe the dimension. For example, the production cube is summarized to the levels Category, Quarter, and Province. Dimensions also have attributes to describe the characteristic of the dimensions. For example, the Product dimension could have attributes such as ProductId and PricePerKg.

In the concept of DW, the term hierarchy on the dimension is known, which enables decision-makers to get more detailed information for strategic analysis purposes. For example, in the data cube shown in fig 6, information on the quantity of production could be enhanced to the finer granularity in the month order, or the coarser granularity on the farmer dimension at the country level. The hierarchy will define the sequence of mapping that connects concepts from higher or more general concepts to lower or more detailed concepts. The hierarchy has many types, including balanced, unbalanced, multiple, recursive, generalized, alternative, and parallel hierarchies.

The hierarchy concept of the data cube related to the aggregation process of each measure in a data cube. The aggregation process performed by traversing to this hierarchy of the dimension. The aggregation process usually takes place when the user wants to visualize the aggregation of measure interactively by changing the level of detail of the dimension. For example, if we want to visualize data cube in figure 5 by Country, then we must to change granularity to the coarser detail from Province to Country, then the Production figures for all farmers in the same country will be aggregated using, for example, the SUM operation. The measure can be categorized as follows:

a. **The additive measure** is a measure that could be aggregated using addition for all the dimensions, using addition. The additive measure is a common type of measure.

b. **The semi-additive measure** is a measure that could be meaningfully aggregated for some dimensions using addition. For example, a measure product inventory that summarized for two months didn’t give meaningful aggregation.

c. **The non-additive measure** is a measure that could not be meaningfully aggregated along any dimension. For example product price, and currency rate.

d. **The derived measure** is a measure derived from another measure.

### 4.1 OLAP Operations

The multidimensional model gives the environment that could interactively analyze data for descriptive information from multiple dimensions and at several levels of detail. The model using OLAP operators that could aggregate and materialize data along dimensions and hierarchies. The OLAP operators are:

(a) **Aggregate Function**: a function that aggregate measure of a cube, including SUM, AVG, COUNT, MIN, MAX, TOPPERCENT, BOTTOMPERCENT, RANK, and DENSERANK. The syntax for the aggregate function is:

\[
\text{AggFunction}(\text{Cube}, \text{Measure})[\text{BY} \text{Dimension}]
\]

For example, from figure 5, total production by month and province could be expressed by

\[
\text{SUM}(\text{Production}, \text{Quantity}) \text{ by } \text{TIME.MONTH, FARMER.PROVINCE}
\]

(b) **ROLLUP**: query to aggregates measures alongside the hierarchy of dimensions using an aggregate function. This query acquires measures at a rougher granularity. The syntax of measures ROLLUP operation is:

\[
\text{ROLLUP}(\text{Cube}, (\text{Dimension} \rightarrow \text{Level}), \text{AggFunction}(\text{Measure}))
\]

for example, total quantity by the month of production cube is:

\[
\text{ROLLUP}(\text{Production}, (\text{Time} \rightarrow \text{Month}), \text{SUM}(\text{Quantity}))
\]

Sometimes in real-world applications, the hierarchy contains a level that rolls up to the
hierarchy itself; it is called the recursive hierarchy. ROLLUP operations will be varied with recursive ROLLUP or RECROLLUP, the syntax of recursive roll up is:

\[
\text{RECROLLUP} (\text{Cube}, (\text{Dimension} \rightarrow \text{Level}), \text{Hierarchy}, \text{AggFunction} (\text{Measure}))
\]

(c) SLICE: cut a cube for a certain dimension and value. The syntax of slice operation is:

\[
\text{SLICE} (\text{CubeName}, \text{Dimension}, \text{Level} = \text{Value})
\]

for example, the total quantity of production in Banten province is:

\[
\text{SLICE} (\text{Production}, \text{Farmer}, \text{Province} = \text{\textquote{T'Banten'}})
\]

(d) DICE: get data from cube to obtain information like dice in the cube, similar to the relational algebra of selection \( \sigma_p (R) \), where \( p \) is the boolean predicate conditions over-dimension levels, attributes, and measures. The syntax of dice operation is:

\[
\text{DICE} (\text{CubeName}, \ p)
\]

for example, total quantity by the month of production cube is:

\[
\text{DICE} (\text{Production}, \ \text{Farmer.Province} = \text{\textquote{T'Banten'}} \ \text{OR} \ \text{Farmer.Province} = \text{\textquote{T'East Java'}}) \ \text{AND} \ \text{Time.Month} = \text{\textquote{T'JAN'}} \ \text{OR} \ \text{Time.Month} = \text{\textquote{T'FEB'}}
\]

(e) DRILLDOWN: query to get more detailed data from a deeper level in a hierarchy. The syntax of the drill-down operation is:

\[
\text{DRILLDOWN} (\text{CubeName}, (\text{Dimension} \rightarrow \text{Level}))
\]

for example, the total quantity by the quarter of the production cube is:

\[
\text{DRILLDOWN} (\text{Production}, \ (\text{Time} \rightarrow \text{Month}))
\]

