ESTIMATION ALGORITHM OF SULFATE CONCENTRATION AT THE SEA SURFACE BASED ON LANDSAT 8 OLI DATA

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ABSTRACT

A model to estimate an element on the earth's surface by remote sensing technique is known as estimation algorithm. Many researches have been conducted to develop estimation algorithm particularly on the elements of the sea surface using Landsat imagery data such as sea surface salinity, sea surface temperature, total suspended solids, chlorophyll-a, etc. This study aimed to develop estimation algorithm of sulfate concentration at the sea surface of Madura Strait waters. Knowing the sulfate concentration at the sea surface was very important for concrete planners to construct a mixture of concrete elements that best matches the existing environmental conditions based on SNI 2847-2013 about the class of sulfate exposure. Besides, it was beneficial for salt farmers as it makes them easier to know the process of precipitation of unnecessary elements in the process of producing salts such as magnesium sulfate (MgSO4). The algorithm was constructed using regression models both linear and nonlinear, including multiple regressions, in which RRS NIR (Band 5) of Landsat 8 OLI as predictor variable and sulfate as the response variable. The finding showed that nonlinear power regression model was the best algorithm to estimate the sulfate concentration at the sea surface than other models with error value (NMAE) 9.53% and residue value (RMSE) 320.84. In the model which was developed, the intercept value was 3055.5 and the slope value was 0.049.

Keyword: Sulfate, Reflectance remote sensing (Rrs), Landsat 8 OLI, Estimation algorithm, Data mining, Madura Strait

INTRODUCTION

Sulfate is one of the polyatomic ion compounds (SO4^{2-}) [1], [2]. Sulfate concentration in seawater influences concrete buildings and salt production [3], [4], thus, knowing the distribution of sulfate concentration at the sea surface becomes important for concrete planners and salt farmers. Knowing the composition of seawater elements at the sea surface is usually done by taking seawater samples to be analyzed in the laboratory (conventional technique); it is usually done to estimate the sea salinity, TSS, sulfate concentration, chlorophyll-a [5],[6],[7],[8]. However, in the development of remote sensing technology, the concentration of the sea surface elements could be estimated by analyzing satellite recorded images using certain algorithms [9], [10]. Its technique can be more effective approach than an in-situ field measurement since it can cover a very wide area [11]. Different from the conventional technique in which the value of sulfate obtained at only one sample point. Certain algorithms have been developed to estimate certain aspect such as sea surface temperature [12], [13], sea surface salinity [6], [7], [13]–[15], chlorophyll-a and TSS [8], [16],[17], and sea surface sulfate concentration [18].

The use of algorithm in elemental extraction at sea surface by analyzing the recorded images both spectral and temporal was very effective since it can cover a very wide area [11]. The algorithm itself was developed using a data mining methods i.e regression equations with image data of remote sensing as predictor variable [19],[20],[21],[22],[23]. In this research will be used linear and non linear regression [24]. The
algorithm was composed of various regression models to know the greatest coefficient of determination ($R^2$) as a basis for selecting a model [25],[26]. Furthermore, validation of the model was done by looking at the value of Root Mean Square Error (RMSE) or Normalized Mean Absolute Error (NMAE) in which the smaller value indicated that the model was good to be implemented [27],[28].

This research is the continuation of the previous research [18] for the development of sulfate estimation algorithm at the sea surface with Landsat 8 OLI data. In the previous research [18], the estimation algorithm model was constructed using regression equation with sulfate as the dependent variable and remote sensing reflectance (Rrs) on band 5 (NIR) Landsat 8 OLI image as the independent variable [29]. Selected regression model with the highest $R^2$ was a logarithmic model, such as $\log(SO_4) = 3.8033 - 0.411*\ln(\log(RrsB5))$, with $R^2=0.58$ and RMSE = 0.08 [18]. Algorithm development is intended to be more accurate in estimating sulfate concentration at the sea surface by adding training data as one of the principles of data mining.

The aim of this research is the development of an algorithm model to estimate sulfate concentration at sea surface by adding the sea surface salinity as the independent variable and the validation using Landsat 8 OLI image which was not done in the previous research. The formulation of the algorithm model used multiple regression since there were two independent variables or predictors, Rrs Band 5 (NIR) of Landsat 8 OLI and sea surface salinity, in order to obtain preferable determination coefficient ($R^2$) than the previous model. Next, the RMSE and NMAE values will be analyzed to validate the algorithm model which has been developed.

