

# ANALYZE AND EVALUATE THE IMPLEMENTATION OF CDS ALGORITHMS USING THE MOBILE AGENT.

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## ABSTRACT

In this work, we identify, analysis and evaluate the role of mobile agent to solve the problem of selecting the minimum connected dominating set CDS better alternative approach than the exchange messages approach. The first problem concerns the nature of the CDS construction algorithms in question. Their design is justified as the purpose to construct a virtual infrastructure for wireless network with varied high cost in the permanent exchanged messages to select the CDS. The redundant broadcasting of the packets effects the overall network performance, increases the latency, the collision and the need of synchronization mechanism.

Common techniques and algorithms such as marking process, Greedy Algorithms, Maximal Independent Set MIS, Pruning process, and Multipoint Relaying are exploited to select the potential nodes of the connected dominating set. We analyzed and implemented some of these techniques from the using perspective of the mobile agent.

We shall argue that the mobile agent implements the CDS algorithms with less cost in its moves comparing with the cost of exchanged messages. Mobile agent just requires local information and a limited number of iterative rounds instead of the redundant broadcasting packets that imposed by other techniques. There is no work similar to our work that discusses the using of mobile agent to construct the connected dominating set based on those common techniques.

We have made slight modifications on those algorithms, their notations and parameters to be appropriate through the implementation by the mobile agent. Using the mobile agent shows encouraging results for constructing connected dominating set with few iterations, eliminates the overhead caused by the large volume of message exchange, and improve the structure of the computed CDS. However, the agent by implementing those algorithms successfully constructs the connected dominating set; the constructed connected dominating nodes are still large set. The agent by implementing those algorithms could not construct the minimum CDS.

**Keywords-** *Mobile Agent, Graphic Theory, Connected Dominating set, Maximal Independent Set, Whiteboard.*

## 1. INTRODUCTION

A virtual backbone is a set of selected nodes employed for routing process [2]. The concept of virtual backbone was first introduced in the literature [1], as the routing infrastructure of ad hoc networks. Exploiting this concept ensures the reducing of the exchanged messages, routing-related control messages and the amount of wireless signal collision and interference from the whole network to the set of backbone nodes. A wireless network lacks a physical infrastructure that manages the nodes and coordinates the exchanged messages among them. Exploiting the virtual backbone overcomes this lack. Thus, any non-

backbone node has to be adjacent to at least one backbone node. Only the nodes in the virtual backbone will be involved in message routing, as a result, the routing protocol will work much faster and efficiently [3]. A virtual backbone plays a significant role in saving energy of limited-energy wireless nodes [4]. More importantly, less involved nodes in message routing, less need to maintain routing information in those nodes. A network can react quickly to changes in the topology [2].

In order to achieve scalability and efficiency, several algorithms have emerged that rely on a virtual network infrastructure. A well-known approach for

constructing this virtual backbone in wireless networks is the Connected Dominating Sets (CDSs) [5]. A subset nodes of a graph  $G$  is a dominating set if every node of the graph either belongs to the subset or adjacent to at least one node in the subset. A dominating set is connected, called CDS, if there exists a path only consists of the nodes in the set [6].

The connected dominating set represents as virtual backbone [9] which is a set  $D$  of vertices has two properties; any node in  $D$  can reach any other node in  $D$  by a path that stays entirely within  $D$ . That is,  $D$  induces a connected sub-graph of  $G$ . Every node in  $G$  either belongs to  $D$  or is adjacent to a node in  $D$ . Thus, any non-dominated connected node wants to communicate will send a packet to one of (one hop away from) the nearest dominated node belongs to the (CDS) connected dominated set which in turn forwards the packet to its destination in efficient way through only the nearest interconnected dominated nodes and takes less number of packet communications and moves. This efficient technique used specially for the wireless ad hoc network, which has no physical backbone infrastructure. Since the networking nodes in wireless ad hoc networks are very limited in resources, a virtual backbone should be low in its number of belonging nodes and be constructed with low communication and computation costs.

A minimum connected dominating defined [10] as set of a graph  $G$  is a connected dominating set with the smallest possible cardinality among all connected dominating sets of  $G$ .

Constructing a CDS based on several techniques and algorithms have raised in literature. The MIS based algorithms usually have good performance bound and time/message complexities. They only need one-hop neighborhood information, but they relies on the single leader or Multiple leader based algorithms. Pruning based algorithms has high message complexity due to the global connectivity checking. The multipoint relaying based heuristic is pure localized. This algorithm selects CDS from a multipoint relay set, but no complexity analysis for this algorithm in literature [7].

Mobile agent is a piece of code with special features such as the ability to sequentially move, clone and run in remote sites in a computer network. It can make decision, search of specific information and gather the results, cooperate, directly communicate through exchanging messages and indirectly through using the whiteboard with other mobile agents and return to its home site after completing the assigned tasks on behalf of its user.

The mobile agent just require the minimum information, as the number of nodes, to explore the network, it does not need to know the whole topology information. The Agent is so convenient for the dynamic environment such wireless networks. Mobile Agent offers the distributed possibility, further the algorithms that based on mobile agent usually have characterized with ease. Ideally, mobile agent just requires local information and a limited number of iterative rounds instead of the redundant broadcasting packets that is imposed by other techniques.

As an initial step and before starting any algorithm to construct CDS, most algorithms depend on exchange routing information among neighbor nodes. The exchange of the required information is based on limited number of hops to ensure the interconnection and the control. The total number of messages is too much and frequently send. That is what can be overcome by using mobile agent. We studied the constructing of CDS algorithms and implemented them using the mobile agent which provides a significant level of flexibility, simplicity. It can be implemented in a number of diverse domains comparing with CDS traditional algorithms. For this, when designing a CDS algorithm we take into account besides the stability, the performance bounds, degree of localization, time and message complexities.

In this paper, we focus on various CDS algorithms that have proposed in the literature for constructing CDS as a virtual backbone. As demonstrated that during the implementation of these algorithms, the nodes exchange their open neighborhood information with their one-hop neighbors which produce varied high cost in the permanent exchanged messages to select the CDS. The redundant broadcasting of the packets effects the overall network performance, increases the latency, the collision and the energy consumption. The data transmission consumes much energy than data processing. Sending a single bit can consume the same energy as executing 1000 instructions at typical sensor node [30]. Therefore, it will be more energy efficient if the nodes keep its data in its memory and waits for a mobile agent to process and carry the special data.

The primary purpose of this study is to present the important role of using the mobile agent to select the CDS set, eliminate the high cost that has imposed by the permanent exchanged messages among all the nodes and minimize energy consumption.

The selected dominating nodes can be used as an optimal itinerary for the mobile agent to reach every node that does not belong to the connected dominating set in order to implement another tasks overall network.

Moreover, after the study and evaluate the CDS algorithms, we implement those evaluated algorithms using the mobile agent. Then, we present how the mobile agent success to construct the connected dominating set, through implementing our evaluated CDS algorithms taking into account minimizing the total number of movements.

Finally, we mentioned that the mobile agent could not select the minimum and optimal CDS even with more constrains and modifications in the implementation procedures of those CDS algorithms.

The rest of the paper organized as follow. In section 2, we discusses the classification of CDS algorithms and elaborates the various algorithms proposed in the literature pertaining to construction of CDS. Section 3 illustrates the used CDS algorithms by the mobile agent and the analytical results. Section 4 concludes the paper.