(f) PIVOT: query to provide an alternative presentation of data. The syntax of the pivot operation is:

\[
\text{PIVOT} (\text{CubeName}, (\text{Dimension} \rightarrow \text{Axis}))
\]

for example, the total quantity by a quarter of the production cube is:

\[
\text{PIVOT} (\text{Production}, \text{Time} \rightarrow \text{Quarter}, \text{Farmer} \rightarrow \text{Province}, \text{Product} \rightarrow \text{Category})
\]

(g) DRILLACROSS: query to get data from the combination of two common schema data cubes. DRILLACROSS query naturally has the same operation with a full outer join in the relational algebra. The syntax of DrillAcross operation is:

\[
\text{DRILLACROSS} (\text{CubeName1}, \text{CubeName2}, \text{Condition})
\]

for example:

\[
\text{DRILLACROSS} (\text{Production}, \text{Product1}, \ \text{Production.Time.Month+1} = \text{Production.Time.Month})
\]

4.2 Linked Cube Data Model and Query

For publishing linked data cube/statistical data, the model of the cube data is a core foundation. The linked cube model is represented by vocabulary. Many vocabularies have been developed to model multidimensional data with facts, dimensions, and hierarchies as RDF graphs and to query RDF graphs with OLAP operators. The first standard model of statistical data proposed by the International Organization for Standardization (ISO) in 2005, it is called the Statistical Data and Metadata Exchange (SDMX). The SDMX initialized by seven international institutions (UN, World Bank, IMF, Eurostat, BIS, and European Central Bank) with the purpose of improving efficiency and enhance quality using advance technology for share and exchange statistical data and metadata among institutions for interoperability. The SDMX covers how to represent statistical data in flat files and as XML to the definition of fact, dimension, and measure. SDMX created under Content-Oriented Guidelines (COGs) that define a set of code lists, cross-domain concepts, and categories with the aim of delivering interoperability and compatibility across organizations. Many researchers have implemented the SDMX to publish statistic data and access the data using web services, and the advent of linked data makes SDMX could be modeled with the linked data that provide some benefits [41]. The design and implementation of SDMX-ML to RDF/XML using XSL transformations have implemented to publish linked data from Organization for Economic Cooperation and Development (OECD), Swiss Federal Statistical Office (BFS), Food and Agriculture Organizations of United Nations (FAO), European Central Bank (ECB), and International Monetary Fund (IMF) [42].

Moreover, SCOVO (Statistical Core Vocabulary) is a first vocabulary that has been defined for statistical RDF data. SCOVO proposes a
framework for modeling and sharing statistical data. But SCOVO has the disadvantage of did not have a feature of organizing the data into slice dataset, or notion of dimensions, measures, and attributes that different in structure [43].

Furthermore, statistical vocabulary standards have been proposed, the vocabulary is called the Simple Knowledge Organization System (SKOS) vocabulary. The SKOS models common features in a standard thesaurus using classes and properties. The vocabulary of the SKOS using a concept-centric view that explains abstract notions represented by terms, but primitive objects are not terms. Each SKOS concept is defined as an RDF resource that can have properties like index terms, synonym, definition, and notes. Concepts could be arranged in hierarchies using broader-narrower relationships, or connected by non-hierarchical relationship. Concepts grouped in concept schemes, containing a consistent and structured set of concept that create controlled vocabulary [44]. However, The SKOS vocabulary that relied on loosely defined notions of ‘broader than’, ‘narrower than’, and ‘related to’ relationships not rich enough to handle more complex hierarchical relations, e.g., generic-specific, whole-part, causal, sequential, and temporal relations. There is a need to extend the SKOS to handle these relations, and also statistical researcher requirements as well as requirements from ISO 704:2000 and ISO 1087-1:2000 standard.

The new vocabulary is called XKOS. Cotton et al. has been described XKOS in the journal paper including the concepts, structures, terms and codes, and associative relations. XKOS categorized data between the concepts and the real-world objects and make a relationship between them. XKOS is built to provide a reusable standard on the RDF for publishing statistical data available through new web technologies [45].

The new milestone in modeling linked cube data has emerged with the RDF Data Cube, QB vocabulary. QB adheres to linked data principles and the RDF model. It becomes a W3C standard for modeling data cubes. QB is based on the core components of the SDMX information model. QB could define the structure of the cube, cube, instance of the cube, measure, dimension, etc. The main class in the QB is qb:DataSet that provides a definition of a cube. The qb:DataStructureDefinition describes the cube’s data structure. The qb:Observation class defines each cell of the cube as a measure. The vocabulary structure of QB is specified by the abstract class qb:Component-Property, that has three sub-classes, namely qb:DimensionProperty that describes the dimensions of the cube, qb:MeasureProperty that defines measured variables, and qb:AttributeProperty that defines the structural metadata [46]. At this moment, 11.24% of the datasets as Linked Data Cubes use the QB vocabulary [47]. The advent of QB vocabulary makes linked data cube popular among organizations. Many organizations created link data cubes, for example, European Commission developed Digital Agenda Scoreboard as a visualization tool that built from linked data cubes, Eurostat transformed their research data to linked data cubes that includes more than 5000 data, and the publication of the linked data cubes of 2011 census data from Ireland, Greece and Netherland [48].