1. MATERIALS AND METHODS

2.1. Study Area

The study area of this research was the sea water of Madura Island, East Java Province, Indonesia; the south side is the Madura Strait and the north side is the Java Sea. It is located between 07°08’ 30”S - 07°44’ 27”S Latitude and 112°39’ 23”E - 114°05’ 24”E Longitude (Figure 1).

2.2. Data Collection

Data were collected from Madura Strait and the north side of Madura Island, or the Java Sea. It was collected twice: on November 23, 2015 (the researchers took the sea water of north area) and June 2, 2016 (the researchers took the sea water of south area along with the date of Landsat 8 passing by). The data required in this research were salinity, sulfate concentration, and reflectance remote sensing (Rrs) at sea surface. All data were taken at first hand for modeling algorithms and the image data is used as validation to test the implementation of the algorithm. Sea surface salinity and Band 5

![Figure 1: Study Area](image)
(NIR) Rrs of Landsat 8 OLI were the independent or predictor variable, while the sulfate concentration was the dependent variable or estimator.

2.3. Insitu Data Processing

The data of the sea surface salinity was taken using a refractometer. Collecting sulfate insitu data was done by taking seawater samples to be analyzed its sulfate concentration in the Laboratory of Environmental Engineering Department of ITS (Sepuluh November Institute of Technology) using turbidimetric method by means of UV-VIS spectrophotometer. While the data of surface Reflectance Remote Sensing (Rrs) was taken using TriOS Ramses spectroradiometer. Meantime, there were three types of data recorded by spectroradiometer TriOS Ramses; water upward radiance (Lu), downward radiance atmosphere (Ls) and downward irradiance atmosphere (Ed) (Figure 2) of which those values will be used later to calculate the Rrs value using formulas (1) and (2) since the Rrs cannot be directly taken on the field [8], [30], [31].

\[ R_{rs}(\lambda) = \frac{L_w(\lambda)}{E_d(\lambda)} \]  
(1)  
\[ L_w(\lambda) = L_u(\lambda) - \rho_s L_s(\lambda) \]  
(2)

where \( L_w \) (water leaving radiance /Wm\(^2\)sr\(^{-1}\)) is the radiance value obtained from the water column and the radiation reflected directly by the thin layer of the sea surface [32], \( L_u \) is upwelling radiance (Wm\(^{-2}\)sr\(^{-1}\)), \( L_s \) is downward radiance atmosphere (Wm\(^{-2}\)sr\(^{-1}\)), \( \rho_s \) is part of the reflectance which is on the surface of the waters derived from the reflection of the sun. \( \rho_s \) can be calculated using the Fresnel formula [33][8], or be calculated using the constant value of the research results [34], or constant value 0.02 as in Nababan research [32].

In recording the data, the spectroradiometer TriOS Ramses used a hyper spectralsensor with 320nm-950nm wavelength range and 3.3nm interval; so then it was done some adjustment based on the characteristic of Landsat 8 which has 11 bands. Landsat 8 has a 400nm-13000nm wavelength range which is divided into 11 bands.

![Figure 2: Graph of Water Upward Radiance, Atmosphere Downward Radiance, and Downward Irradiance](image-url)
In reducing Ramses data into Landsat 8 OLI characteristics, the researchers used the Relative Spectral Response (RSR) Landsat 8 value in calculating the mean of each band (Figure 3) by using formula (3).

\[ RSR_{mean} = \frac{1}{\Delta \lambda} \sum_{\lambda_1: RSR > 0.9}^{\lambda_2: RSR > 0.9} \Delta RSR \]  

where RSR is Relative Spectral Response and \( \lambda \) is wavelength.

2.4. Satellite Data Processing

The Landsat 8 OLI images which were used as data sets of the algorithm model application were available for free download on page https://earthexplorer.usgs.gov/ or on http://glovis.usgs.gov/ on path 118 and row 65. Landsat 8 OLI image taken out within the directory of Landsat Collection 1 Level-2 (On-Demand) was Landsat 8 OLI/TIRS C1 Level-2. Furthermore, to get the value of sea surface Rrs for each pixel of Landsat 8 OLI image, the first calculation was the division of the pixel value by 10000 to obtain the reflectance value. The result was then divided by a constant value of pi (\( \pi \)) to find the sea surface Rrs.