## 2. CDS CONSTRUCTION TECHNIQUES

The construction algorithms of the connected dominating set vary on the adopted techniques on which the CDS algorithms have based. Jeremy Blum in [7], P. S. Vinayagam in [8] and Jiguo Yu in [9] surveyed the exploiting distributed CDS construction techniques such as: Marking, greedy, MIS based, Steiner tree based, pruning based, and Multipoint Relaying. Those techniques are classified to Centralized and Decentralized algorithms. Algorithms belong to centralized category assume the prior knowledge of network global information. As well as the availability of the complete network topology information, which is usually not practical in the case of mobile wireless networks. While in the Decentralized algorithms, local network information is essential. These algorithms can be further categorized to Distributed and Localized algorithms, [8, 9, 27] for more details.

In this section, we give brief review of some those techniques and their works in order to identify the main differences among them and the most appropriate to be implemented by the mobile agent.

### 2.1. Based on the Greedy Algorithm

The first technique called the Marking process, which uses different colors to classify the vertices in the graph. The dominating vertex is colored black,

with its neighbor vertices colored gray and other vertices with white color. Two greedy heuristic algorithms for constructing CDS proposed in [10], which guarantees the bounded performance. The first algorithm initially starts by marking all vertices white. Then selects the node with the maximum number of white neighbors, marks it black and marks its white neighbors gray. The algorithm examines the gray nodes simultaneously with their white neighbors. The selected gray node with its white neighbor must have the maximum number of white neighbors. The selected pair of nodes are marked black, with their white neighbors marked gray. The algorithm terminates when all the vertices of the graph are marked gray or black.

The second algorithm starts by marking all vertices white. At the first iteration, it selects a node that reduces the maximum number of a connected black component (the black component is one or more black nodes connect to their gray neighbors). Selected node is marked black and its white neighbors are marked gray. The algorithm does not guarantee the connectedness of the black components. Therefore, in order to connect the black nodes by two or more intermediate gray nodes belong to the two components and change their color to black.

### 2.2. Based on Maximal Independent Set MIS

A subset nodes of  $V$  is an *independent set* if for any pair of vertices in  $V$ , there is no edge (connection) between them. A *maximal independent set (MIS)* is the independent set in which adding any extra vertex will cause connection between any pair of nodes in the set. Any maximal independent set is also a dominating set. The technique for constructing the CDS based on MIS can be simultaneously compute and connect the MIS [11] or connect the selected nodes after the construction is over [12, 13, 14], these selected MIS nodes form the skeleton of the CDS, in order to connect the nodes in the MIS, additional nodes are added, thus the CDS is formed. To compute an MIS the algorithm relies on either single leader or multiple leaders, with additional complexity cost. The node has the maximum degree or id among all neighbors can serve as leader.

Cheng *et al.* propose in [11, 15] their algorithm in which a new status for white vertices is introduced, the active status. The active status of white vertex is designated to a white vertex which has at least one adjacent dominate node (gray). At the beginning, all the nodes are non-active white. The leader node starts the algorithm by marking itself black and becomes a dominator. Adjacent

white nodes to the leader node changed to be a dominatee (gray). A non-active white node changes to status *active* if one of its neighbors becomes a dominate (gray). Its color still keeps white. Then, an active node with the smallest cost among all its active neighbors (the local cost is the id or sometimes a random value with the id) will compete to be a dominator; it then invites its gray parent node to be its dominator. Its minimum cost gray parent also changes to serve as its dominator (black), ensuring the connectivity of the dominating tree. Finally, all black leaf nodes can change back to be dominatees (gray). This process terminates when all nodes are colored gray or black, and all the black nodes form a connected dominating set. This algorithm has the time complexity of  $O(n)$ , and the message complexity of  $O(n \log n)$ , which is dominated by leader election [7]. As a result, a dominating tree is grown from the leader.

Alzoubi *et al.* [16] propose an algorithm to construct the dominating set. They employ the distributed leader election algorithm [17] to construct a rooted spanning tree. With different types of messages used to classify the nodes of the constructed spanning tree, the nodes become either black (dominator) or gray (dominatee), based on their ranks. The rank of a node is the number of hops to the root of the spanning tree with its ID. The labelling process begins from the root node and finishes at the leaves. The node with the lowest rank marks itself black and broadcasts a DOMINATOR message. The marking process then continues according to the following rules:

- If the node firstly receives a DOMINATOR message, it marks itself gray and broadcasts a DOMINATEE message.
- If a node received DOMINATEE messages from all its lower rank neighbors, it marks itself black and sends a dominator message.

Finally, the root node connects the selected nodes of the MIS to form a CDS. It broadcasts an INVITE message. Then, the INVITE message rebroadcasts by dominatee (gray) nodes to all two-hop neighbors out of the current CDS. When a black node receives the INVITE message for the first time, it joins the dominating tree together with the gray node, which broadcasts the message and so on. The process terminates when all the black nodes join the CDS. This algorithm has time complexity of  $O(n)$ , and message complexity of  $O(n \log(n))$ .

### 2.3. Based on Pruning CDS Construction

Wu *et al.*'s work [18, 19] proposes a completely localized algorithm to construct CDS. All the vertices exchange their open neighborhood information with their one-hop neighbors. Thus, each node knows all of its two-hop neighbors. Each node has two unconnected neighbors marks itself as a dominator. The set of marked vertices form a connected dominating set,  $S$ , the result is big number of dominator nodes. To avoid the redundant of those nodes, two rules have proposed as follow:

**Rule1:** a node  $u$  deleted from  $S$ , the CDS, if there exists a node  $v$  with higher ID such that the closed neighbor set of  $u$  is a subset of the closed neighbor set of  $v$ , (The closed neighbor set of node  $u$  is one-hop neighbors adjacent to  $u$  with the node  $u$  itself).

**Rule2:** node  $u$  deleted from  $S$  when two of its connected neighbors in  $S$  with higher IDs can cover all of  $u$ 's neighbors.

Another good pruning-based rule has proposed by Butenko's algorithm in [14, 15]. The connected dominating set  $S$  is initialized to all white nodes of the graph  $G$ , and then each node will be examined to determine whether it should be still belonging to the CDS or not. If removing node  $u$  from  $S$  causes disconnecting to the induced graph of  $S$ , then node  $u$  *must be part of the CDS* and color it black. Otherwise, remove  $u$  from  $S$ . At the same time, if  $u$  does not have a black neighbor in  $S$ , color its neighbor that have maximum degree in  $S$  black. This procedure repeated until no white node left in  $S$ . This algorithm has time complexity  $O(|V| \cup |E|)$ .

### 2.4. Based on Multipoint Relaying CDS Construction.

The multipoint relay (MPR) is a neighbor-designated method that shows both efficiency and simplicity. Neighbor knowledge methods can be classified as neighbor-designated methods and self-pruning methods. In neighbor-designated methods, a node that transmits a packet specifies which one of its one-hop neighbors should forward the packet, while in self-pruning methods, a node receiving a packet will decide whether or not to transmit the packet by itself. Compared to other neighbor knowledge broadcasting protocols, MPR uses a simple algorithm to calculate the forwarding nodes, which makes it easy to implement. The redundant broadcasting of the packets effects the overall network performance, increases the latency, the collision and the need of synchronization mechanism.

For computing a connected dominating set based on multipoint relays, the only knowledge assumed for a given node is two-hop neighborhood. The idea behind this technique is to compute some kind of local dominating sets. Each node computes a multipoint relay set with the following properties: In particular, each node  $u$  in the network selects a subset of its 1-hop neighbor nodes called multipoint relays (MPRs), based on the information of its 2-hop neighbors, those forwarding node retransmit broadcast packets. Other nodes that are not in the MPR set can read but not retransmit broadcast packets. The MPR set guarantees that all two-hop neighbor nodes of each node receive a copy of the broadcast packets and, therefore, all nodes in the network can be covered without retransmissions by every single node. The algorithm does not need any distributed knowledge of the global network topology. For these reasons, MPR has successfully employed to construct CDS by many other algorithms in wireless ad hoc. Several good heuristic algorithms such as [23, 24, 25] have been proposed to compute a small size CDS in the network based on multipoint relay.

