

A MODIFIED BIT PLANE COMPLEXITY SEGMENTATION STEGANOGRAPHIC METHOD: INCREASING PAYLOAD IMPERCEPTIBILITY AND ROBUSTNESS

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ABSTRACT

Embedding of secret information in a digital image will definitely introduce some noise or modulate the image signal in some way. A good steganographic method ensures that such noise is not perceptible or is minimal in order to maintain the fidelity of the vessel. The Bit Plane Complexity Segmentation (BPCS) method uses the Canonical Gray Coded (CGC) bits of the complex bit plane blocks of a vessel image for embedding secret information. Though this guarantees a high payload capacity, it can potentially compromise the fidelity of the vessel particularly in its high order bits. To ensure that the vessel is evenly modulated and hence increase imperceptibility of the embedded data, this paper suggests a tweaking of the BPCS embedding procedure by employing a random selection of the CGC bits in the noisy regions of the vessel. Additionally, in order to boost the vessel's robustness against compression and other image processing activities, the proposed embedding procedure does not utilize the 0 (zero) CGC bit plane, which is normally targeted for removal by such activities. Results from the experiments carried out showed that stego images from the proposed method had improved signal to noise ratios compared to those from the traditional BPCS method.

Keywords: *Steganography, Fidelity, Floor Noise, Payload, Compression, Embedding Rate*

1. INTRODUCTION

All steganographic algorithms must comply with basic requirements for steganography. The most important of this requirement is that the embedding procedure must not leave perceptible distortions in the carrier vessel. This ensures that the fidelity of the carrier file is not compromised and that the stego image's statistical characteristics are consistent with those of the original image [1]. The second requirement is to ensure that the embedding procedure provide for adequate payload capacity. This is the size of information that can be embedded relative to the size of the cover file without degrading it [2]. A good steganographic algorithm should therefore ensure a high payload capacity without perceptibly degrading the carrier vessel. Lastly, the secret information should be embedded robustly to guard against effects of vessel manipulation on the embedded data.

Robustness ensures that a carrier vessel can withstand some level of modification without necessarily affecting the integrity of the hidden information [3].

According to [4], it is difficult to effectively ensure that an embedding procedure meets all the three requirements at the same time. There must therefore be a balanced trade-off between them. [3] Defined this trade-off as the data-hiding problem space. He outlines that in order to achieve robustness, redundant encoding of the embedded data on the cover-medium must be performed, which in turn definitely compromises capacity. Working on the midpoint between imperceptibility and hiding capacity provides an optimum balance between the two parameters [5]. This is illustrated in figure 1 based on the Fridrich's diagram for the data-hiding problem space, which depicts the

mutually competitive nature of these parameters [2].

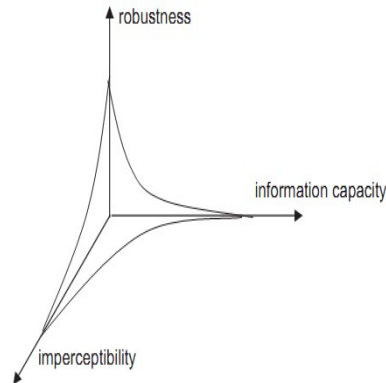


Figure 1: The Data-hiding problem space

2. THE BPCS METHOD

BPCS embedding technique was firstly introduced by Kawaguchi and Eason [6] as a solution to the low payload capacity of the traditional steganographic methods. In this method, the bits of the carrier vessel are first converted from the Pure Binary Code (PBC) to the CGC. Embedding secret data using the CGC bits pattern leaves less distortion to the original image bit map hence improving on the imperceptibility of the vessel [7]. The image is then subdivided into several bit planes, which are categorized as either “informative” or “noisy”. Noisy bit planes have high complexity. A threshold value $\alpha_0 = 0.3$ is used to determine the complexity of a bit plane by measuring how many times the bit of an image plane changes from 0 to 1 and from 1 to 0 [8]. If the complexity of any given bit plane exceeds the threshold, it is skipped during the embedding process. The complexity of the secret data to be embedded is also calculated and if found to be below the threshold value, it is conjugated to make it complex before it is embedded in the carrier file [9]. For a $2^n \times 2^m$ gray scale black and white image with black as the foreground area and white as the background area, conjugation operation proceeds as follows:

i) Two checkboard patterns W_c and B_c are

introduced where W_c has white pixel (i.e 1) at the upper left position and B_c has a black pixel (i.e 0) upper left position.