Moreover, a new linked cube model is developed by Etcheverry et al., their research develops Open Cube (OC) vocabulary. This OC model supports the representation of facts, dimensions, and multiple hierarchies dimension using RDFS. The OC also develops an algorithm that applies basic cube operators such as slice, dice, roll-up, and drill-down. This vocabulary is the first approach in the field of BI over the Semantic Web, but OC has a disadvantage that could not reuse QB vocabulary that has been used before [28]. Furthermore, Etcheverry et al. proposed QB4OLAP linked cube model. The QB4OLAP is a vocabulary that extends the QB model to supports the characteristics of the cube model, including balanced hierarchy, recursive, many-to-many, and ragged relationships. This model offers a translation from the conceptual multidimensional model into an RDF model using the QB4OLAP vocabulary and maps relational implementation of a DW via R2RML into QB4OLAP cubes that could be queried using SPARQL for basic cube operations directly over the RDF representation like OC. This research also provides algorithms that build the QB4OLAP structures needed to analyze observations already published using QB, and vice versa, with only provide dimensional information modification that efficient in size compared with observations OLAP fact data [17].
Furthermore, the researchers try to enhance the feasibility of a linked cube model with optimization. Colazzo et al. proposed analytical schema and queries using full RDF warehousing with schema materialization [34]. Azirani et al. proposed systematic optimization for efficient OLAP operations. His technique tries to solve the question of computing an Analytical Query based on the materialized answer of another Analytical Query [49].

The QB is becoming a W3C standard to represent data cube on the SW, but the QB still lacks some critical features needed for OLAP analysis. The QB4OLAP tries to overcome this limitation with a new algorithm for OLAP analysis using SPARQL, but writing a query with a simple and efficient analysis, not a simple task. User needs an in-depth knowledge of standards like RDF SPARQL that not easy for analytical users. Etcheverry et al. develop a simple, high-level query language that operates over data cubes called Cube Query Language (CQL). CQL queries will be translated into SPARQL queries efficiently, with optimization techniques and best practices. CQL provides functionalities to general query data cube for a roll-up, drill-down, slice, and dice [37].

The summary of the completeness of linked cube data model is shown in table 3, but all the approach still does not support to model many to many relationships between facts and dimensions, multiple hierarchies, alternative hierarchy, and parallel hierarchy. All the approach also does not have the opportunity to query data with drill-across, drill-through, and pivot functions.
Table 3. The summary of the completeness of the linked cube data model and query

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5 SPATIOTEMPORAL DATABASE

Spatiotemporal database is a database that stores information from spatiotemporal objects and manages the data for query retrieval. Every object has space and time attributes, these objects are called spatiotemporal objects. Along with GPS technology and location-based technology, the number of spatiotemporal objects and spatiotemporal data has increased in quantity. Spatiotemporal objects have spatial and temporal attributes and their combinations. **Spatial attributes** describe real-world phenomena consisting of descriptive components, which are presented with traditional data types such as integers, strings, and dates, and spatial extent components, which explain the real world in the form of geometric data types such as **Point, Points, Line, Polygon, and Surface** (MADS Model). Spatial attributes are stored differently and are often called thematic layers (themes). Spatial attribute represented by spatial data types that have operators associated with, as shown in table 4.
Table 4. Operator in spatial data types

<table>
<thead>
<tr>
<th>Class</th>
<th>Operators</th>
</tr>
</thead>
<tbody>
<tr>
<td>Topological Operations</td>
<td>Intersects, Disjoint, Equal, Overlaps, Contains, Within, Touches, Covers, CoveredBy, Crosses</td>
</tr>
<tr>
<td>Predicates (Boolean)</td>
<td>isEmpty, OnBorder, InInterior</td>
</tr>
<tr>
<td>Unary Operations</td>
<td>Boundary, Buffer, Centroid, ConvexHull</td>
</tr>
<tr>
<td>Binary Operations</td>
<td>Intersection, Union, Difference, SymDifference</td>
</tr>
<tr>
<td>Numeric</td>
<td>NoComponents, Length, Area, Perimeter, Distance, HaversineDistance, Direction, NoOfInterior</td>
</tr>
<tr>
<td>Spatial Aggregation</td>
<td>Intersection, Union, ConvexHull, MinimumBoundingRectangle, Center of n Point, Center of Gravity, Equipartition, Nearest-neighbor index</td>
</tr>
<tr>
<td>Azimuthal Relationship and Direction</td>
<td>North, South, East, West, Direction</td>
</tr>
</tbody>
</table>

Table 5. Operator in temporal types

<table>
<thead>
<tr>
<th>Class</th>
<th>Operators</th>
</tr>
</thead>
<tbody>
<tr>
<td>Projection to domain/range</td>
<td>DefTime, RangeValues, Trajectory</td>
</tr>
<tr>
<td>Predicates (Boolean)</td>
<td>IsDefinedAt, isContinuousIn</td>
</tr>
<tr>
<td>Interaction with domain/range</td>
<td>GetValue, HasValue, AtInstant, AtPeriod, InitialInstant, InitialValue, FinalInstant, FinalValue, At, AtMin, AtMax, startSequence, endSequence, etc</td>
</tr>
<tr>
<td>Unary Operations (Spatial)</td>
<td>Length, Transform, CumulativeLength, NearestApproachDistance</td>
</tr>
<tr>
<td>Binary Operations</td>
<td>Before, Equals, Meets, Overlaps, During, Start, Finish</td>
</tr>
<tr>
<td>Rate of Change</td>
<td>Derivative, Speed, Turn</td>
</tr>
<tr>
<td>Temporal Aggregation</td>
<td>Integral, Duration, Length, TAvg, TVariance, TStDev, TMin, TMax</td>
</tr>
<tr>
<td>Lifting</td>
<td>All new operations inferred</td>
</tr>
</tbody>
</table>