2.5. Data Mining

Data mining can be defined as a process aimed at finding a pattern of amounts large data since data is useless without analysis [24]. Data mining can be interpreted as a process to find interesting patterns and descriptive models that can be understood and predictive of large-scale data [35] or the process of discovering useful patterns and trends in large [36].

2.6. Regression Model

Regression is a statistical analysis technique to see functional relationship between two or more variables [37], [38]. In other literature, a variable can be predicted or estimated by other variables [39] by using regression calculation with The least-squares method. In regression equation there are independent variables known as predictor variable of which equation model written as X. While the dependent variable is the predicted or estimated response variable which is known as Y [38]. The predictor variable in regression can be more than one which is later known as multiple regression [40]. In certain literature, there are two models of regression: regression model for sample and population [41]. The equation forms of simple
linear regression are like formula (4) for population and formula (5) for sample. While multiple linear regression with more than one predictor variables are like formula (6) for population and formula (7) for sample [38].

\[ Y = \beta_0 + \beta_1 X_1 + \varepsilon \]  
(4)

\[ \hat{Y} = a + bX \]  
(5)

\[ Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 \ldots + \beta_n X_n + \varepsilon \]  
(6)

\[ \hat{Y} = a + b_1 X_1 + b_2 X_2 \ldots + b_n X_n \]  
(7)

Where \( Y \) is the estimated value (predictor variable), \( a/\beta_0 \) is a constant value or intercept of the regression coefficient of \( Y \) if the predictor variable is zero, \( b/\beta_1 \) is a constant value or slope of regression coefficient, and \( X / X_1 \) is a predictor variable. While \( b_2 / \beta_2 \) is a constant value or slope of the second multiple regression coefficient up to \( n \) (\( b_n / \beta_n \)), and \( X_2 \) is the predictor variable of the second multiple regressions up to \( n \) (\( X_n \)). In the use of regression algorithm model in estimating the value of an element to be compared with the actual value of the measurement results, an error value \( \varepsilon \) is involved as what stated in formula (4) and Formula (6).

Beside the linear regression, there is a nonlinear regression in which the predictor variable is a factor, fractional or exponent. Some nonlinear regression equations are logarithmic formula (8), exponential formula (9), polynomial formula (10), and power formula (11).

\[ \hat{Y} = a \times \ln(x) + b \]  
(8)

\[ \hat{Y} = a \times \text{EXP}^{bx} \]  
(9)

\[ \hat{Y} = a + b_1 x^2 + b_2 x \]  
(10)

\[ \hat{Y} = a \times x^b \]  
(11)

Where \( Y \) is the dependent variable to be estimated, \( a \) is a constant value or intercept of the regression coefficient, \( X \) is an independent or predictor variable, \( b \) is a constant value or slope of the regression coefficient and \( b_1 \) is the value of a constant or slope of the regression coefficient of order 2 polynomial regression and could be up to order 6.

To select the best algorithm model which delivers consistent estimation between the result of the applied model and the result of insitu data collection, the researchers applied coefficient determination value (R²) like formula (12)[13], and the amount of diversity or variability in \( Y \) variable is provided by a model or level of relationship between the dependent and independent variables. The range of values which was used was from 0 to 1. The algorithm model is considered good or has a very strong relationship between the dependent and independent variables if the determination coefficient closed to 1 and it is multiplied by 100% [42][43].

\[ R^2 = \frac{\left(\frac{1}{n} \sum (\hat{Y} - \bar{Y})^2 - \frac{1}{n} \sum (Y - \bar{Y})^2\right)}{\left(\frac{1}{n} \sum (Y - \bar{Y})^2\right)} \]  
(12)

Where \( R^2 \) is determination coefficient, \( n \) is total samples, \( X \) is an independent variable (predictor), and \( Y \) is a dependent variable (response). Apart of \( R^2 \), the performance of the algorithm model can also be seen from the accuracy of the data obtained from the calculation using the algorithm model (estimation) which later is compared to the insitu data (measurement results directly on the field or laboratory) in form of residue or error. The method used was Root Mean Square Error (RMSE) formula (13) and Normalized Mean Absolute Error (NMAE) index formula (14)[44],[45],[27]. RMSE was used to see the residue average of model performance, whereas NMAE was used to see the average of absolute error of model performance in percentage. In estimation algorithm model, the most important thing to consider is the RMSE or NMAE value rather than \( R^2 \) since the researchers concerned at the residue or error of the comparison between the estimation and the measurement data on the field.

