

## SPEED BACKSTEPPING CONTROL OF THE DOUBLE-FED INDUCTION MACHINE DRIVE

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### ABSTRACT

This paper presents a new strategy to improve the performances of speed control of a Double-Fed Induction Machine (DFIM), whose stator and rotor windings are connected to a voltage inverter PWM (Pulse Width Modulation) independently. This work shows the robustness of the adaptive Backstepping control strategy applied to the DFIM. The main objective of this work is to stabilize the speed of the machine to be used in the Aeolians systems. The overall stability of the system is shown through using Lyapunov technique. Therefore, this paper presents the study and analysis of the Backstepping control. Finally, the simulation results of the Backstepping technique are valid on Matlab / Simulink, followed by a detailed analysis and clearly show that the proposed system provides good static and dynamic performance.

**Keywords:** *Double-fed Induction machine (DFIM); Backstepping control non-adaptive; PWM; Robustness.*

### 1. INTRODUCTION

In the recent times, in the industrial areas, the Current Alternative rotating machines are more usable especially double-fed Induction machine (DFIM), because of its many advantages over other types of rotating electrical machines. Its advantages can be summarized as following variable speed, its construction is simple, low cost, dependability, durability, and especially its maintenance is simple and economical. These benefits have made it the target of a lot of research, mainly as far as the realization of robust controls and its operation with or without a speed sensor. Double-Fed Induction machine (DFIM), is the nonlinear machine, fed by two voltage source the stator and rotor, strongly Torqued (the coupling between the electromagnetic Torque and flux), they function as multivariate machines, hence the complexity and difficulty of operation and control. With the evolution and development of new technologies of electronics and computers, the problems inherent in the control and the operation of various applications of variable speed DFIM are solved and simplified; it gives opportunities for speed control with or without mechanical sensors, as well as flux control for the

characteristics regimes hypo-synchronous and hyper-synchronous.

In this context, for a good and correct operation of the variable speed DFIM, the power converter (inverter / rectifier) PWM must be inserted to allow the design and performance of synchronization between DFIM machine and electrical network. With the use the development of modern control methods, such as the vector control flux oriented, DTC and Backstepping nonlinear control can control and stabilizes the system.

In this article, we present the non-adaptive Backstepping nonlinear control, as a method of recursive control and represents a tool for the research of dynamic stability, whose objective is to regulate the speed of the machine to the reference value regardless of external disturbances, we then apply this technique successfully to the DFIM, which gives a powerful tool for its control. In this technique we have to make sure that its parameters are constant and known. The disadvantage of this control is the sensitivity to changes in electrical and mechanical parameters of temperature, the skin effect, the magnetic saturation and the measurement errors. For this, in another study we estimate the state variables of the machine and make it more

stable and powerful to all instant changes DFIM machine system. The performance of this control will be shown by simulation results and performances. First, DFIM modeling system in Reference Park (d-q) and presentation of electronic power components. Second, the analysis and the

development of non-adaptive Backstepping control nonlinear speed of DFIM are studied.

Finally, there will be a discussion of interpretations of simulation results. In the below sample we provide a definition of general structure of an electric engine control, which is shown in Fig.1:

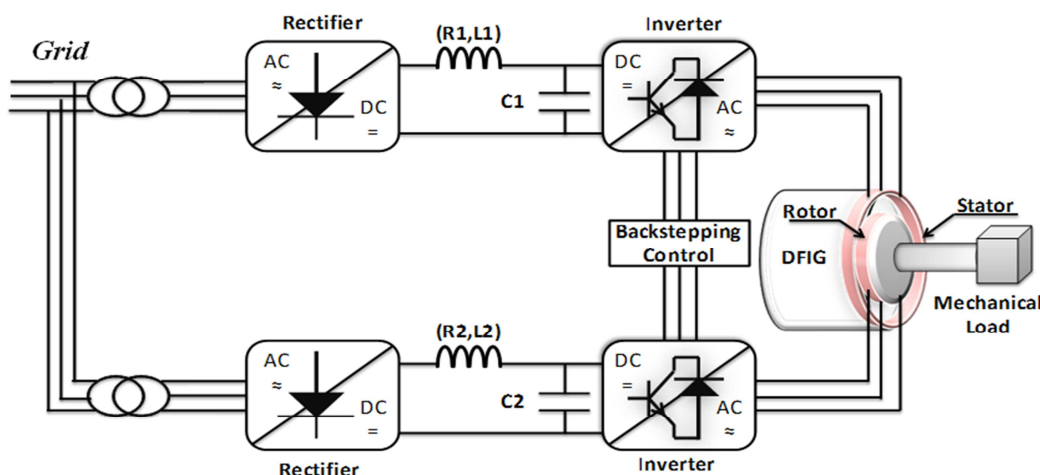


Figure 1: General Structure Of The DFIM Motor With The Backstepping Control Of Speed Regulation