The original MPR selection heuristic for computing an MPR set follows a greedy algorithm [26]. The set of all one-hop neighbors of  $u$  is denoted by  $N(u)$ , and the set of all two hop neighbors of  $u$  as  $N_2(u)$ . The number of two-hop neighbors of  $u$ , that can be only covered by  $v$  where  $v$  is an one-hop neighbor of  $u$  is  $D(v)$ . Let the selected MPR set of node  $u$  be  $MPR(u)$ . The heuristic of the  $MPR(u)$  calculation operates as follows:

- Start with an empty MPR set  $MPR(u)$ .
- Calculate  $D(v)$  for each node in  $N(u)$ .
- Add to  $MPR(u)$  those nodes in  $N(u)$ , which only cover some nodes in  $N_2(u)$ .
- Remove nodes from  $N_2(u)$  which are now covered by nodes in  $MPR(u)$ .
- Add to  $MPR(u)$  those nodes in  $N(u)$  which covers maximum number of remaining two-hop neighbors of  $u$ .
- In case of multiple choices, select the node as MPR whose  $D(v)$  is larger.
- To optimize the  $MPR(u)$ , remove the node in  $MPR(u)$  if all its covered two-hop neighbor nodes can also be covered by the remaining nodes in  $MPR(u)$ .

In order to recognize neighbor nodes and calculate  $D(v)$  for each one-hop neighbor, a HELLO message has to be exchanged between one-hop neighbors periodically. A HELLO message from a node may contain information such as its node ID, MPRs it has

selected, and all related information about its one-hop neighbors. These HELLO messages are exchanged in a fixed time period so that necessary information for the MPR calculation can be obtained and the status of the network can also be updated [24].

Mans and Shrestha proposed a new concept in [20, 21] called in-degree which was presented in this heuristic as a new criterion for MPR selection. The value of the in-degree of a node  $v$  is the number of shared neighbors between node  $v$  and node  $u$ , where  $u$  is a one-hop neighbor of source node  $S$  and  $v$  is a two-hop neighbor of  $S$ . They observed that the in-degree of each two-hop node of source  $S$  is a smaller value compared to the out-degree of each one-hop node of  $S$ . Consequently spent less time to calculate the MPR for each two-hop neighbor. Nevertheless, this increases the size of the MPR set.

J. Wu proposed an extended heuristic of the original MPR in [25], namely, enhanced MPR (EMPR). New notion called free neighbor of the node is proposed, node  $u$  is a *free neighbor* of  $v$  if  $v$  is not the smallest ID neighbor of  $u$ , it exists at least one neighbor node of  $u$  has smallest ID than the ID of  $v$ . The heuristic of the EMPR extends the MPR-CDS in two phases shown as follows:

Enhanced Rule 1: The node has the smallest ID among all its one-hop neighbors and it has two unconnected neighbors.

Enhanced Original MPR Heuristic: Initially, add all free neighbors of source node  $S$  to the MPR set and eliminate two-hop nodes that have covered by these free neighbors. Then apply the original MPR heuristic to the residual one-hop neighbors to cover all remaining two hop nodes. Use the node ID to break a tie when two nodes cover the same number of uncovered two-hop nodes.

Xiao Chen and Jian Shen in their article [22] observed that the node degree is more related to the size of CDS. Here, we only present the improved scheme based on the EMPR in [20], which we refer to as degree-based enhanced MPR (DEMPR). The heuristic of DEMPR is the same with the EMPR except it applies two extended rules:

Extended Rule 1: A node is in the CDS if it has the largest node degree among all its one-hop neighbors and it has two unconnected neighbors.

Extended Rule 2: A node is in the CDS if it has selected as an MPR and its selector has the largest node degree among its one-hop neighbors. Based on these two rules, the notion of free neighbors also needs to change correspondingly. The one-hop free

neighbors of source node  $S$  are its one-hop neighbors who have at least a one-hop neighbor that has larger node degree than  $S$ .

### 3. USED TECHNIQUES AND OUR CONTRIBUTION

In this work, we studied, analyzed the CDS construction algorithms based on the traditional marking process, the MIS algorithms and multipoint relay set MPR in order to select the most efficient and appropriate implementation by the mobile agent to get the near-optimal solution. We discussed and made a comparison on the total number of moves which performed by the agent and the final number of the selected connected dominating set when the agent complete constructing the CDS.

We implemented our approaches to construct the CDS in java through the VISIDIA simulation platform [29]. The machine has Intel CORE i5 2520M at 2,50 GHz and 4 GB of RAM. The agent succeeded to construct the CDS in all cases with different instances. The VISIDIA platform provides an environment to design any graph and simulate the CDS algorithms on that graph. The platform equips each node in the graph with an ID, memory called whiteboard and those nodes communicate to each other through links with specific ports numbers. The platform provides the ability to implement the algorithm by one mobile agent or multi-agents and shows the statistics such as the moves total number and execution time that made by agent. The platform provides for each node in the graph  $G$  an associated set of nodal properties locally memorized in its whiteboard, those properties can be used as a variables in the status of the mobile agent.

We assumed that, the mobile agent does not know the degree of each node  $u$ . It visits the node  $u$ , explores all its adjacent neighbor nodes  $N(u)$  and then it registers the degree  $D(u)$  in the whiteboard of that node.

We observed that in the traditional marking process, at each iteration the agent must enter the selected dominating node, which has the largest number of adjacent white nodes, explores all of its adjacent white nodes, marks them gray and then explores all adjacent white nodes of those gray nodes. It select one of those gray nodes that has the largest adjacent white nodes to be the next connected

dominating node and so on. The agent in this way performs large number of moves due to directly entering the selected dominating node again in the next iteration, it moves again to all adjacent white nodes, marks them gray and finally it explores their adjacent nodes to count the number of white nodes. Since some of the white nodes become gray, the agent must make additional moves to count the adjacent white nodes of those gray nodes at each iteration. The resultant CDS based on the traditional marking algorithm guarantees the connecting of the selected dominating nodes, since the selected dominating nodes are restricted by gray nodes. The constructed CDS is not always minimum.

In contrast, constructing the CDS based on MIS is complicated to implement by the mobile agent. The algorithm produces inappropriate additional dominating nodes and accomplishes in two phases. In the first phase, the agent performs additional moves to ensure the independence of each selected independent node. And additional moves in the second phase to ensure the connecting of all the selected dominating nodes. For selecting the MIS, the agent starts at arbitrary node  $u$ . The agent explores every neighbor node  $v \in N(u)$  of  $u$ . At each visiting, it also explores the adjacent nodes of  $v$  in order to make sure there is no direct connection among these independent. By this approach, the agent may select large number of independent nodes. As well as, the agent must connect those selected independent nodes to construct the CDS, it selects additional nodes from the remained nodes, and the constructed connected dominating set is far from being minimum. The resultant CDS based on MIS imposes on the agent to perform too much moves to construct minimum CDS. We can decrease those additional moves by selecting the MIS nodes simultaneously with the construction of the CDS at the same phase.

Now, how the mobile agent implements CDS algorithms based on MIS and multipoint relay algorithms. Moreover, what are the optimal strategies and techniques used to minimize the overall cost in order to select the minimum connected dominating set? We implement those algorithms with some modifications and improvements to suit with the agent's behavior through the exploration procedure. In this work, we try to answer those questions and explain the positive and negative implementation aspects.