\[ \text{RMSE} = \sqrt{\frac{1}{N} \sum (X_{\text{esti}} - X_{\text{meas}})^2} \]  
(13)

\[ \text{NMAE}(100\%) = \frac{1}{N} \sum \frac{|X_{\text{esti}} - X_{\text{meas}}|}{X_{\text{meas}}} \times 100 \]  
(14)

Where RMSE is Root Mean Square Error, \( N \) is total samples, \( X_{\text{esti}} \) is data value from the model result, \( X_{\text{meas}} \) is insitu data value from the measurement results on the field or in laboratory, and NMAE is Normalized Mean Absolute Error.

In some remote sensing studies, the estimation of elemental concentrations at sea surface was analyzed by regression, [46],[47],[48],[49]. In this research, the researchers also used regression analysis. After the regression analysis was done, the researchers then developed algorithm model to estimate the elements in the image by changing the pixel digital value into elements value [50],[51].
2. ALGORITHM DEVELOPMENT

2.1. Developing the Algorithm

The algorithm in this study is an expanded model of the previous algorithm which used a non-linear regression such as logarithmic [18]. In this study, the algorithm was constructed using both linear (Formula 5) and non-linear regression with various models (Formula 8, 9, 10 and 11), including the multiple regression with two independent variables (Formula 7).

The independent variable (predictor) used was Band 5 (NIR) insitu Rrs of Landsat 8 OLI and the dependent variable was the insitu sea surface sulfate. For the multiple regressions, the second dependent variable was the insitu salinity, as listed in Table 1.

Then, plotting will be done between the band 5 (NIR) insitu Rrs of Landsat 8 OLI with insitu sulfate to develop the algorithm with the insitu sulfate data by a scatter graph to see trendline of various regression models both linear and non-linear (Formula 8, 9, 10 and 11) as shown in Figure 5. Where Figure 5a is scatter graph for linear trendline, Figure 5b is scatter graph for logarithmic trendline, Figure 5c is scatter graph for power trendline, Figure 5d is scatter graph for polynomial trendline and Figure 5e is scatter graph for polynomial trendline.

### Table 1: Sulfate, Salinity, and Band 5 (NIR) Rrs of L8 Insitu Data for Training

<table>
<thead>
<tr>
<th>No</th>
<th>Insitu Sulfate (mg/L)</th>
<th>Insitu Salinity (psu)</th>
<th>Band 5 (NIR) Rrs of L8 Insitu nW/(m²·nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2089.14</td>
<td>31.18</td>
<td>0.000724871</td>
</tr>
<tr>
<td>2</td>
<td>2433.00</td>
<td>31.15</td>
<td>0.001388778</td>
</tr>
<tr>
<td>3</td>
<td>1984.50</td>
<td>30.95</td>
<td>0.000596093</td>
</tr>
<tr>
<td>4</td>
<td>2285.54</td>
<td>30.78</td>
<td>0.000852525</td>
</tr>
<tr>
<td>5</td>
<td>2167.82</td>
<td>30.82</td>
<td>0.000470973</td>
</tr>
<tr>
<td>6</td>
<td>1747.79</td>
<td>30.89</td>
<td>0.000162041</td>
</tr>
<tr>
<td>7</td>
<td>1890.14</td>
<td>30.99</td>
<td>0.000250217</td>
</tr>
<tr>
<td>8</td>
<td>1910.80</td>
<td>30.91</td>
<td>5.19759E-05</td>
</tr>
<tr>
<td>9</td>
<td>2046.43</td>
<td>31.01</td>
<td>0.000295619</td>
</tr>
<tr>
<td>10</td>
<td>2256.04</td>
<td>31.18</td>
<td>0.000118129</td>
</tr>
<tr>
<td>11</td>
<td>2360.79</td>
<td>31.00</td>
<td>0.000437175</td>
</tr>
<tr>
<td>12</td>
<td>1837.07</td>
<td>31.18</td>
<td>0.000305518</td>
</tr>
<tr>
<td>13</td>
<td>2083.00</td>
<td>31.27</td>
<td>0.000380465</td>
</tr>
<tr>
<td>14</td>
<td>2058.72</td>
<td>31.25</td>
<td>0.000936818</td>
</tr>
<tr>
<td>15</td>
<td>2366.92</td>
<td>31.30</td>
<td>0.000639645</td>
</tr>
<tr>
<td>16</td>
<td>1984.50</td>
<td>31.27</td>
<td>0.000454784</td>
</tr>
<tr>
<td>17</td>
<td>2366.92</td>
<td>31.23</td>
<td>0.000420605</td>
</tr>
<tr>
<td>18</td>
<td>2.045.18</td>
<td>31.26</td>
<td>0.001150861</td>
</tr>
<tr>
<td>19</td>
<td>1.920.85</td>
<td>31.28</td>
<td>0.000635676</td>
</tr>
</tbody>
</table>