ii) Image P is introduced which has its pixels in foreground area with B (black) pattern, and its pixels in the background area with W (White pixels).

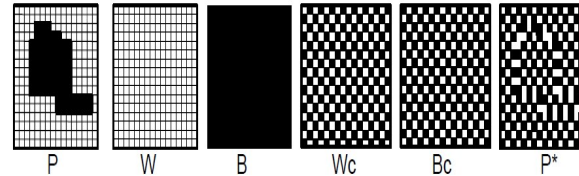


Figure 2: Conjugation binary patterns

iii) P^* is then defined as the conjugate of P satisfying the following conditions:

- The foreground area shape is the same as P
- The foreground area has the B_c pattern
- The background area has the W_c pattern

The following properties hold true for the conjugation operation. [9]

- $P^* = P \oplus W_c$ where \oplus designates exclusive OR
- $P^* \neq P$
- If $\alpha(P)$ is the complexity of a given image P , then,
 $\alpha(P^*) = 1 - \alpha(P)$. (1)

Since the Human Visual System (HVS) is more sensitive to patterns represented by the informative regions of the image, embedding of secret data is done in the noisy bit plane blocks in order to effectively conceal the information [5]. The method utilizes both the Most Significant Bits (MSB) and the Least Significant Bits (LSB) of the noisy blocks of the vessel ensuring a significantly high embedding rate compared to the traditional LSB methods which utilize only the LSBs of the vessel. The BPCS embedding procedure is summarized in figure 3.

Input $m \times n$ vessel Image

- Transform carrier image from PBC to CGC
- Segment each bit-plane of the vessel image into informative and noise-like regions using the threshold value $\alpha_0 = 0.3$
- Group the bytes of the secret file into a series of secret blocks
- If a block (S) is less complex than threshold, then conjugate it to make it more complex block.
- Embed each secret block into the noise-like regions of the bit-planes.
- Convert the vessel image from CGC back to PBC

Output stego Image (s_1)

Figure 3: BPCS embedding procedure

One of the advantages of the BPCS embedding technique is its high payload capacity. However due to the data hiding problem space, increased payload in a vessel imparts negatively on imperceptibility. Additionally, robustness of the carrier vessel against image processing activities such as compression is key to ensuring that the embedded information is safe. BPCS is not robust to even small changes in the image unless the secret data is embedded in high order bit planes which would consistently compromise on the imperceptibility of the vessel [6]. The BPCS embedding framework is shown in figure 4.