Temporal attributes describe time, changing in time that the value could be represented by temporal types. For instance, temporal integers could be used to describe the evolution of employee salary, temporal geometries represent the area of an agricultural field that decreases every year, temporal points denote the flight path data from an aircraft and tourist movement from one place to another as reported as GPS device. The temporal type has subtype like boolean, integer, float, text, and geographic. Depending on the subtype, temporal types could be discrete or continuous. Discrete temporal types evolve in a stepwise manner like boolean, integer, and text, but continuous temporal types evolved in a continuous manner like float and geometric. The example of the temporal float is the temperature of the human body, on the other hand, the example of temporal geometric (point) is the location of a truck read by GPS device.

Temporal types are based on four-time types: timestamp with time zone, period, timestamp set, and period set. A value of period type has two bounds, lower and upper with timestamp type. Temporal types recognize duration that states the temporal extent at which the evolution of values is recorded. The temporal type also distinguishes valid time and transaction time. Valid time is the time when the value of a tuple is valid in the database, while the transaction time is the time at which tuples are recorded in the database. For example, if the salary of an employee is recorded in the database on January 28, 2014, this will be stored as its transaction time, but if it holds for the employee from February 28, 2014, the later date will be recorded as the valid time for this attribute. Figure 3 illustrates an example of simple temporal attributes that represent salary changes. John’s salary is 20 that valid from January 1, 2012, until July 1, 2012, and 30 that valid from October 1, 2012, until January 1, 2013. On the other hand, Mary’s salary is 60 that valid from April 1, 2012, until April 1, 2013.

Figure 8. Examples of salary change [1]

Temporal types have an associated set of operators, as shown in table 5.

5.1 Temporal Spatial Types

The combination of spatial and temporal types create new data types called temporal-spatial types.
This combination occurs in moving objects, such as moving pedestrians, moving trucks, moving clouds, shrinking agricultural areas. All operations for temporal types are also valid for spatial types. The following figure 9 is an example of moving trucks in a palm oil simulation plant.

![Figure 9. Examples of temporal-spatial types: moving trucks](image)

The more details of the examples of moving objects are depicted in the following figure 10. Figure 10 displays the example of a moving pedestrian that can be manipulated using the temporal operator in table 4. Someone (f) walks from location A (0,2) at 8:00 to location B (8,9) and arrives at 08:10 proceed (g) to location E (12,9) and arrives at 08:15, and someone (h) walks from location D (1,1) at 8:00 to location E (12,5). The distance of the moving pedestrian is varying in time that depicted in figure 11.

![Figure 10. Examples of moving pedestrians](image)

The temporal-spatial types could be extended to represent field/region that varies both in time and space. The examples of this representation are the area that is shrinking every year at a certain speed. The ill of the phenomena is depicted in figure 11. The grey area is a missing area that becomes bigger every year.

![Figure 11. The distance of the moving pedestrians](image)

The spatiotemporal database is then used to store spatial types, temporal types, and temporal-spatial types. This database could store the position of moving objects at any point in time, regions with the reduced area continuously, and so on. Although some examples of queries could be solved like “When did an airplane from Jakarta coded KL870 arrive at Kuala Lumpur International Airport?”, “How fast is the reduction of rainforests in Kalimantan in the last 5 years?”, but this kind of databases do not provide a foundation for complex analytical queries such as “How many total numbers of transports started in Kuala Lumpur in January, February, and March 2012?” or “How long average duration of transportations by region.” These kind of queries could be handled efficiently using DW, and the DW could be extended in order to support the concept of spatiotemporal data warehouses that contain spatial types, temporal types, and temporal-spatial types data.
6 SPATIOTEMPORAL DATA WAREHOUSE

Spatiotemporal DW is an infrastructure of OLAP that performs on spatial and temporal data. Spatiotemporal DW, which attracts researchers in the early 2000s, is a combination of GIS and OLAP that support spatial data types, temporal data types, temporal-spatial data types (moving object types) and evolving data warehouse dimensions. Exploration for a spatial data warehouse for the first time has been conducted by the design of spatial dimension hierarchy in the form of geometric and non-geometric attributes [50]. Rivest et al. began to study spatiotemporal DW by combining GIS and time with OLAP, with defining operators such as drill-down and roll-up on maps. This study succeeded in identifying features and operators imposed on spatiotemporal databases [51].