### 3.1. Network Model and Connected Dominating Set (CDS)

We present a mathematical model for the network under consideration that introduces useful terminologies and definitions from graph theory. Each node  $u$  in the graph  $G$  has an associated set of nodal properties locally memorized in its whiteboard. We assumed those nodes are fixed and accessible by the mobile agent, the agent does not need prior information except the total number of the nodes in the graph. The agent has the ability of computing the degree of each node. The degree of the node represents the cost of implementation in those algorithms. Typical properties includes the following:

We define the following variables that used by the agent during the exploration:

- $N1(u)$  is the set of one-hop adjacent nodes to the node  $u$  :  $N1(u) = \{v \in V / \exists (u, v) \in E1\}$
- $N[u]$  is the set of one-hop adjacent nodes to the node  $u$  plus the  $u$  itself :  $N[u] = \{v \in V / \exists (u, v) \in E1\} \cup \{u\}$
- $N2(u)$  is the set of two-hop nodes to the node  $u$  :  $N2(u) = \{x \in V / \exists! (u, x) \in E; \exists v \in N1(u) / (v, x) \in E2\}$ .
- $MPR(u)$  is the multipoint relays set of  $u$  which is selected by the agent.
- The node  $u$  has two type of degree: normal degree  $d(u)$  and exclusive degree  $D_{exc}(u)$ , for each node  $v \in MPR(u)$  the  $D_{exc}(v)$  represents the number of one-hop nodes  $x \in N1(v)$  and  $x! \in N1(u)$ , those nodes are two-hop nodes of  $u$  exclusively reached by the node  $v$ . The node  $u$  is considered as a selector node for each node  $v \in N1(u)$ . A node  $v$  has a normal degree value means that the agent visits this node and all its one-hop neighbor nodes. A node  $v$  has one or more an exclusive degree means that node has been selected as MPR by one or more selector nodes.
- Explored node is a node  $u$  that the agent visited all its one-hop neighbor nodes  $N1(u)$ .

**These variables are available in each node to be used by the mobile agent.**

### 3.2. MA-CDS based on Minimum Independent Set

In this section, the agent constructs the connected dominating nodes based on the selected minimum independent set. The construction of CDS possible simultaneously implemented in the same

phase with the selecting of MIS or in separate two phases. In the first phase, the agent selects the minimum independent set for the whole graph and then in the second phase, it connects those selected independent nodes to constructs the connected dominating set.

With slight modification, we implement the first algorithm proposed by Cheng's [11, 15], in which new status is introduced, the active node concept. In our implementation, the concept of active node is slightly changed. Non-active white node becomes active when the agent visited all its adjacent one-hop nodes, it becomes explored node, and at least one of its neighbor nodes is dominate (gray). The node degree represents the local cost that serves as the selection criterion (parameter). We assumed that the node degree is more effective to select the optimal dominating nodes. The first node in which the agent starts implement the algorithm is arbitrary selected, but we believed that the degree of this node has a critical effect too. Therefore, we presents two scenarios as below.

In the first iteration, two scenarios are available, the first one achieved by directly mark the first node  $u$  as a dominator (Black), then the agent moves to each one-hop adjacent neighbor nodes  $v \in N1(u)$ , it marks them as dominate (Gray). At each visited gray node  $v$ , the agent moves to each one-hop adjacent nodes  $x \in N1(v)$ , marks them as non-active white  $D_{NA}(k)$ , no one of these nodes are known their degree, therefore no change in their status. Thus, the agent knows the degree of the first dominator node  $u$  and the degree of each one-hop adjacent gray nodes  $v \in N1(u)$ . Actually, this scenario does not guarantee the optimal selection of the first dominator nodes. In our implementation, the agent simultaneously constructs the CDS with the selecting of the independent set.

The agent in each node  $u$  performs the following steps:

- The agent starts the iteration at a node  $u$ ;
- Visit and explore each one-hop nodes  $v \in N1(u)$  of  $u$ , marks them as non-active white;
- Visit each one-hop nodes  $x \in N1(v)$  of  $v$ , marks them as non-active white;
- Calculate the normal degree  $D(u)$ ,  $D_{NA}(u)$  of  $u$  and the normal degree  $D(v)$ ,  $D_{NA}(v)$  for each node  $v \in N1(u)$ ;
- Add the node  $k \in N1[u]$  which has the maximum degree to the Independent Set IS, and to the Connected Dominating Set CDS;

- Announce the one-hop neighbor nodes  $N1(k)$  information to each  $x \in N1(k)$ ;
- Marks the node  $k$  as dominator (Black), and each node  $x \in N1(k)$  as dominate (gray);
- If there is an explored non-active node  $x$  which is adjacent to at least one dominate (gray) node  $y$  then:
  - Change the status of the non-active node  $x$  to Active;
  - Add the node  $x$  to the Independent Set IS, and to the Connected Dominating Set CDS;
  - To guarantee connection of the dominating nodes, add the maximum degree dominate (gray) node, adjacent to the node  $x$ , to the Connected Dominating Set CDS;
  - Marks each non-active node that is adjacent to the selected dominator node as dominate (gray).
- Select the dominate node (gray) that has the largest degree and largest  $D_{NA}(x)$  for starting the next iteration. The agent could not directly add this gray node to the independent set because this gray node connected to an independent node.

The second scenario achieved as follow: the agent starts at the first node  $u$ ; it intends to select the node with largest degree to become the first dominator node (black). Therefore, the agent keeps moving to each one-hop neighbor nodes  $v \in N1(u)$  adjacent to the first node  $u$ . To get the degree of those  $v$  nodes, it moves to their one-hop neighbor nodes  $x \in N1(v)$  too. Since the agent does not select any dominator or dominate node yet, it could not changes the status of any visited node to active white. Once the agent knows the degree of the first node  $u$  and the degree of each one-hop neighbor nodes of  $u$ , it moves to the node that has the largest degree. It marks this node as dominator (Black), and then it moves to each one-hop neighbor nodes adjacent to this dominator node in order to marks them as dominate (Gray), as well as, it moves to the one-hop neighbor nodes adjacent to each dominate (Gray) node to mark them as non-active white. Consequently, the agent knows the degree of all dominate nodes (gray).

In case the agent does not select the first node  $u$  as a dominator and selects anyone of one-hop nodes of  $u$  to become the dominator, node  $u$  will be marked as dominate (gray). Thus, the agent changes the status of each one-hop neighbor nodes adjacent to  $u$

to become active white since it explores them; it knew their degree and they are not gray.

This scenario induces more movements when the agent visited some two-hop nodes to the first node  $u$  without mark them and moves to them again to mark them as active or gray. Therefore, as previously mentioned that the selecting of the node in which the agent must starts the algorithm has potential impact on the total number of the agent's movements.

For the next iteration and following anyone of these two scenarios, the agent must know the degree of the active white nodes in order to select the appropriate nodes since these selected nodes become part of the independent set. The agent moves to the dominate node (gray) that has the largest degree, let's say node  $v$ , it then moves to and explores each node  $k \in N1(v)$  to get some information such as the node's degree  $D(k)$ , the number of dominate (gray) and non-active nodes  $D_{NA}(k)$  adjacent to each non-active node of those  $k \in N1(v)$ . Once the agent gets the degree of these non-active nodes, it changes their status to be active white if they are connecting to at least one dominate (gray) node. Depending on those computed information, the agent selects one of those active nodes that has the largest degree and has largest number of non-active adjacent nodes to become dominator (black). The status of this selected node directly changed from active (white) to dominator (black). The agent is not allowed to select and add any gray node to the independent set, it changes the dominate node  $k$  (gray) to dominator (black), ensuring the connectivity of the selected dominating nodes based on MIS. The agent then moves to the one-hop nodes adjacent to those new dominator nodes to change their adjacent nodes to become dominate (gray), and so on.