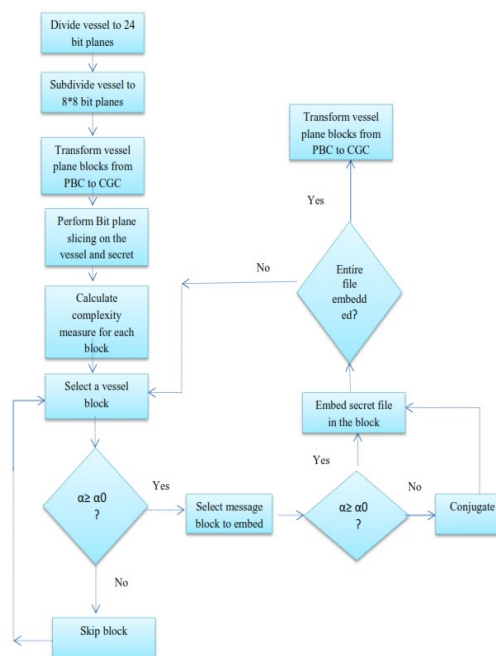


Figure 4: BPCS embedding framework

3. THE PROPOSED METHOD

To increase imperceptibility and robustness in the traditional BPCS method, this paper proposes a modification to its embedding procedure by tweaking it using the Marsenne Twister (MT) Pseudo Random Number Generator (PRNG), in order to randomly scatter the bits of the secret data in the CGC bits of the carrier vessel. MT provides for fast generation of very high-quality pseudorandom numbers with a long period length which is chosen to be a mersenne prime [10]. Using the PRNG to spread the bits of the secret data within the bit planes of the vessel not

only ensures that the modulation of the carrier vessel is uniformly done, but also that the extraction of the embedded data and the eventual reconstruction of the embedded file is impossible without the original seed used in generating the pseudo random numbers [11]. This further increases the security of the embedded data.

To improve on the robustness of the stego system, the 0 bit plane of the noisy region of the vessel is skipped during the embedding process as it is normally targeted for removal by lossy compression algorithms. The summary of the proposed embedding and extraction procedures are shown in figure 5 and figure 6 respectively. The complete proposed MBPCS framework is shown in figure 7. The highlighted areas indicate the proposed modifications.

Input: An $m \times n$ Image (S), M (secret file)
Output: Stego image ($S1$)

Algorithm: Steps-

1. Divide S to 24-bit planes
2. Sub divide S to 8×8 plane blocks
3. Transform the S blocks from PBC to CGC
4. Perform bit plane slicing on S
5. Calculate the complexity measure 'alpha' (α) for each bit plane block of vessel image (S)
6. Calculate the complexity measure alpha' (α') for each bit plane block of the secret image M
7. Mask the 0 bit plane
8. Carry out conjugation operation on the "informative" blocks of M i.e if $\alpha \geq \alpha_0$ Where $\alpha_0 = 0.3$ (conjugation threshold).
9. Use mersenne twister to select a random CGC bit for writing
10. Let bitToWrite [x][y] denote the selected CGC bit for writing
11. Let M_i [x][y] denote the secret message bit embedded in a CGC bit for all image color channels do the following:
12. If $CGC(\text{bitToWrite}[x][y]) = M_i[x][y]$ skip this bit
13. If $CGC(\text{bitToWrite}[x][y]) \neq M_i[x][y]$ then
14. $\text{bitToWrite}[x][y] = M_i[x][y]$
15. While secret file length; Repeat step 9 to 14 to embed the entire data
16. Convert the entire vessel from CGC back to PBC.

Figure 5: Proposed MBPCS embedding procedure

Input: Stego Image (S1) (image containing embedded M)
Output: M file
Algorithm: Steps-

1. Divide S to 24-bit planes
2. Sub divide S to 8*8 plane blocks
3. Transform S1 from PBC to CGC
4. Perform bit plane slicing on S1
5. Calculate the complexity measure for each bit plane block of stego image (S1)
6. Use MT to select a random CGC bit in the noise-like block region
7. Let bitToRead [x][y] denote the selected CGC bit for reading
8. Let M_i denote the message bit read in the noise-like block of the vessel
9. If $CGC(\text{bitToRead}[x][y]) \neq M_i$ skip this bit
10. If $CGC(\text{bitToRead}[x][y]) = M_i$ then
11. $\text{bitToRead}[x][y] = M_i$
12. Pack bit in bitSet
13. While secret file length; Repeat step 6 to 12 to read entire M