Furthermore, Da Silva et al. designed and built the GeoDWFrame framework, a framework of processing Geographical Data Warehouse and the GeoMDQL language used in the Spatial Cube based on geographical or hybrid dimension, MDX, and Open Geospatial Consortium (OGC) features [52]. Malinowsky et al. discovered the MultiDim conceptual model, which could model several spatial and temporal features, like spatial dimension, and spatial level using topological relationship. In the MultiDim model, the spatial measure could be represented by geometry, which is an aggregation of dimensions, or aggregation of numerical value representing in shape which is calculated based on topology operators and metric operators. Almost all proposals for geometry aggregation are represented in sets of coordinates or sets of pointers to objects [53]. The spatial extension of the MultiDim model based on the spatial data types of MADS also found in [54]. A great discovery of the integration of GIS and OLAP arises when Gomez et al. found geometric data aggregation, and measure associated with component aggregation. In this research, a combination of GIS and OLAP is maintained through a language, GIS-OLAP-QL. They also developed a framework called Piet, which provides four features of queries, including the standard query of GIS, OLAP, geometric aggregation, and integrated GIS-OLAP queries. The examples of geometric aggregation are like “how many total population in the district through which more than three river pass”, and the examples of integrated GIS-OLAP query is like “how many average crop production by-product by district around the slopes of the mountain”. Furthermore, Piet outfits a new query processing using decomposition technique to split the thematic layer in a GIS, into open convex polygons; then, implement the overlay precomputation as a materialization technique [55].

Moreover, modeling and querying spatiotemporal data has been demonstrated by the framework SECONDO. SECONDO was developed as a DBMS platform that can implement several data models, such as Spatio-temporal data, and graph models, and run a query on these data models [56], [57]. SECONDO has been extended to Distributed SECONDO as a scalable and fault-tolerant DBMS using Apache Cassandra as data storage [58]. Additionally, HERMES, a robust framework capable of modeling, constructing and querying spatiotemporal databases that are implemented in the Relational DBMS Object [59]. Spatiotemporal databases are then developed into spatiotemporal DW, which put forward the concept of a trajectory DW that provides an infrastructure for aggregating mobile data objects and mining data. This study also puts forward an efficient ETL process from track observation data to DW [60]. Braz et al. introduce the term of Trajectory DW by extending the conventional DW to store trajectory aggregation of the moving objects, and implement the OLAP operations over the trajectory DW. Trajectory DW is able to analyze interesting measures of mobility objects such as the number, speed, and acceleration of moving objects in a particular region and other measures [61]. The Trajectory DW makes trajectory data become valuable knowledge, which provides a basic foundation for a wide range of applications such as traffic management and control, analysis of social behavior, and recommender system [62]. Trajectory DW has been successfully implemented in PostGIS, an extended version of PostgreSQL with OGC based model [63]. Trajectory DW also could be used to organize and analyze trajectory data using OLAP and data mining techniques [64].

Wagner et al. proposed Trajectory DW with semantics annotated enrichment. The mobility of Spatio-temporal objects embedded with several semantic dimensions such as transportation means, mobility patterns, motion segment, categories and hierarchies [65], [66]. Vaisman et al. developed the Mobility Data Warehouse for mobility analysis. The DW store moving objects data that generally come
in the form of long sequences of spatiotemporal coordinates \((x, y, t)\), and store the positions of moving objects at any point in time. This DW contains mobility object data that can be analyzed in combination with other kinds of data (e.g., spatial data), for instance, a road network, altitude data, and the kind [67].

On the other hand, in the absence of a commonly agreed definition of what is a Spatiotemporal DW and what functionality it should support. Vaisman and Zimanyi present a conceptual framework for defining spatiotemporal DW using an extensible datatype system. This conceptual framework defines a taxonomy of models that integrate OLAP, spatial data, and moving data types. From the classes in this taxonomy, they also represent queries from tuple relational calculus, extended aggregate functions to spatiotemporal calculus supporting moving data types [68]. Spatiotemporal DW taxonomy is categorized into four classes, namely: Temporal dimensions, OLAP, GIS, and moving data types. The combination of these classes is shown in the following picture:

![Figure 13. Taxonomy of Spatiotemporal OLAP](image)

Combining GIS with Moving Data Types produces Spatiotemporal data, OLAP, and GIS resulting in SOLAP, OLAP and Spatiotemporal Data resulting in Spatiotemporal OLAP, Temporal Dimension and Spatiotemporal OLAP resulting in Spatiotemporal TOLAP. Temporal Dimensions and OLAP produce TOLAP, while TOLAP combined with GIS becomes Spatial TOLAP. The taxonomy also produces different queries for each class. Examples of queries from each taxonomy are as follows:

1. **OLAP**: For each field in a particular village and certain districts show the total production of three types of plants: rice, corn, and soybeans, every year.

2. **Spatial OLAP**: Show the total production of three types of plants: rice, corn and soybeans, each year at a distance of 10 km from the peak of Mount X in Central Java Indonesia.

3. **Temporal OLAP**: For each village and type of plant, show average production in the first quarter of 2018, for each location of water pollution monitoring, give information on how many days in a year where pollution levels exceed the threshold.

4. **Spatiotemporal OLAP (ST-OLAP)**: For certain types of plants at a radius of 10 km from the summit of Mount X how much is the total loss of harvest failure due to eruption in February 2019.