This process terminates when all nodes are colored gray or black, and all the black nodes form the connected dominating set.

It is remarkable that there are two types of changes the agent performs to select the dominating nodes. The agent changes the status of the node from white active node to (independent node) black dominator node or changes the status from gray dominate to black dominator node in order to ensure the connecting of the selected dominating nodes. Whenever the agent performs the first change, it must move to each two-hop nodes of the changed node in order to mark them as non-active white nodes. In contrast that, if the agent changes the status of the node from gray dominate to black dominator, it does not perform any additional moves in order to



change the status of the two-hop nodes, as those nodes already visited.

Finally, if the agent visits all the nodes of the graph and it remained active white node, which its one-hop neighbors are dominate or white active nodes, the agent selects one of those dominate nodes that has the largest degree to become the dominator, and changes this active white node to gray dominate node.

Let us illustrate an example of construction the CDS based on MIS. As we are looking for the optimal selecting of CDS, we outbalance for the agent to implement the second scenario to guarantee the optimal selecting of dominator node in the first iteration, even though this scenario induces additional movements by the agent Figure.1.

The agent starts the implementation of the algorithm in the node  $u=1$ , it randomly explores the one-hop nodes  $v \in N1(u)$  that are adjacent to  $u$ . In each node  $v$ , the agent explores all one-hop nodes  $x \in N1(v)$  to calculate the degree of each node  $v$ . So, in the first iteration the agent explores the one-hop nodes  $N1(1)=\{2,3,6\}$  and visits the two-hop nodes  $N2(u)=\{4,5,7,8,9,10,14\}$  of the node  $u$ , it marks them non-active white. Thus, the agent knows the degree of the node 1 and the degree of each one-hop neighbor nodes of 1, it select and adds the node 6 that has the largest degree  $D(6)=7$  to the independent set,  $IS=\{6\}$ . The agent constructs the CDS simultaneously with the selecting of independent nodes. Thus, it moves to the node 6, marks this node as dominator (Black) and the connected dominating set is  $CDS=\{6\}$ . The agent moves to each one-hop neighbor nodes  $N1(6)=\{1,2,5,7,9,10,14\}$  adjacent to node 6 in order to marks them as dominate (Gray), and explores each dominate (Gray) node. It moves to the one-hop neighbor nodes adjacent to each dominate (Gray) node to mark them as non-active white and calculate the degree of each dominate (gray) node. Since the agent explored the node 3 and it knew its degree, the agent changes the status of node 3 to active white. This active node becomes qualified to belong the independent set. Therefore, the resultant independent set is  $IS=\{6,3\}$ . The agent moves to and marks the node 3 as dominator (Black) and all its adjacent non-active nodes as dominate (gray), node 4,  $N_{NA}(3)=\{4\}$ , see Figure.1b. To construct and guarantee the connection of the dominating nodes, the agent adds the dominate node 1 which is the parent node of the node 3 to the dominating set  $CDS=\{6,3,1\}$  and changes the node 1 to dominator (Black). The agent then moves to each one-hop nodes adjacent to these selected

dominator nodes and marks them gray, see Figure.1c.

To start the next iteration, the agent selects and moves to the dominate (gray) node 14 that has the largest degree,  $D(14)=5$ , and the largest number of non-active nodes  $D_{NA}(14)=3$ , 3 non-active nodes  $\{11,13,15\}$ , Figure.1d. This dominate node 14 does not allowed to be independent; it has one adjacent independent node 6. The agent moves to and explores each one-hop neighbor nodes  $N1(14)=\{7,11,13,15\}$  adjacent to node 14 in order to select the optimal independent node. The resultant of this iteration is adding new independent node to the set  $IS$ , the node 13 which has one non-active nodes  $D_{NA}(13)=1$ , non-active nodes  $\{12\}$ , the independent set becomes  $IS=\{6,3,13\}$ , see Figure.1e. The agent marks the node 13 as dominator (Black), adds it to the connected the dominating set  $CDS=\{6,3,1,13\}$  and changes its adjacent non-active node  $\{12\}$  to dominate (gray). To guarantee the connection of the dominating nodes, the agent adds the dominate node 14 which is the parent node of the node 13, that has the largest degree, to the connected dominating set  $CDS=\{6,3,1,13,14\}$ , changes the nodes 14 to dominator (Black) and changes its one-hop active nodes  $\{11,15\}$  as dominate (gray), see Figure.1f.

The third iteration starts when the agent moves to the last active node 8. This node is explored, active and all its adjacent nodes are dominate (gray). Therefore, no one of these dominate nodes would be selected as independent node. The agent selects and adds the node 8 to the independent set  $IS=\{6,3,13,8\}$ . It marks the node 8 as dominator (Black), adds it to the connected the dominating set  $CDS=\{6,3,1,13,14,8\}$ . To guarantee the connection of the dominating nodes, the agent adds the dominate node 2 or node 7 to the connected dominating set  $CDS=\{6,3,1,15,14,8,7\}$  which has the largest degree among all one-hop nodes adjacent to node 8, it selects and marks the nodes 7 as dominator (Black), see Figure.1(g).

At this point, the agent explores all the nodes in the graph. All the nodes of the graph  $G$  either dominating (Black) or dominate (gray), thus the agent successfully constructs the connected dominating set based on the maximal independent set, but this set is not minimum CDS as it consists of 7 nodes.

### 3.3. MA-CDS based on multipoint relays

In this section, we implemented two instances algorithms using the mobile agent, the original greedy algorithm which proposed by A. Qayyum in

[28] and then compare it with the extended greedy algorithm which proposed by Wu in [25] in which the free neighbor notation is introduced. In the first phase the agent applies one of these greedy algorithms in each node  $u$  to select the multipoint relay set denoted by  $MPR(u)$ , we denote the first instance by **MA-OriginalGreedy** and the second instance by **MA-ExtendGreedy** algorithms. Depending on the selected MPRs sets, the agent selects the CDS using two rules in the second phase.

#### **Greedy Algorithm:**

For each node  $u$ :

1. Add  $v \in N1(u)$  to  $MPR(u)$ , if there is a node in  $N2(u)$  covered only by  $v$ .
2. Add  $v \in N1(u)$  to  $MPR(u)$ , if  $v$  covers the largest number of nodes in  $N2(u)$  that have not been covered.