## 2. MODEL OF DFIM CONTROL SYSTEM

The study and analysis of DFIM in the reference to PARK (d-q) allows us to state the following electrical equations:

$$\begin{cases} V_{sd} = R_s \cdot I_{sd} + \frac{d\varphi_{sd}}{dt} - \omega_s \cdot \varphi_{sq} \\ V_{sq} = R_s \cdot I_{sq} + \frac{d\varphi_{sq}}{dt} + \omega_s \cdot \varphi_{sd} \\ V_{rd} = R_r \cdot I_{rd} + \frac{d\varphi_{rd}}{dt} - \omega_r \cdot \varphi_{rq} \\ V_{rq} = R_r \cdot I_{rq} + \frac{d\varphi_{rq}}{dt} + \omega_r \cdot \varphi_{rd} \end{cases} \quad (1)$$

With:

$$\begin{cases} \omega_r = \omega_s - P \cdot \omega \\ I_{sd} = \frac{1}{\sigma \cdot L_s} \cdot \varphi_{sd} - \frac{M_{sr}}{\sigma \cdot L_r} \cdot \varphi_{sd} \\ I_{sq} = \frac{1}{\sigma \cdot L_s} \cdot \varphi_{sq} - \frac{M_{sr}}{\sigma \cdot L_s \cdot L_r} \cdot \varphi_{sq} \\ I_{rd} = \frac{1}{\sigma \cdot L_r} \cdot \varphi_{rd} - \frac{M_{sr}}{\sigma \cdot L_r \cdot L_s} \cdot \varphi_{sd} \\ I_{rq} = \frac{1}{\sigma \cdot L_r} \cdot \varphi_{rq} - \frac{M_{sr}}{\sigma \cdot L_r \cdot L_s} \cdot \varphi_{sq} \end{cases} \quad (2)$$

With:

$$\sigma = 1 - \frac{M^2}{L_r \cdot L_s}$$

The equations of the magnetic flux in relation to the electric current are as follows:

$$\begin{cases} \varphi_{sd} = L_s \cdot I_{sd} + M_{sr} \cdot I_{rd} \\ \varphi_{sq} = L_s \cdot I_{sq} + M_{sr} \cdot I_{rq} \\ \varphi_{rd} = L_r \cdot I_{rd} + M_{sr} \cdot I_{sd} \\ \varphi_{rq} = L_r \cdot I_{rq} + M_{sr} \cdot I_{sq} \end{cases} \quad (3)$$

The electromagnetic Torque of the DFIM is:

$$C_{em} = P(\varphi_{rd} \cdot \varphi_{sq} - \varphi_{rq} \cdot \varphi_{sd}) \quad (4)$$

By applying of the fundamental principle of dynamics, we find the following Torque:

$$C_{em} = C_r + J \cdot \frac{d\Omega}{dt} + f \cdot \Omega \quad (5)$$

With:

- $d, q$  : Indices components direct axis and quadrature axis.
- $S, R$  : Indices of the stator and rotor.
- $\theta_s, \theta_r$  : Angle tracking of the stator flux and rotor relative to the benchmark.
- $\psi$  : mechanical rotor frequency (rad/s).
- $J$  : Moment of inertia.
- $f$  : Coefficient of viscous friction



$I_d, I_q$  : two-phase stator currents and rotor in a rotating frame.  
 $V_d, V_q$  : two-phase stator voltages and rotor in a rotating frame.  
 $\varphi_{sd,q}, \varphi_{rd,q}$ : stator and rotor resistances and Flux two-phase in a rotating frame.  
 $R_s, R_r$  : stator and rotor resistances.  
 $L_s, L_r$  : stator and rotor cyclic coefficient of inductance.  
 $M_{sr}$  : coefficient of mutual inductance cyclic stator / rotor.  
 $\sigma$  : dispersion coefficient.  
 $P$  : number of pole pairs of the machine.  
 $w_s, w_r$  : angular speed (pulsation) electrical stator and rotor.  
 $C_r$  : load Torque.  
 $C_{em}$  : Electromagnetic Torque.  
 $\Omega$  : Speed of rotation of the machine.