5. **Spatio-Temporal OLAP (S-TOLAP)**: For each village above the Y river determine how long (in days) successive hot clouds hit

6. **Spatiotemporal-Temporal OLAP (ST-TOLAP)**: What is the total number of days in which Z Regency is under at least one CO-charged cloud so that the average load of the cloud is greater than the load limit when the cloud appears

### 6.1 Conceptual Model Spatiotemporal Data Warehouse

DW has characteristics of subject-oriented, integrated, time-variant, and non-volatile [40]. DW is designed in the form of a star schema or snowflake that has a fact table and dimension table and has query operators like drill down, roll up, slice and dice. In the context of spatiotemporal, DW has spatial and/or temporal levels, spatial and/or temporal attributes, spatial and/or temporal hierarchy, spatial and/or temporal dimension, and spatial and/or temporal fact. The spatial level is the level where the spatial characteristics are to be stored. These characteristics are based on geometry, that is, one attribute must have a spatial data type. Spatial attributes are attributes that have a spatial data type domain (point, line, polygon, and continuous field). Spatial hierarchy is a hierarchy that has one spatial level. The spatial dimension is a dimension that has at least one spatial hierarchy. Two spatial levels in one spatial hierarchy can have topological constraints. Spatial fact is a fact that relates to several levels, two or more of these levels are spatial. The spatial fact can have topological constraints with related levels. The fact has a measure that represents data that has a meaning related to the related dimension. The measure can be...
either numerical data or spatial data (geometry). The data measure type determines what operations can be imposed on it, by default sum is an operation for numerical measure and spatial union to measure geometry. Some types of spatial aggregation for a spatial type are distributive spatial (spatial union, spatial intersection, convex hull), spatial algebraic (center of n point, the center of gravity), spatial holistic (equipartition, nearest-neighbor index).

The examples of the DW that support spatiotemporal analysis is depicted in figure 14. The idea is developing spatiotemporal DW that keeps track of deliveries of fruit bunch in the plantation and analysis of fruit load/unloading from fruit collection points. In the company, there is an armada of trucks that load some fruits from several fruit collection points and transporting them into the loading ramp of the plant and unloading them for processing. The driver of the trucks performs a delivery according to an order from the plant. There are spatial data about the road network, the geographic hierarchy from the plantation (afdeling, block, and fruit collection point/FCP), and the trajectory traced by the trucks. Additionally, there are non-spatial data about drivers and the trucks. Figure 6 depicts the conceptual schema showing the scenario using MultiDim model extended to support spatial, temporal, and temporal-spatial types.

As shown in the figure, the fact Delivery is a spatial fact that related to five dimensions: Truck, Time, Plant, TruckDriver, and FruitCollectionPoint (FCP), where the latter is a spatial dimension related to the fact through a many-to-many relationship. The truck dimension is composed of two levels, with one-to-many relationships. Spatial attributes or levels have an associated geometry (e.g., point, line, and region), which is indicated by $\bullet$, $\rightarrow$, and $\varnothing$. In this example, dimensions Plant and FCP are spatial and share geography hierarchy where geometry is associated with each level in both dimensions. The FCP Dimension has a topological constraint that indicates an FCP is contained in Plantation Block and Plantation Block is contained in Plantation Afdeling and creates a parent-child relationship.

The spatial fact table Delivery has seven measures. The first measure is Route that captures the truck position at any point in time. This measure is a spatiotemporal measure of temporal point type, as shown by the symbol $t(\bullet)$. The other measures are derived from Route, measure Trajectory captures the geometry of the route traversed by the truck, which is represented by a line, without temporal information, measure Distance, Load, and Duration are numeric, while StartTime and EndTime are timestamps. Trajectory measure is a spatial measure of line type, as shown by the symbol $\rightarrow$.

The Route measure as a temporal point type allowing Deliveries to be aggregated along the dimensions, for example the similar route could be merge into a single owner, the route could be union, intersect, etc. Thus, the query like “give me the total number trajectory by TruckOwner”, or “give me the total trajectory that passes road segment X in the month of February” could be answered. Query like “give the average of fruit loading time by month and afdeling”, where fruit loading time has been computed using spatial operator within a radius is possible to be computed. These queries are the example of a spatial roll-up function.

Figure 14. An example of the conceptual schema of the spatiotemporal Data Warehouse

“give me the total trajectory that passes road segment X in the month of February” could be answered. Query like “give the average of fruit loading time by month and afdeling”, where fruit loading time has been computed using spatial operator within a radius is possible to be computed. These queries are the example of a spatial roll-up function.
Thus, Spatiotemporal Slice also possible to determine like query “Give the aggregate of fruit weight deliveries within the location of Block Geo (polygon \((102.251223\ 55.4745345; \ 102.251233 \ 55.474535; \ldots)\) in a week that begin from 28 March 2019”, spatiotemporal dice query like “Give the average duration of fruit deliveries from the FCD location and PlantGeo within 5 km in an hour interval from 7.00 AM on 28 March 2019, temporal aggregation query like “For truck with the velocity 20 km/h, give the total distance travelled by each of the truck”, and spatial slice like “Compute the deliveries that traversed at least two plantation afdeling”.