**A node  $u$  selected as a member in the CDS if it is compatible with the following rules:**

**Rule 1:** It has the largest degree than all its neighbors and it has two unconnected neighbors.

**Rule 2:** the node is a multipoint relay selected by its neighbor that has the largest degree.

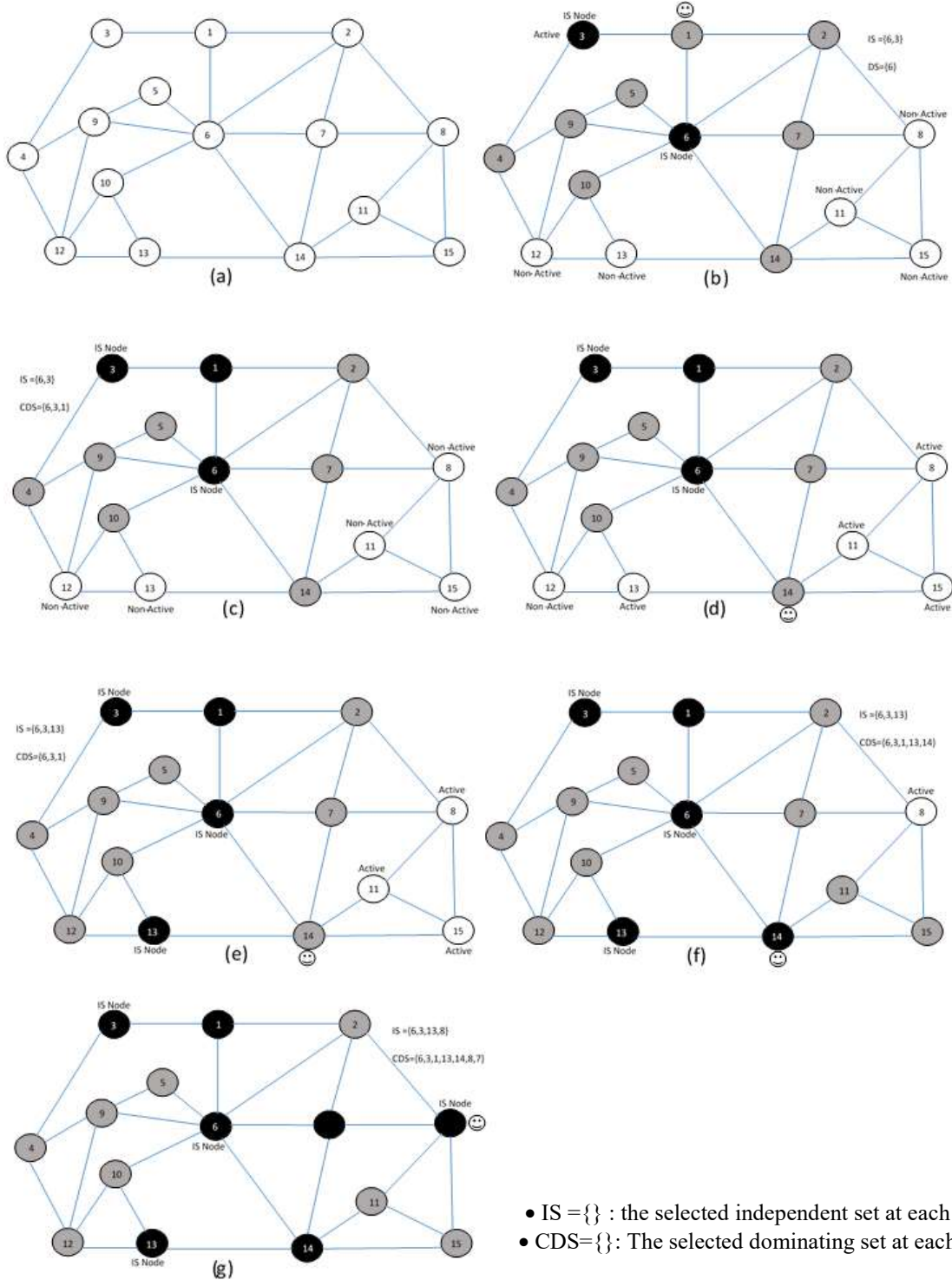


Figure.1: Constructing the CDS based on MIS algorithm.

**Extend Greedy Algorithm:**

Wu's EMPR [25] introduces a novel notation of free neighbor node in the EMPR. This notation originally introduced by using the node ID, Node  $v$  is a free neighbor of  $u$  if  $u$  is not the smallest ID neighbor of  $v$ . Chen and Shen in [22] observe that the node degree is more related to the size of the CDS instead of the ID. Therefore, based on this observation we replaced the ID by the degree of the node in our implementation through **MA-ExtendGreedy algorithm**. The node  $v$  is free neighbor of  $u$ , if  $u$  is not the largest degree neighbor of  $v$ , there is at least one neighbor of  $v$  has larger degree than  $u$ .

For each node  $u$ :

1. Add all free neighbors of the node  $u$  to the MPR( $u$ ) set.
2. Apply the original greedy algorithm to the residual one-hop neighbors to cover all remaining two-hop nodes.

**A node  $u$  selected as a member in the CDS if it is compatible with the following rules:**

**Rule 1:** It has the largest degree than all its neighbors and it has two unconnected neighbors.

**3.3.1. Rule 2:** the node is a multipoint relay selected by its neighbor that has the largest degree.

**MA-OriginalGreedy Algorithm:**

Constructing the connected dominating set simultaneously with selecting each MPR set induces unacceptable number of agent moves. The agent needs to explore all one-hop nodes and visit all two-hop node to select the MPR of the node  $u$ , then it needs to explore all one-hop nodes and visit all two-hop nodes of the node  $v \in N1(u)$ , which has the maximum degree.

Our algorithm goes in two phases, the first phase is applying the MPR heuristic algorithm to select the MPR set for each node and the second phase is globally applying the mentioned two rules. The agent selects a CDS based on the existing MPR set for each node that has generated using the original MPR heuristic algorithm. The used technique is to compute local MPR set formed in each node and then distributed in each node of the whole network to generate global CDS. The mobile agent applies the first phase to all nodes in the network, to select the MPR sets by the MPR heuristic algorithm. Then

the selected nodes as MPR become qualified to participate in the second phase to determine whether or not belong to the dominating set.

The agent in the node  $u$  intends to select a small multipoint relay set MPR( $u$ ) from the one-hop neighbor nodes  $v \in N1(u)$ . The whiteboard of each node  $u$  in the graph contains of the  $N1(u)$ , the selected MPR( $u$ ) nodes, the normal degree  $D(v)$  for each node  $v \in N1(u)$ , the exclusive degree  $D_{exc}(v)$  for each node  $v \in MPR(u)$  and the selector nodes which select the node  $u$  as one of their MPR nodes. The number of two-hop nodes of  $u$ , that be exclusively covered by  $v$  where  $v$  is an one-hop neighbor of  $u$  is  $D_{exc}(v)$ .

To be more accurate, when the mobile agent explores a node  $u$  that means the agent visited all one-hop neighbor nodes of  $u$ ,  $N1(u)$ . Nodes announced themselves means that they exchange their one-hop nodes. Two adjacent nodes  $v1$  and  $v2$  can exchange their degree, and exclusive degree  $D_{exc}(v1)$  and  $D_{exc}(v2)$  when the agent explores each one-hop neighbor nodes of them  $N1(v1)$  and  $N1(v2)$ . The mobile agent announces this information on behalf of those nodes. At the beginning, the agent does not rely on the degree of the visited nodes, the Basic criterion to select the MPR( $u$ ) of  $u$  is the existence of one node or nodes  $x \in N1(v)$  that are covered only by the node  $v \in N1(u)$  to calculate the  $D_{exc}(v)$  for each node  $v \in N1(u)$ .

**MA-OriginalGreedy:**

The agent in each node  $u$  performs the following steps:

- The agent starts the iteration at a node  $u$ ;
- Visit and explore each one-hop nodes  $v \in N1(u)$  of  $u$ ;
- Visit each one-hop nodes  $x \in N1(v)$  of  $v$ ;
- Calculate the normal degree  $D(v)$  and the  $D_{exc}(v)$ ;
- Announce the information of the one-hop neighbor nodes  $N1(v)$  to each  $x \in N1(v)$ ;
- Calculate the two-hop nodes of  $u$  and select the MPR( $u$ ) set;
- Announce the information of the one-hop neighbor nodes  $N1(u)$ , selected MPR( $u$ ) nodes and their corresponding two-hop neighbor nodes  $N2(u)$  to each  $v \in N1(u)$ ;
- End the iteration.

- Selects the node  $v \in \text{MPR}(u)$  for the next iteration which has largest  $D_{\text{exc}}(v)$ , has maximum shared one-hop nodes with the node  $u$ , and has the largest difference between its normal degree  $D(v)$  and the number of its one-hop nodes announced themselves to  $v$ .