Figure 6: Proposed MBPCS extraction procedure

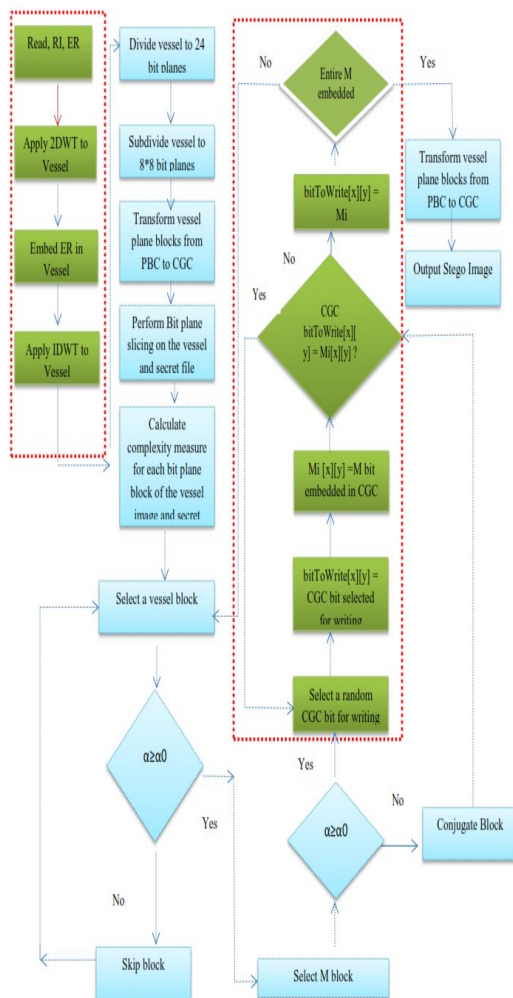


Figure 7: Proposed MBPC framework

4. EXPERIMENT RESULTS AND PERFORMANCE EVALUATION

An experiment was set up to compare the results of the proposed method with those of the traditional BPCS method. The quality of the stego images produced by each method was evaluated through an objective quantitative criterion where the metric $\Theta(x,y)$ was used to estimate the difference between a stego image and the original reference vessel image. Twenty randomly sampled payload images were used in this experiment. These were embedded in five standard steganographic test images as vessels (i.e Lenna.png, Boat.png, House.bmp, Peppers.png and Fruits.png). The results were then analyzed using full reference image error sensitivity analysis metrics [12]. The tests assume that the original perfect vessel image is available for comparison with the stego image [13]. The experiment ensured the following constants.

- i) Same steganography test images were used on both the methods.
- ii) Equal payload images were embedded in each vessel.
- iii) Same quality evaluation metrics were measured and recorded.
- iv) All the tests were implemented and run on a PC pentium IV Duo core, 2.1 GHz with 2GB of RAM Under the Windows 7 Home Edition operating system.

Tables 1 and 2 summarizes the characteristics of the test data images used.

Table 1: Test data images (Payloads)

File Name	Dimension	File Size	Remarks
PL1	512 X 512	87.5 Kilobytes	Payload 1
PL2	512 X 512	92 Kilobytes	Payload 2
PL3	512 X 512	105 Kilobytes	Payload 3
PL4	512 X 512	117 Kilobytes	Payload 4
PL5	512 X 512	76 Kilobytes	Payload 5
PL6	512 X 512	161 Kilobytes	Payload 6
PL7	512 X 512	165 Kilobytes	Payload 7
PL8	512 X 512	191 Kilobytes	Payload 8
PL9	512 X 512	232 Kilobytes	Payload 9
PL10	512 X 512	239 Kilobytes	Payload 10
PL11	512 X 512	240 Kilobytes	Payload 11
PL12	512 X 512	252 Kilobytes	Payload 12
PL13	512 X 512	324 Kilobytes	Payload 13
PL14	512 X 512	350 Kilobytes	Payload 14
PL15	512 X 512	394 Kilobytes	Payload 15
PL16	512 X 512	420 Kilobytes	Payload 16
PL17	512 X 512	410 Kilobytes	Payload 17
PL18	512 X 512	426 Kilobytes	Payload 18
PL19	512 X 512	454 Kilobytes	Payload 19
PL20	512 X 512	460 Kilobytes	Payload 20



Figure 8: Test data (vessel images)

Table 2: Test data (Vessels)

File Name	Dimensions	File Size	Remarks
Lenna.png	512 x 512	117 Kilobytes	Vessel 1
Boat.png	512 x 512	174 Kilobytes	Vessel 2
House.bmp	512 x 512	258 Kilobytes	Vessel 3
Peppers.png	512 x 512	527 Kilobytes	Vessel 4
Fruits.png	512 x 512	426 Kilobytes	Vessel 5

Figure 8 shows the vessel images used as test data for this experiment.