6.2 Spatiotemporal Multidimensional Data Model on the Semantic Web

The semantic web continues to grow with various types of data, including for spatiotemporal data. Spatiotemporal data continues to grow due to the use of mobile devices, GPS, IoT, network sensors and location-based applications. Development of Spatiotemporal Multidimensional Data model on the semantic web starts from the Spatial Semantic Web, or commonly referred to as Geospatial Semantic Web. The Geospatial Semantic Web development began with the finding of a new retrieval method for geospatial data built on the semantics of spatial and ontologies developed at the University of Maine [69]. Then, Basic Geo Vocabulary has been standardized by W3C Semantic Web Interest Group using WGS84 as a reference datum [70].

Perry et al. instated that the Web has abundant spatial and temporal data, and the technology of SW potentially could make the accessibility and usefulness of data better. Because of the lack of ability of SPARQL to query complex spatial and temporal data, therefore Perry et al. proposed a new query language SPARQL- ST, which an extension of SPARQL for complex spatiotemporal queries. This research suggested a formal syntax and semantics and also added spatial variables and constructs for manipulating temporal triples in SPARQL-ST and applied as a prototype built on top of a commercial DBMS [71]. This is the approach that combines spatiotemporal semantic web, but limited only for basic operation for spatiotemporal like a topological and temporal relationship, but not for aggregation and analytic query functions.

Research continues to grow and has been successfully implemented such as Linked Geospatial Data in the UK government, followed by the manufacture of geospatial datasets by the Ordnance Survey Company for regions in the UK that can be accessed using SPARQL Endpoints [72]. Linked data becoming popular with the advent of Geonames, which is a dataset in the form of linked data that collects spatial and thematic information for place names in various hemispheres in various languages. The information stored in it is in the form of latitude, longitude, altitude, population, and administrative information with the rules of the World Geodetic System 1984 (WGS84). Furthermore, there is LinkedGeodata, which is a linked data which is a semantic web infrastructure that is converted from OpenStreetMap, this linked data is very useful for integrating and aggregating data related to maps [73] and can be easily queried with SPARQL. This approach attracts many researchers as a promising spatial linked data paradigm, but still, this approach did not cover temporal data.

The temporal aspect then entered as a Spatiotemporal Semantic Web on the development of YAGO2 ontology which is a continuation of YAGO knowledge-based ontology where entities, events, and facts are combined with information on space and time. YAGO2 was developed by automating Wikipedia, GeoNames, and WordNet linked data. At present YAGO2 contains 447 million facts and 9.8 million entities. YAGO2 uses the SPOTL model data (5 tuples), which is the extension of SPO (3 tuples). Entities on YAGO2 are assigned a time span, while fact is assigned a time point or time span [74]. YAGO2 become a good methodology for enriching large spatiotemporal knowledge bases but this approach did not have a query extension for this spatiotemporal representation.

Furthermore, a query language with the addition of geographic features on SPARQL has developed, namely GeoSPARQL. GeoSPARQL is an SW vocabulary that provides geospatial data representation [75]. GeoSPARQL has two essential parts: an ontology for storing geospatial objects, and a set of query functions for processing relationships between the geospatial entities. The ontology is developed from the OGC standards that have expressive concepts and terminology. The ontology
of the GeoSPARQL is built to be small for easily understood and attached. GeoSPARQL ontology has two main classes: Feature and Geometry. A Feature is an entity with spatial attributes. An example of the Feature is a building, statue, palace, lake, etc. A Geometry is a shape, for example, a point, line, triangle, hexagon, etc. and is used as a representation of a feature’s spatial location. The third class, SpatialObject, is a superclass of both Feature and Geometry. GeoSPARQL has become as a geospatial RDF standard from W3C for data modeling and querying [76]. GeoSPARQL has some impressive features for geospatial implementation on SW, but this language did not accommodate for analytical query and has no extension for spatiotemporal and mobility data representation and query.

Further, EU research running the GeoKnow project for three years from late 2012 to 2015. This project is the extension of the LinkedGeoData project, which develops OpenStreetMap that makes data available as an RDF base. The project applies the RDF model and the GeoSPARQL standard as the basis for representing and querying geospatial data. GeoKnow contributive findings are (a) introduction of query optimization methods of geospatial RDF for better performance than existing RDF store, even still lack analysis performances compared to relational DBMS (b) aggregation of geospatial RDF data with fusion [77]. The adoption of the RDF Triple store for Semantic Geospatial and GeoSPARQL queries developed with the advent of Parliament RDF [78].

Another proposal similar to GeoSPARQL is the development of stRDF/stSPARQL. The stRDF is a data model with an extension of RDF to represent geospatial information that changes over time [79]. stRDF defines spatial and temporal dimensions that have literal spatial and spatial data types. stRDF also uses OGC standards like WKT and GML for serialization. stSPARQL was developed as an extension query language for SPARQL by adding function defined in the OpenGIS standard Simple Feature Access. These functions are in the form of basic functions (get, test), basic function access functions (equals, disjoint, intersect, touches, crosses, within, contains, overlaps, relate), Egenhofer, RCC8, spatial analysis functions, spatial metric functions (distance, area), the function of aggregate spatial (union, intersection, extent). Strabon was then developed as an RDF store that supports semantic geospatial query languages in stSPARQL and GeoSPARQL. Strabon has expressive power by these query languages with the data stRDF model. The Performance of Strategic scales to vast volumes of data and performs well [79]. stRDF/stSPARQL has accommodated many features of spatial data representation and query implementations, but it still lacks spatiotemporal data adoption and analytical capabilities.