**3. BACKSTEPPING CONTROL DFIM NONLINEAR NON-ADAPTIVE**

**3.1. Principle of Backstepping control non-adaptive**

The principle of Backstepping control non-adaptive is to analyze the stability of the system, without solving non-linear differential equations in the following form:

$$\begin{cases} \dot{x}_1 = f(x_1) + x \\ \dot{x}_2 = u \\ f(0) = 0 \end{cases} \quad (6)$$

With:

$[x_1 \ x_2]^T$  : is the state vector.

$u$ : is the control vector.

$x_1=0$  and  $x_2=0$  : is the equilibrium point of the system (the origin).

Lyapunov methods are a very powerful tool for testing and finding sufficient stability of dynamical system conditions.

The stability depends only on the variations (sign of the derivative), or a function which is equivalent, along the trajectory of the system.

The research of the stability system (6) characterized by a state vector  $[x_1 \ x_2]^T$ , consists of finding a function  $V(x)$  of definite sign, In order to illustrate the recursive procedure of backstepping method, considering that the output of the system follows the reference signal. The system (6) is of order 2 , the implementation is done in two stages.

**3.1.2. Step 1:**

We define the tracking error  $e_1$  such as:

$$e_1 = x_{1d} - x_1 \quad (7)$$

With  $x_{1d}$ : Output a desired trajectory. Its derivative (7) is:

$$\dot{e}_1 = \dot{x}_{1d} - \dot{x}_1 = \dot{x}_{1d} - f(x) - x_2 \quad (8)$$

For such a system (6), we first construct the first Lyapunov function  $V_1$  as a quadratic form:

$$V_1 = \frac{1}{2} e_1^2 \quad (9)$$

The derivative of the function is written:

$$\dot{V}_1 = e_1 \dot{e}_1 = e_1 (\dot{x}_{1d} - \dot{x}_1) = e_1 (\dot{x}_{1d} - f(x) - x_2) \quad (10)$$

To ensure the stability of the system (6), we search to ensure the negativity of the Lyapunov function  $V_1$  (9), from which the error convergence to 0 (7). For this we define a positive constant  $K_1$  such that:

$$\dot{V}_1 = e_1 (-K_1 e_1 + K_1 \dot{x}_{1d} - f(x) - x_2) \quad (11)$$

$$\dot{V}_1 = -K_1 e_1^2 + e_1 (K_1 \dot{x}_{1d} - f(x) - x_2)$$

With  $K_1 > 0$  is a constant design.

In order to ensure the stability of the system (11), a virtual control is defined as follows:

$$x_{2k} = K_1 e_1 + \dot{x}_{1d} - f(x_1) \quad (12)$$

With  $x_{2k}$  is the error value of  $x_2$ .

The derivative is:

$$\dot{x}_{2k} = K_1 \dot{e}_1 + \ddot{x}_{1d} - \dot{f}(x_1) \quad (13)$$

This implies:

$$\dot{V}_1 = -K_1 e_1^2 \leq 0 \quad (14)$$

**3.1.3. Step 2:**

Now the new desired reference variable will be the previous virtual control, it is a new regulation error  $e_2$  defined by the following equation:

$$\begin{aligned} e_2 &= x_{2k} - x_2 = K_1 e_1 + \dot{x}_{1d} - f(x_1) - x_2 \\ &= K_1 e_1 + \dot{e}_1 \end{aligned} \quad (15)$$

Its derivative is:

$$\dot{e}_2 = \dot{x}_{2k} - \dot{x}_2 = K_1 \dot{e}_1 + \ddot{x}_{1d} - \dot{f}(x_1) - \dot{x}_2 \quad (16)$$