4.1 Evaluation Metrics

The Mean Square Error (MSE) and the Peak Signal to Noise Ratio (PSNR) full reference metrics were used to compare the quality of the stego image signals produced by each method under equal payloads.

4.1.1 The MSE

MSE measures the average pixel intensity difference between two images, in this case the original and the stego image [14]. MSE is calculated using equation 1. Lower levels of MSE indicate a better quality image signal [12].

$$MSE_{AVG} = \frac{1}{(MN)} \sum_{i=1}^M \sum_{j=1}^N (X_{ij} - \bar{X}_{ij})^2 \quad (2)$$

Where:

X_{ij} is the i^{th} row and the j^{th} column pixel

in the original vessel image,

$\overline{X_{ij}}$ is the i^{th} row and the j^{th} column pixel

in the stego image,

M and N are the height and the width of the image.

Table 3 shows a comparison of MSE bench mark test results for the traditional BPCS method and the proposed Modified Bit Plane Complexity Segmentation (MBPCS) technique using vessel 1 (lenna.png) with payloads 1 to 4. These results are further summarized in figure 9.

Table 3: MSE for Vessel 1

Embedding Technique	Payload 1	Payload 2	Payload 3	Payload 4
BPCS method	12.10	11.91	10.77	11.10
MBPCS method	3.0	2.93	2.77	2.78

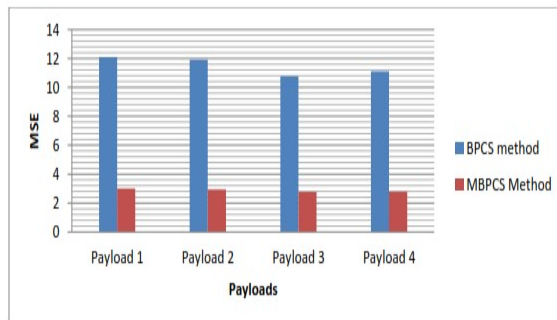


Figure 9: MSE for vessel 1

Table 4 shows a comparison of MSE bench mark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 2 (boat.png) with payloads 5 to 8. These results are further summarized in figure 10.

Table 4: MSE for vessel 2

Embedding Technique	Payload 5	Payload 6	Payload 7	Payload 8
BPCS method	13.55	13.58	13.60	13.62
MBPCS method	4.51	4.60	4.57	4.53

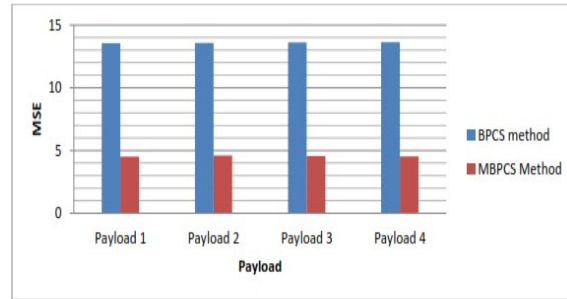


Figure 10: MSE for vessel 2

Table 5 shows a comparison of MSE bench mark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 3 (house.bmp) with payloads 9 to 12. These results are further summarized in figure 11.