![Figure 4a: Scatter Graph for Linear Trendline](image1)

![Figure 4b: Scatter graph for logarithmic trendline](image2)

![Figure 4c: Scatter graph for power trendline](image3)

![Figure 4d: Scatter Graph for Polynomial Trendline](image4)

![Figure 5a](image5)
While the multiple regression with two predictor variables ($X_1$, $X_2$), band 5 (NIR) insitu $R_{rs}$ of Landsat 8 OLI as $X_1$ and sea surface salinity as $X_2$, was calculated using formula (15):

$$\sum Y = a N + \beta_1 \sum X_1 + \beta_2 \sum X_2 \quad \ldots \quad \ldots$$

$$\sum X_1 Y = a \sum X_1 + \beta_1 \sum X_1 \sum X_1 + \beta_2 \sum X_1 X_2$$

$$\sum X_2 Y = a \sum X_2 + \beta_1 \sum X_1 X_2 + \beta_2 \sum X_2 \sum X_2$$

(15)

Where $Y$ is dependent variable (response), $X_1$ and $X_2$ are first and second independent variables (predictor). The results of modeling with multiple regression using formula (15) was the value of coefficient $a$ (intercept) = 1550.54, $X_1/R_{rs} = 13.40$ and $X_2/SSS$ = 239214.45 with significant value > 0.05, i.e. 0.20746954738219. While the determination coefficient ($R^2$) using formula (12) was 0.1785. From several regression equations obtained from the results of model compilation for sulfate estimation algorithm at sea surface, the researchers obtained five algorithms as in (Table 2).

### Table 2: Models of Estimation Algorithm for Sea Surface Sulfate

<table>
<thead>
<tr>
<th>No</th>
<th>Regression</th>
<th>Model</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Linear</td>
<td>$y = 240956x + 1966.3$</td>
<td>0.1784</td>
</tr>
<tr>
<td>2</td>
<td>Exponential</td>
<td>$y = 1960.8x^{115.82}$</td>
<td>0.1815</td>
</tr>
<tr>
<td>3</td>
<td>Logarithmic</td>
<td>$y = 101\ln(x) + 2881.4$</td>
<td>0.1657</td>
</tr>
<tr>
<td>4</td>
<td>Polynomial</td>
<td>$y = -3E+07x^2 + 281572x + 1956.5$</td>
<td>0.1788</td>
</tr>
<tr>
<td>5</td>
<td>Power</td>
<td>$y = 3055.5x^{0.049}$</td>
<td>0.1720</td>
</tr>
<tr>
<td>6</td>
<td>Multiple Regression</td>
<td>$1550.54 + 13.40(SSS) + 239214.45(R_{rs})$</td>
<td>0.1785</td>
</tr>
</tbody>
</table>

Where $y$ is sea surface sulfate (dependent variable) and $x$ is band 5 (NIR) $R_{rs}$ of Landsat 8 OLI (independent variable). $R_{rs}$ is reflectance remote sensing of band 5 (NIR) from Landsat 8 OLI at sea surface and SSS is sea surface salinity.

From the five algorithms, it showed that the value of $R^2$ was low. It meant that the band 5 (NIR) $R_{rs}$ of Landsat 8 OLI had a low functional relationship with seawater sulfate. Then, the researchers considered the value of RMSE and NMAE of the five algorithms when they were validated and tested with other data, and the selection of this estimation algorithm depended on the RMSE and NMAE values.

### 2.1. Model Validation and Testing

The six models were then validated and tested using the $R_{rs}$ of Landsat 8 OLI data which were taken on different dates to see the performance of the model as the estimation algorithm of sulfates at sea surface (Table 3). Landsat 8 OLI image was downloaded on https://earthexplorer.usgs.gov/ on November 3, 2015. In the same date, the researchers took in situ sulfate data as the comparator to validate the data obtained from the estimation of the algorithm model. Next, the 10 data in Table 3 were then divided into two; five data for validation and five data for testing.