In first iteration, the agent moves two hops from the current node  $u$ . It moves to each one-hop neighbor node  $v \in \text{N1}(u)$ . In each visited node  $v$  the agent initiates the values of the normal degree of  $v$ , the exclusive degree of  $v$  and the one-hop selector nodes in the whiteboard and then starts the exploration. It explores the node  $v$  by visiting each adjacent nodes  $x \in \text{N1}(v)$  to compute the two-hop nodes of  $u$  which are exclusively covered by each node  $v$ . Thus, the agent knows the degree of each one-hop node  $v \in \text{N1}(u)$ . Whenever the agent completes visiting the set nodes  $\text{N1}(v)$ , it again moves to those visited nodes  $x \in \text{N1}(v)$  in order to announce the information of the one-hop neighbor nodes of the node  $v$ . Those information saved in the whiteboard of each node  $x$ . Therefore, each node  $x \in \text{N1}(v)$  has the  $\text{N1}(v)$  information. The agent could not announces the  $\text{N1}(u)$  information to each node  $v \in \text{N1}(u)$ , unless the agent finishes exploring the set nodes  $\text{N1}(u)$ . The agent comes back to  $u$ , specifies the MPR set of  $u$  from  $\text{N1}(u)$ , and computes the exclusive degree  $D_{\text{exc}}(v)$  for each node  $v \in \text{MPR}(u)$ . Finally, it moves to those explored nodes  $v \in \text{N1}(u)$  in order to announce the information of the one-hop nodes  $\text{N1}(u)$  and the selected  $\text{MPR}(u)$ . The agent registers this information in the whiteboard of each node  $v \in \text{N1}(u)$ . It will registers the node  $u$  as a selector in each node  $v \in \text{MPR}(u)$  that has been selected to be multipoint relay. In this way, each node  $v \in \text{N1}(u)$  knows the one-hop nodes of the node  $u$ , those nodes represent the two-hop nodes for each other through the node  $u$ .

For the next iteration, we add additional constrains to select the node in which the agent starts this iteration. The agent selects the node  $v \in \text{MPR}(u)$  that has largest exclusive degree  $D_{\text{exc}}(v)$ , has maximum shared one-hop nodes with the node  $u$ , and has the largest difference between its normal degree  $d(v)$  and the number of its one-hop nodes announced themselves to  $v$ . Thus, we assumed that by adding this constrain the agent simultaneously computes the MPR set for more than one node in each iteration.

Whenever the agent visits node let's say  $v1$  that has been visited or explored in previous iteration,  $v1 \in \text{N1}(v)$  and  $v1 \in \text{N1}(u)$ , the agent collects shared information to compute the MPR for both nodes  $v$  and  $v1$ , it memorizes the  $\text{N1}(v)$  in the whiteboard of  $v1$  and the  $\text{N1}(v1)$  in the whiteboard of  $v$ .

Until now, the agent does not know the degree of the two-hop nodes of the node  $u$ . With the progress of the algorithm, the agent may enter a two-hop node  $x \in \text{N1}(v)$  that has the information of all its one-hop nodes  $\text{N1}(x)$ . The agent already visited this node  $x$  in different iterations. Thus, the agent computes the MPR set of node  $x$  and performs additional movements, it will move to all one-hop nodes of node  $x$  to announce the set of one-hop neighbor nodes  $\text{N1}(x)$  and its selected  $\text{MPR}(x)$  set. Following these procedure, the agent successfully select the optimal MPR nodes for each node in the graph and selects the CDS.

Let us illustrate an example of construction the CDS based on MPR set by the mobile agent. The agent starts the implementation of the algorithm in the node  $u=1$ , see Figure.2, it randomly explores the one-hop nodes  $v \in \text{N1}(u)$  that are adjacent to  $u$ . In each node  $v$ , the agent explores all one-hop nodes  $\text{N1}(v)$  to compute the degree of each node  $v$ . So, in the first iteration the agent explores the one-hop nodes  $\text{N1}(u)=\{2,3,6\}$  and visits the two-hop nodes  $\text{N2}(u)=\{4,5,7,8,9,10,14\}$  of the node  $u$ . The agent will provide the two-hop nodes of  $u$  by the information of the one-hop nodes before the one-hop nodes get the information of the node  $u$ . Thus, when the agent finishes visiting the one-hop nodes  $\{6,7,8\}$  of the node 2 which are two-hop nodes to node 1, it moves again to those nodes to announce and register the  $\text{N1}(2)$  information in the whiteboard of those nodes as well as the node 1. The agent repeats the same action for the one-hop nodes 3 and 6. The node 4 will receives  $\text{N1}(3)$  information and the nodes  $\{5,7,8,9,10,14\}$  will receive the  $\text{N1}(6)$  information respectively by the agent, table 2 shows the result of each iteration. At the end of the iteration and based on the collected information, the agent selects multipoint relay nodes of the node 1,  $\text{MPR}(1)=\{6,3,2\}$  nodes. It moves again to the one-hop nodes  $\{2,3,6\}$  to announce the  $\text{N1}(1)$  and the selected multipoint relay nodes  $\text{MPR}(1)$ . According to the original greedy algorithm the agent selects  $\{6,3,2\}$  nodes as the  $\text{MPR}(1)$ , node 6 selected as

multipoint relay for node 1 as it exclusively covers {5,9,10,14}, while node 2 selected as multipoint relay for node 1 as it exclusively covers {8} and node 3 selected as multipoint relay for node 1 as it exclusively covers {4}.

The agent then move to the node 6 according two criteria, node 6 has the largest exclusive degree among the one-hop nodes and it has the largest difference between its normal degree and the number of its one-hop nodes that it has their N1 information. The agent at each selected MPR node registers the information of the exclusive covered nodes, the exclusive degree, the information of one-hop nodes and the selectors nodes. After three iterations, the agent has visited all the nodes and has an overall vision, thus it can reach any node in the graph.

Finally, the agent be able to select the nodes that are qualified to belong to the CDS. The agent will use the two rules in the first instance and the notation of free neighbor with the two rules in the second instance. Actually, the agent by implementing those algorithms could not successfully construct the minimum connected dominating set. As we mentioned, the induced connected dominating nodes by those algorithms are large.

Figure.2 and table 1 explain the first phase for the first instance. Table 1 illustrates the generated MPR(u) sets for each node u based on the original greedy algorithm, the one-hop neighbor nodes, two-hop neighbor nodes and the selectors nodes  $v \in N1(u)$  which select u as MPR(v). All the nodes are selected as MPR except the nodes 5, 10, and 11, see the selectors column in the Table.1.

In the second phase, Rule1 and Rule2 applied to select the nodes belonged to the CDS, thus ten connected dominating nodes {1, 2, 3, 4, 6, 8, 9, 12, 13, 14} which their selectors have the largest degree and marked with red color in the Selectors column.

Table1: Multipoint relays set for each node of the graph in Figure.1a that is selected by the mobile agent based on the original greedy algorithm.