Table 5: MSE for vessel 3

Embedding Technique	Payload 9	Payload 10	Payload 11	Payload 12
BPCS method	13.12	12.96	12.87	13.07
MBPCS method	4.17	4.15	4.18	4.15

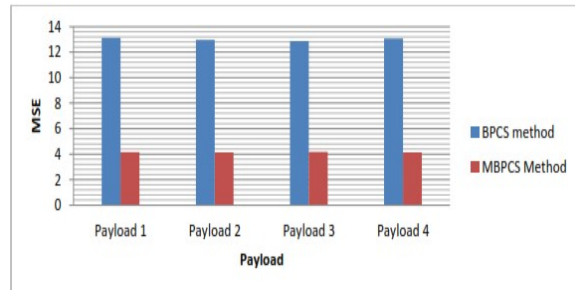


Figure 11: MSE for vessel 3

Table 6 shows a comparison of MSE bench mark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 4 (peppers.png) with payloads 13 to 16. These results are further summarized in figure 12.

Table 6: MSE for vessel 4

Embedding Technique	Payload 13	Payload 14	Payload 15	Payload 16
BPCS method	11.88	11.65	11.85	11.86
MBPCS method	2.96	2.92	2.96	2.96

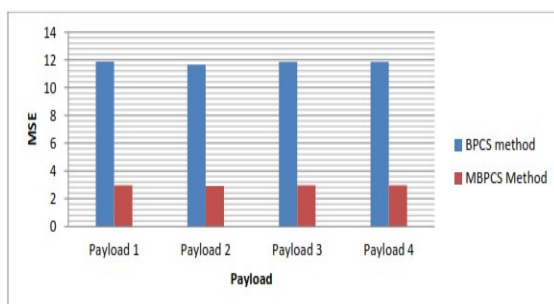


Figure 12: MSE for vessel 4

Table 7 shows a comparison of MSE benchmark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 5 (fruits.png) with payloads 17 to 20. These results are further summarized in figure 13.

Table 7: MSE for the vessel 5

Embedding Technique	Payload 17	Payload 18	Payload 19	Payload 20
BPCS method	11.78	12.01	12.12	11.81
MBPCS method	2.93	2.99	3.04	2.94

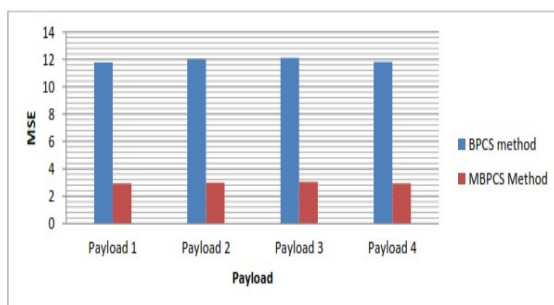


Figure 13: MSE for vessel 5

The proposed MBPCS posted lower levels of MSE metrics in all the vessels for all the payloads considered. It was also noted that increase in payload resulted in minimal changes in MSE metrics for the proposed method compared to the traditional BPCS. Since MSE is the squared euclidean norm of the pixel-wise difference between the reconstructed and the original image, the proposed embedding algorithm ensures minimal and equitable pixel differences in the stego files.

4.1.2 The PSNR

PSNR is used for comparing the value of the required image signal against the value of a corrupting noise in decibels [15]. The lesser the value of PSNR, the more perceptible the background noise [16]. The value of PSNR is computed using equation 2.

$$PSNR = 10 \cdot \log_{10} \frac{I^2}{(MSE)} db \quad (3)$$

Where:

I is the dynamic range of pixel values $I=255$ for 8-bit images.

MSE is the Mean Square Error.

Table 8 shows a comparison of PSNR benchmark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 1 (lenna.png) with payloads 1 to 4. These results are further summarized in figure 14.

Table 8: PSNR for the vessel 1

Embedding Technique	Payload 1	Payload 2	Payload 3	Payload 4
BPCS method	46.84	46.91	47.34	47.21
MBPCS method	52.89	52.99	53.24	53.22

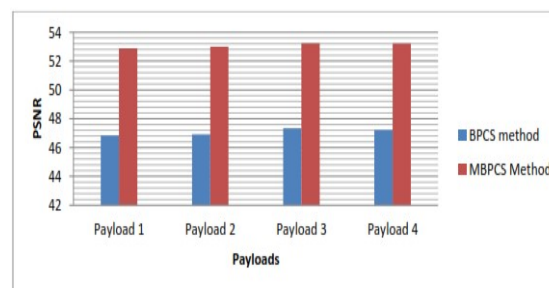


Figure 14: PSNR for vessel 1

Table 9 shows a comparison of PSNR benchmark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 2 (boat.png) with payloads 5 to 8. These results are further summarized in figure 15.