Zhang et al. proposed an extension of SPARQL to spatiotemporal modeling and querying a quantitative spatiotemporal relationship. The extension model is adding an event model with time and space. The query extension created 30 new query operators that claimed could effectively find the unseen connections between entities in event ontology and have excellent performance and effectiveness [80]. This approach comprehensively adds the functionality of SPARQL but this approach still does not handle the spatiotemporal analytical query.

On the other hand, Gur et al. proposed QB4SOLAP, a generic and extensible vocabulary (meta-model) for spatial DW on the SW. QB4SOLAP extends QB4OLAP vocabulary with spatial concepts. They also give a formalization of QB4SOLAP. This paper has defined the critical concepts of spatial cube numbers, spatial hierarchies and levels, spatial measures, spatial aggregation functions, and topological relations among spatial dimension and hierarchy level members. They also defined several analytical spatial OLAP operators over QB4SOLAP, the formal semantics of these operators, and algorithms for generating spatially extended SPARQL queries [8]. This work has a significant result for modeling and querying spatial analytical data but this work is only limited for spatial data and not for spatiotemporal data that have the more dynamic characteristics.

The summary of the completeness of the model and query for spatiotemporal multidimensional data analysis shown in table 3. This table shows that there are still many data representations/model and query operators that have not been accommodated in those kinds of literature, such as spatiotemporal facts, measures, operators, temporal aggregation operators, and spatiotemporal aggregation operators. This opportunity will be our future work for the year to come.
Table 6. The Summary Of The Completeness Of The Spatiotemporal Analytical Data Model And Query

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7 CONCLUSION AND FUTURE WORKS

BI grows with the ability to adapt to external data sources that have an unstructured, semi-structured, and flexible format. This ability has been supported by Semantic Web (SW) technology as a concept of sharing data on the web with its semantics, and intelligent querying with active inference and reasoning on the data. Linked Open Data on the SW is an important source to support BI. The state-of-the-art SW technologies help advanced analytics over spatial and non-spatial SW data.

SW has a great vision to represent data on the web in a machine-readable way and could add semantic annotation so that information on the web could be retrieved and processed by machine or human effectively. SW technologies open a new paradigm of integration data, transparency data, semantically linked data using description logic for inference tasks. SW sets shared vocabularies
semantically express metadata and provides data annotations over web data with semantic through RDF and ontology, which then generates Semantic Linked Data. The availability of a web of data can be access using query language named SPARQL with its endpoint and support intelligent querying.

For publishing linked data cube/statistical data, vocabulary is a core foundation. Many vocabularies have been created to enable modeling multidimensional data with facts, dimensions, and hierarchies as RDF graphs and mechanism to query RDF graph with OLAP operators. The work-related to the modeling and querying multidimensional data reported in this paper may be continued in many directions. We present the next several areas in which extensions may be developed.

7.1 Linked Cube Data Model

As previously described in the section of the data cube linked model, modeling and querying are fundamental aspects of data warehousing. The DW model is crucial for data representation and how data will be stored. The querying methods also necessary for retrieving and visualizing the information for decision making. Table 2 summarized the completeness of the model and querying on linked cube data / semantic web including SDMX, SCOVO, SKOS, XKOS, QB, OC, QB4OLAP, and CQL. But all the models still open for further research. These models even did not support many to many relationships between facts and dimensions, multiple hierarchies, alternative hierarchy, and parallel hierarchy representation. These models also did not allow query functions such as pivot, drill across, and drill through to be implemented. The authors will propose the solution to this problem in the next works.

7.2 Spatiotemporal Multidimensional Data model and query on Semantic Web

Spatiotemporal analytic for multidimensional data on SW has been attracting many researchers. Nevertheless, the research of modeling and querying of spatiotemporal multidimensional data on SW still leaves quite a lot of work to do. Geospatial SW successfully develops semantics and ontology for modeling features and geometries. LinkedGeoData and YAGO2 also have a significant contribution to modeling the spatial and temporal aspects of multidimensional data on SW. However, these approaches still lack of functionality to query spatiotemporal multidimensional data for analytical purposes.

Furthermore, the SPARQL language has been successfully extended to accommodate spatiotemporal functionalities such as SPARQL-ST, GeoSPARQL, and stSPARQL, but the extension still did not accommodate spatiotemporal aggregation operators. The last proposal by Gur et al. [8] has a significant contribution to modeling and querying spatial DW for analytical purposes, but these works is only accommodated for spatial multidimensional data, while models for more dynamic data, like spatiotemporal, and moving objects DW have not been defined. Querying in the spatiotemporal data warehouse on the semantic web also leaves several important queries such as spatiotemporal rollup, slice, dice, drill-down, drill-across, and combination of these operations that still have to be further investigated. The authors will work in this area in the coming year.

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