No u	MPR(u)	N1(u)	N2(u)	Selectors
1	6,2,3	2,3,6	4,5,7,8,9,10,14	2,6,3
2	6,1,8	1,6,7,8	3,5,9,10,14,15	1,6,8
3	4,1	1,4	2,5,6,9,12	4,1
4	12,3,9	3,5,9,12	1,6,10,13	5,9,12,3

5	6,4	4,6	1,2,3,7,9,10,12,14	Null
6	14,9,2,1	1,2,5,7,9,10,14	3,4,8,11,12,13,15	1,2,5,7,9,10,14
7	6,14	2,6,8,14	1,5,9,10,11,13,15	14
8	2,15	2,6,15	1,6,11,14	2,15
9	6,4,12	4,6,12	1,2,3,5,7,10,13,14	4,6,12
10	6,12	6,12,13	1,2,4,5,7,9,14	Null
11	14,15	14,15	6,7,8,13	Null
12	4,9,13	4,9,10,13	3,5,6,14	4,9,10,13
13	14,12	10,12,14	4,6,7,9,11,15	12,14
14	6,7,13	6,7,11,13,15	1,2,5,8,9,10,12	6,7,11,13,15
15	14,8	8,11,14	2,6,7,13	8,11

### 3.3.2. MA-Extended Greedy Algorithm:

The agent in each node u performs the following steps:

- The agent starts the iteration at a node u;
- Visit and explore each one-hop nodes  $v \in N1(u)$  of u;
- Announce the information of  $N[u]$  to each node  $v \in N1(u)$ ;
- Calculate the normal degree  $D(u)$  and the normal degree for each node  $v \in N1(u)$ .
- For each one-hop node  $v \in N1(u)$  except the node that has the maximum degree:
- Add the node u to the free neighbor set of v.
- Select the node  $v \in N1(u)$ , v has the maximum degree among all the nodes  $v \in N1(u)$  to start the next iteration;
- End the iteration.

The agent starts the implementation of the algorithm in the node  $u=1$ , it randomly explores the one-hop nodes  $v \in N1(u)$  that are adjacent to u. In each node v, the agent explores all one-hop nodes  $N1(v)$  to calculate the degree of each node v. So, in the first iteration the agent explores the one-hop nodes  $N1(1)=\{2,3,6\}$  and visits the two-hop nodes  $N2(1)=\{4,5,7,8,9,10,14\}$  of the node 1. It adds the node 1 as a free neighbor in the free neighbor set of the nodes {2,3} except the node 6 as this node has the maximum degree among the nodes of  $N1(1)$ , node 1 not free node of node 6. Then, the agent selects and moves to the node 6 to start the next iteration and repeats the same steps. It explores each non-explored one-hop nodes  $N1(6)=\{5,7,9,10,14\}$  and visits the two-hop nodes  $N2(6)=\{4,8,11,12,13,15\}$  of the node 6. It does not

explore any node that has its degree such node 1 and node 2. It adds the node 6 as a free neighbor in the free neighbor set of the nodes {1,2,5,7,9,10} except the node 14 as this node has the maximum degree among the nodes of N1(6). In this iteration, the agent visits all the nodes of the graph but does not explore all of them. In the third iteration the agent selects the node 14 which has the maximum degree among the nodes of N1(6), node 6 not free of the node 14 and repeats the same steps. After 6 iterations, the agent successfully explores all the nodes of the graph and selects all the free nodes for each node in the graph.

Figure.2 and table 2 illustrates the implementation of the Extended Greedy Algorithm in the first phase for the second instance. The generated one-hop free neighbors for each node  $u$  are adding to the  $MPR(u)$  sets based on the Extended greedy algorithm. We observed that the new notation of free neighbor insufficient to cover the two-hop nodes for some nodes, e.g. node 2 does not select node 8 as free neighbor, even though node 15 covered only by node 8. Likewise, the same action in node 4, which does not select nodes 3 and 12, but those one-hop nodes selected by applying the original greedy algorithm in step two. Thus, this new notation adds additional nodes to the MPR sets.

Table 2: Multipoint Relays Set For Each Node Of The Graph In Figure.1a That Selected By The Mobile Agent Based On The Extended Greedy Algorithm.

Node number	one-hop free neighbors	MPR(u)	Selectors
1	2,3,6		2, 3, 6
2	1,6,7	8	1, 6, 7, 8
3	1,4		1, 4
4	5,9	3,12	3, 5, 9, 12
5	4,6		4
6	Null	14,9,2,1	1, 2, 5, 7, 9, 10, 14
7	2,6,14		2, 8, 14
8	2,7,15		2, 15
9	4,6,12		4, 6, 12
10	6,12,13		12, 13
11	14,15		15
12	9,10,13	4	4, 9, 10, 13
13	10,12,14		10, 12, 14
14	7	6,13	6, 7, 11, 13, 15
15	8,11,14		8, 11

In the second phase, Rule1 and Rule2 applied to select the nodes belonged to the CDS, thus the same ten elected dominating nodes {1, 2, 3, 4, 6, 8, 9, 12, 13, 14} which their selectors have the largest degree and marked with red color in the Selectors column. Thus, those algorithms induce large number of dominating nodes whether we use the free neighbor notation or not. As well as, comparing to the original greedy algorithm that requires 38 selection, the extended greedy algorithm requires 46 selection in the process of electing the MPR nodes.

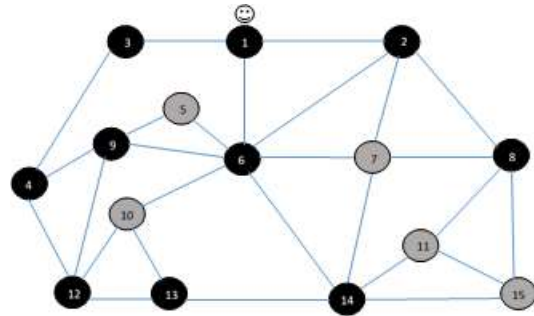


Figure.2: Selected Dominating Nodes By The Mobile Agent Based On The MPR Original And The MPR Extended Greedy Algorithms.

#### 4. CONCLUSION

In This work, we analyzed and evaluated the implementation of CDS construction based on the traditional marking, the MIS, and Multipoint Relays algorithms with slight modifications on those implemented algorithms to become appropriately used by the mobile agent. We discussed and made a comparison on the moves and iterations which performed by the agent and the final number of the constructed connected dominating nodes when the agent complete the CDS constructing. We believed that using the mobile agent has great promise alternative way instead of exchange messages approach.

Almost all connected dominating set algorithms relay on the maximum number of nodes degree in order to select the dominating nodes. The basic standard in all approaches to select the dominating node is depending on the maximum number of white nodes that directly connected to the selected dominating node. The direction of interconnection among the nodes during the selection process is from the selected dominating node toward the covered nodes. We implement two common traditional algorithms to construct CDS using the mobile agent

starting at the same node in the same graph. The first used algorithm based on the MIS and the second based on the MPR to select the dominating nodes. We noted an excess in the number of moves that have made by the agent at the earlier iterations in the exploration phase and the agent selects large number of dominating nodes. Selected dominating nodes based on the MIS illustrates good result in the number of selected dominating nodes, but the agent performs more movements. Constructing the CDS based on MPR using the mobile agent is complicated and produces inappropriate additional dominating nodes and the agent performs additional moves to ensure the independence of the selected independent set and finally to ensure the connecting of the selected dominating nodes.

For implementing these algorithms, the mobile agent intends directly to enter the node that has the largest degree in each iteration to select the dominating nodes. Thus, the agent performs large number of movements, it then tries to link other nodes (nodes have to be covered) adjacent to the selected dominating node by visiting and exploring those nodes. This behavior adds additional selected dominating nodes.

Therefore, we need an efficient approach by which the agent achieves several goals, decreases the total number of agent moves; selects the minimum connected dominating nodes; and explores the nodes with minimum degree to select an appropriate dominating node for each node. As well as the direction of the interconnection among the nodes during the selection of the dominating node must be from the covered nodes toward the selected dominating node, which means every node has its opportunity to select and connect to the optimal dominating node. We assume by following this approach, the mobile agent will potentially perform fewer movements and reduce the total cost for exploring the graph. This is the motivations for the next work, and possibility of implementing those algorithms using Multi-agents taken into account for exploring large graph.

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