Table 9: PSNR for the vessel 2

Embedding Technique	Payload 5	Payload 6	Payload 7	Payload 8
BPCS method	46.35	46.34	46.33	46.32
MBPCS method	51.12	51.04	51.06	51.11

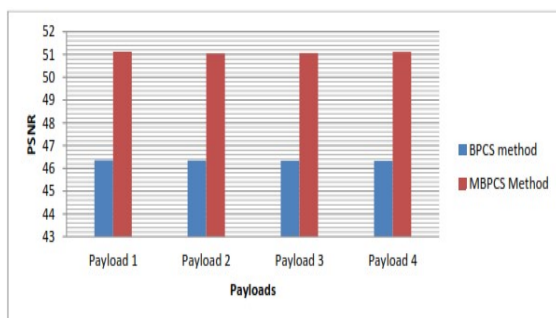


Figure 15: PSNR for vessel 2

Table 10 shows a comparison of PSNR bench mark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 3 (house.png) with payloads 9 to 12. These results are further summarized in figure 16.

Table 10: PSNR for the vessel 3

Embedding Technique	Payload 9	Payload 10	Payload 11	Payload 12
BPCS method	46.49	46.54	46.57	46.50
MBPCS method	51.46	51.48	51.45	51.48

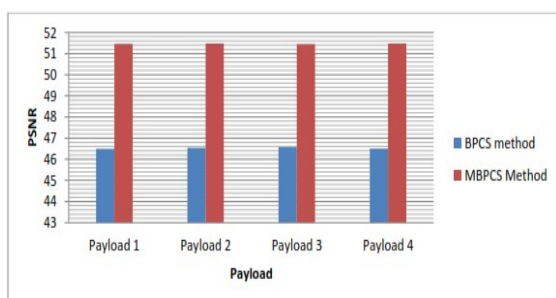


Figure 16: PSNR for vessel 3

Table 11 shows a comparison of PSNR bench mark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 4 (peppers.png) with payloads 13 to 16. These results are further summarized in figure 17.

Table 11: PSNR for the vessel 4

Embedding Technique	Payload 13	Payload 14	Payload 15	Payload 16
BPCS method	45.80	45.89	45.82	45.81
MBPCS method	51.84	51.90	51.84	51.83

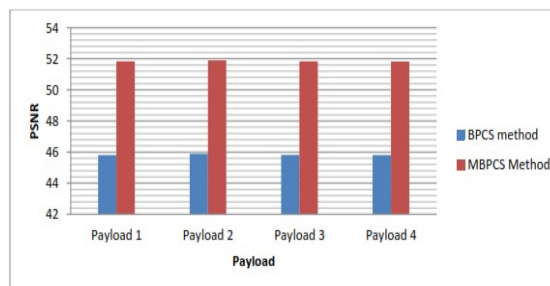


Figure 17: PSNR for vessel 4

Table 12 shows a comparison of PSNR bench mark test results for the traditional BPCS method and the proposed MBPCS technique using vessel 5 (fruits.png) with payloads 17 to 20. These results are further summarized in figure 18.