The results of validation and testing of the data using formula (13) and formula (14) as in Table 4. There, the data showed that the power regression model had better performance than other models. The evidence were the smaller NMAE and RMSE values compared to other models, 9.36% and 299.66 respectively for validation; 9.53% and 320.84 for the test. Thus, by considering the related results of estimation, the algorithm model selected for this current research was the power regression with coefficient value $a$ (intercept) = 3055.5 and coefficient value $b$ (slope) = 0.049.

### Table 3: Insitu Sulfate, Insitu Salinity, and Band 5 (NIR) $R_{rs}$ of L8 OLI Image for Testing

<table>
<thead>
<tr>
<th>No</th>
<th>Insitu Sulfate (mg/l)</th>
<th>Insitu Salinity (psu)</th>
<th>Band 5 (NIR) $R_{rs}$ of L8 Citra (NW/m² nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2669.64</td>
<td>31.08</td>
<td>0.012605071</td>
</tr>
<tr>
<td>2</td>
<td>2451.21</td>
<td>31.06</td>
<td>0.013528170</td>
</tr>
<tr>
<td>3</td>
<td>2797.05</td>
<td>31.09</td>
<td>0.01241486</td>
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<td>4</td>
<td>2797.05</td>
<td>31.10</td>
<td>0.012191269</td>
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<td>5</td>
<td>2800.20</td>
<td>31.11</td>
<td>0.012286762</td>
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<td>6</td>
<td>2900.20</td>
<td>31.12</td>
<td>0.012509579</td>
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<td>7</td>
<td>2960.87</td>
<td>31.13</td>
<td>0.012891551</td>
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<td>31.08</td>
<td>0.013369015</td>
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<tr>
<td>9</td>
<td>2797.05</td>
<td>31.12</td>
<td>0.013639015</td>
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</table>
Table 4: NMAE and RMSE values of Each Regression Model

<table>
<thead>
<tr>
<th>No</th>
<th>Regression</th>
<th>Validation</th>
<th>Testing</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>NMAE (%)</td>
<td>RMSE (sr⁻¹)</td>
<td>NMAE (%)</td>
</tr>
<tr>
<td>1</td>
<td>Linear</td>
<td>85.55</td>
<td>2328.86</td>
</tr>
<tr>
<td>2</td>
<td>Exponential</td>
<td>217.79</td>
<td>5932.02</td>
</tr>
<tr>
<td>3</td>
<td>Logarithmic</td>
<td>10.34</td>
<td>323.11</td>
</tr>
<tr>
<td>4</td>
<td>Polynomial</td>
<td>76.61</td>
<td>2092.41</td>
</tr>
<tr>
<td>5</td>
<td>Power</td>
<td>9.36</td>
<td>299.66</td>
</tr>
<tr>
<td>6</td>
<td>Multiple Regression</td>
<td>85.91</td>
<td>2304.8</td>
</tr>
</tbody>
</table>

3. ALGORITHM IMPLEMENTATION

The developed algorithm was then implemented into the data of Landsat 8 OLI as distribution media of sulfate mapping at sea surface. Algorithm application and image processing were done by using Beam Visat software started from the change of the digital number on the image pixel into Rrs sea surface.

The first thing to do was inserting the Band 5 (NIR) Landsat 8 OLI image into the Beam Visat editor. Next, the image was processed by changing a DN of image pixel into surface reflectance values by dividing DN by 10000 and phi constant value that was put into Band Maths Expression Editor on Beam Visat software as shown in Figure 5. The result of this process was an image with a pixel value of sea surface Rrs on Band 5 (NIR) of Landsat 8 OLI (Figure 6).

The second was inserting the estimation algorithm (the formula in Table 2, number 5) into Band Maths Expression Editor on Beam Visat software (Figure 7). The result showed that each image pixel was converted into sulfate value.

When the algorithm was implemented, the model converted all pixels into sulfate values for both land and water object. So, in this case, the researchers separated the mainland pixel and the water pixel using formula (16) that was shown in Figure 8. Since the researchers only separated sulfate values, the word "unsur" was changed into sulfate (Figure 9). Therefore, the result was the image of sulfate distribution at sea surface in Madura strait (Figure 10).

\begin{equation}
NDWI > 0? unsur : 0
\end{equation}

\begin{equation}
NDWI = \frac{Rrs Band 3 - Rrs Band 5}{Rrs Band 3 + Rrs Band 5}
\end{equation}

Where NDWI (Normalized Difference Water Index) was the algorithm to separate water and land pixels on the image by creating a water value index. The result was the NDWI values and classified into
2: when it was greater than 0, it was defined as water zone. In contrast, if the NDWI was smaller or equal to 0, then the zone was defined as mainland. RRS value used to calculate NDWI was Reflectance Remote Sensing of band 3 and 5 of Landsat 8 OLI imagery.

Highest sulfate concentration zone was near the beach with high public activities like Kamal harbor, Bangkalan regency. In addition, the general overview of the statistic, minimum pixel value was 0 and the maximum value was 8248.489 (Figure 12).

The data of sulfate concentration obtained from the estimation algorithm which was compared to insitu sulfate by utilizing Landsat 8 OLI image data showed NMAE 9.53% and RMSE 320.84 of which showed little error and low residue level. Table 5 and Figure 13 showed differences of the sulfate concentration values obtained from the estimation algorithm and the insitu data that were extracted from the pixel of Landsat 8 OLI image. Both of them referred to the same coordinate point of which the image data and seawater samples were taken.
4. DISCUSSION

Development of a model, as an estimation algorithm sulfate in sea surface, is intended to improve the performance of model itself. The indicators used in addition to the reliability and usefulness of the model to estimate are the accuracy of data which result of model application compared with the field data. Among several methods that can be used to evaluate the accuracy of model applications are NMAE and RMSE. Both models, previous research results [18] and current research, will be applied to the same data ie Rrs values in band 5 (NIR) of Landsat 8 OLI image. Another similarity is the region and time of field data retrieval (Table 3).

In the previous model [18], each variable data value (X and Y) convert to log value. Then enter into a model which is a logarithmic regression equation and the result is still a log value. To convert into sulfate value, the result value of the model is made a power of 10 since the log used is base-10. By using the Formula (13) and Formula (14) obtained values of NMAE and RMSE as in Table 6.

Table 6 shows the value of NMAE and RMSE on the previous model is very high, respectively 75.8% and 8688 sr^-1. While for the current research the values of NMAE and RMSE only 9.5% and 343 sr^-1. This occurs because previous models [18] were built using less data than the current research. Wherein the use of data mining to get patterns more accurately using a lot of data since of variations in value will determine the type of pattern and the information will be obtained.

This research was done in the regional waters of the Madura strait-Indonesia with a tropical climate and then the data is collect in the dry season. With the region's characteristics the influence of the atmosphere and the latitude position on the equator line will affect the satellite recording of the reflectance spectra (Rrs) of the sea surface and the sulfate concentration in sea water. So that territorial use of this algorithm can be evaluated to produce a more optimal estimation value when will be used in other regions with very different characteristics.

The use of Rrs from Band 5 (NIR) of Landsat 8 OLI imagery is based on previous research [52] showed that among the band 1 (CA), band 2 (blue), the band 3 (green), band 4 (red), and band 5 (NIR), as measured by tool Spectroradiometer TriOS Ramses, which is sensitive (spectral signature) to sulfate in sea surface is a band 5 (NIR). Then there are other studies also using band 5 (NIR) for modeling near-infrared reflectance spectra of clay and sulfate mixtures and implications for Mars [53].

5. CONCLUSIONS

The authors have evaluated the performances of the previous research model as estimation algorithm to estimate a sulfate concentration at the sea surface. By using NMAE and RMSE values have been obtained that the model of current research is smaller than previous research,
respectively 9.5% and 320.8 sr\(^{-1}\). While previous research has NMAE and RMSE values respectively 75.8% and 8688 sr\(^{-1}\).

The developed estimation algorithm of the sea surface sulfate concentration using both linear and non-linear regression model obtained non-linear model: a power regression with higher degree of precision and smaller value of average error and residue. The algorithm can be applied to estimate sulfate concentration at sea surface with the value obtained for coefficient \(a\) (intercept) 3055.5 and coefficient \(b\) (slope) 0.049 and one predictor variable (X) that was band 5 (NIR) Rrs of Landsat 8 OLI. In addition, the correlation functionality between sulfate and band 5 (NIR) Rrs of Landsat 8 OLI imagery was low with R\(^2\) value only 0.1720 or 1.72% Rrs as the estimation factor of sulfate concentration at sea surface.

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