Table 12: PSNR for the vessel 5

Embedding Technique	Payload 17	Payload 18	Payload 19	Payload 20
BPCS method	46.95	46.87	46.83	46.94
MBPCS method	52.99	52.91	52.83	52.98

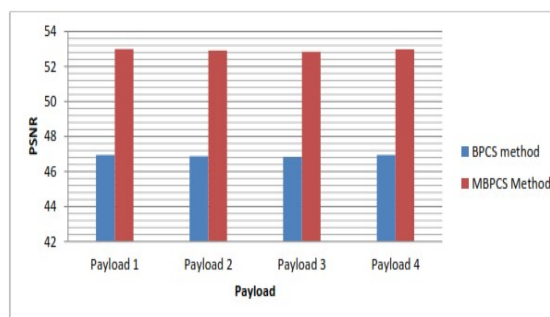


Figure 18: PSNR for vessel 5

The pseudo random technique employed in scattering the bits of the secret data in the bit planes of the carrier vessel in the proposed MBPCS method ensured that the deviation in pixel values between the original image signal and the reconstructed signal is minimal thereby enhancing imperceptibility of the embedded data. This was evidenced by the comparatively higher PSNR outputs recorded by the stego images of the proposed method. Compared to the traditional method, increase in payloads resulted in minimal changes in the PSNR measure for the proposed method indicating less detectable noise as the vessel is smoothly and uniformly modulated during the embedding process.

5. RESEARCH CONTRIBUTION

The study and the findings established in this research contributes to the theory and the practical application of information hiding techniques by tackling the data hiding problem space in stego systems thereby improving the embedding capacity and robustness of a carrier vessel. A steganographic artifact that provides a high payload capacity, while ensuring that the vessel is robust against compression and filtering consequently represents a contribution in this area. Based on the results presented and discussed in this paper, the proposed MBPCS method clearly provides an improved high hiding capacity while ensuring that the fidelity and quality of the carrier file remains fairly uncompromised. This is in comparison to existing LSB techniques and the original BPCS method. Therefore the proposed embedding method therefore presents an acceptable trade-off between high payload capacity and the stego image robustness reducing the data hiding problem space.

Data imperceptibility is at the core of any usable steganographic method. While embedding information in a digital image is definitely expected to introduce noise or modulate the cover image in some way [17], the important thing is to ensure that the introduced noise does not degrade the perceived quality of stego image in order to maintain the security of the steganographic system. In this paper, an embedding technique that utilizes the marsenne twister PRNG to randomly and uniformly scatter the information within the CGC bits of vessel's bit planes forms a significant contribution compared to the techniques used in the traditional LSB and BPCS methods. This is demonstrated by the MSE and PSNR results presented. Increased imperceptibility of the embedded information in a carrier file helps to ensure the security of the entire steganographic system. A good steganographic method therefore ensures that the embedding procedure introduces minimal noise to the carrier vessel in order to ensure that the statistical characteristics of both the original vessel and the stego image are almost indistinguishable [18].

6. CONCLUSION

Imperceptibility of the embedded information is at the core of any usable steganographic method. While embedding information in a digital image is definitely expected to modulate the cover image in some way [14], the important thing is to ensure that the introduced noise does not perceptibly degrade the vessel in

order to guarantee the security of the embedded data.

In this paper, an embedding technique that utilizes the MT to randomly and uniformly scatter the information within the CGC bits of the vessel's noise like bit planes was proposed and evaluated. MSE and PSNR results demonstrated improvements on the quality of stego images produced by the proposed technique. In any steganographic method, imperceptibility of the hidden data cannot be compromised and a good steganographic method should ensure that the embedding procedure introduces minimal noise to the carrier vessel [14].

7. RECOMMENDATION AND FUTURE WORK

The steganographic method presented in this research was found to be significantly effective as it makes minimal imperceptible modifications to the cover images. In comparison to existing traditional LSB methods, the proposed MBPCS method posted relatively superior results in most of the bench mark tests in steganography. As is the practice in digital image steganography, the recommended carrier images should be original photographs taken from high quality digital cameras. The recommended mode of transmission of the stego images is through web postings, email attachments, electronic bulletin boards and by file transfer such as file transfer protocol (FTP) (Cole,2013). Whichever method of transmission is chosen, it should be one that prevents tracing by potential attackers.

To further strengthen the proposed method, other carrier files and stego media such as audio, video and text can be tested for this application to establish their versatility in terms of data hiding problem space and security.

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COMPETING INTERESTS

The authors declare that they have no competing interests.

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