With:

$$u = \dot{x}_2$$

So:

$$\dot{e}_2 = K_1 \dot{e}_1 + \ddot{x}_{1d} - \dot{f}(x_1) - u \quad (17)$$

To take account of this error (15), the Lyapunov function  $V_2$  is in the form:

$$V_2 = \frac{1}{2}e_1^2 + \frac{1}{2}e_2^2 \quad (18)$$

Its derivative is:

$$\begin{aligned} \dot{V}_2 &= e_1\dot{e}_1 + e_2\dot{e}_2 \\ &= e_1(e_2 - K_1e_1) + e_2(K_1\dot{e}_1 + \ddot{x}_{1d} - \dot{f}(x_1) - u) \\ &= e_1(e_2 - K_1e_1) + e_2(K_1(e_2 - K_1e_1) + \ddot{x}_{1d} - \dot{f}(x_1) - u) \\ &= -K_1e_1^2 + e_2(e_1 + K_1e_2 - K_1^2e_1 + \ddot{x}_{1d} - \dot{f}(x_1) - u) \end{aligned} \quad (19)$$

To ensure the negativity of the Lyapunov function (18), it is necessary that the expression in brackets (19) be equal to  $K_2e_2$  with  $K_2 > 0$ , in this case the command  $u$  is:

$$\begin{aligned} u &= K_2e_2 + e_1 + K_1e_2 - K_1^2e_1 + \ddot{x}_{1d} - \dot{f}(x_1) \\ &= e_2(K_1 + K_2) + e_1(1 - K_1^2) + \ddot{x}_{1d} - \dot{f}(x_1) \end{aligned} \quad (20)$$

With  $K_2 > 0$  is a constant design.

This ensures that the negative of the derivative of the Lyapunov function scope:

$$\dot{V}_2 = -K_1e_1^2 - K_2e_2^2 \leq 0 \quad (21)$$

The equation (18) is a Lyapunov function in the system (6), which proves the asymptotic stability to the origin.

The overall advantage of the Backstepping control is its flexibility, by a correct choice of the gains  $K_1$  and  $K_2$ , the equation (19) gives a convergence error to zero and consequently the output of the system follows its reference.

In this part, the main idea of the Backstepping control is demonstrated by its application to the Double-fed Induction Machine consists in establishing a control law of the machine via a Lyapunov function selected. It has the advantage of being robust towards the parametric variations of the machine and a good continuation of the references. The association of Backstepping control and orientation of rotor flux gives the control of the machine, the good qualities of interesting robustness and consolidates the overall stability of the system.

The primary purpose of non-adaptive backstepping control is to regulate the speed of DFIM to its reference value  $\Omega_{ref}$  irrespective of external disturbances. We suppose in this study that machine parameters are constant and known.

The general structure of the non-adaptive Backstepping control non-linear of the Double-fed Induction Machine (DFIM) in rotor flux oriented is detailed in the following sample:

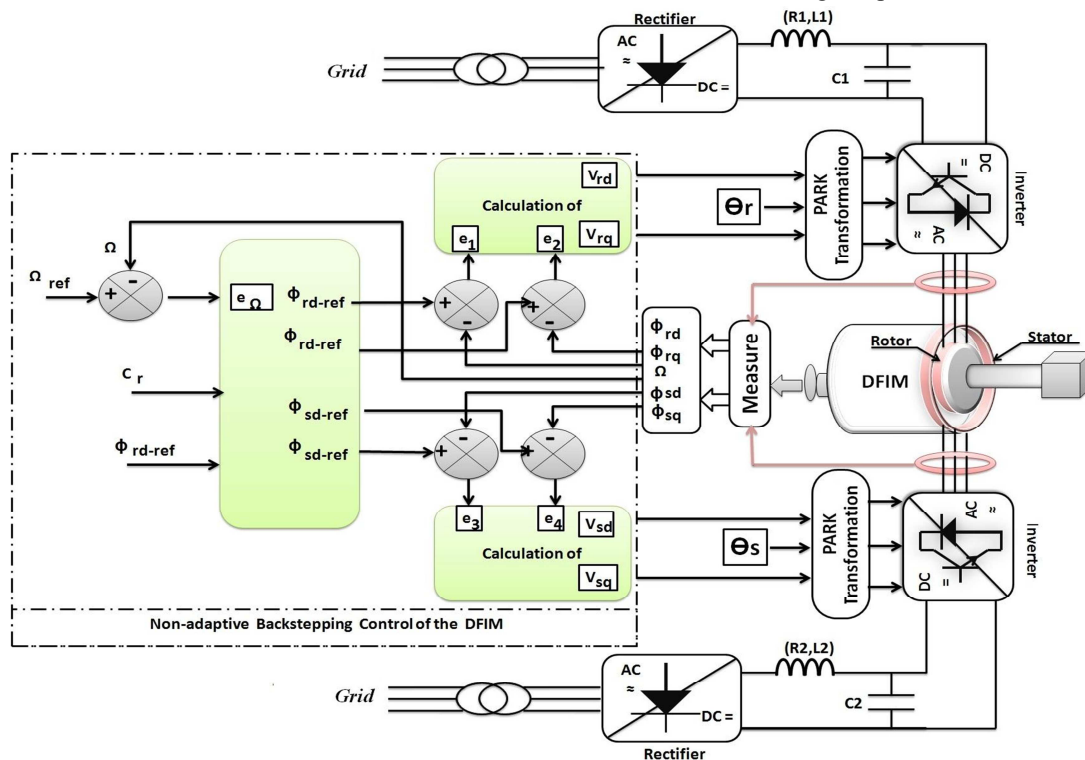


Figure 2: General structure of the non-adaptive Backstepping control the DFIM

### 3.1 Backstepping control applied to DFIM

From the electrical equations (2) of the Doubly Fed Induction Machine, we can write the following expressions:

$$\begin{aligned} \frac{d\varphi_{rd}}{dt} &= V_{rd} + \left(\frac{R_r \cdot M}{\sigma L_s L_r}\right) \varphi_{sd} - \left(\frac{R_r}{\sigma L_r}\right) \varphi_{rd} + \omega_r \cdot \varphi_{rq} \\ \frac{d\varphi_{rq}}{dt} &= V_{rq} + \left(\frac{R_r \cdot M}{\sigma L_s L_r}\right) \varphi_{sq} - \left(\frac{R_r}{\sigma L_r}\right) \varphi_{rq} - \omega_r \cdot \varphi_{rd} \\ \frac{d\varphi_{sd}}{dt} &= V_{sd} + \left(\frac{R_s \cdot M}{\sigma L_s L_r}\right) \varphi_{rd} - \left(\frac{R_s}{\sigma L_s}\right) \varphi_{sd} + \omega_s \cdot \varphi_{sq} \\ \frac{d\varphi_{sq}}{dt} &= V_{sq} + \left(\frac{R_s \cdot M}{\sigma L_s L_r}\right) \varphi_{rq} - \left(\frac{R_s}{\sigma L_s}\right) \varphi_{sq} - \omega_s \cdot \varphi_{sd} \end{aligned} \quad (22)$$

With:

The flux  $\varphi_{rd}$ ,  $\varphi_{rq}$ ,  $\varphi_{sd}$  and  $\varphi_{sq}$  are the instantaneous Torque control.

It is obvious that the dynamic model (22) is highly non-linear due to the coupling between the velocity and magnetic flux.

For the study of stability, the system is characterized by:

$[X] = [\varphi_{rd} \ \varphi_{rq} \ \varphi_{sd} \ \varphi_{sq} \ \Omega]^T$ : is the state vector (the flux and speed are measurable).

$[U] = [V_{rd} \ V_{rq} \ V_{sd} \ V_{sq}]^T$ : is the control variable (voltage stator and rotor).

To find a Lyapunov function two steps are needed one for the control of speed and the other for the control of the Flux.

### 3.2 Backstepping Controller speed.

The first step of the Backstepping control is defined Lag error of the state variable by the following calculation:

$$e_\Omega = \Omega_{ref} - \Omega \quad (23)$$

Its derivative gives:

$$\dot{e}_\Omega = \frac{de_\Omega}{dt} = \dot{\Omega}_{ref} - \dot{\Omega} \quad (24)$$

With:

$$\dot{\Omega} = \left(\frac{P(1-\sigma)}{J \cdot \sigma \cdot M}\right) (\varphi_{rd} \cdot \varphi_{sq} - \varphi_{rq} \cdot \varphi_{sd}) - \frac{f}{J} \Omega - \frac{C_r}{J} \quad (25)$$

One finds:

$$\dot{e}_\Omega = \dot{\Omega}_{ref} - \left(\frac{P(1-\sigma)}{J \cdot \sigma \cdot M}\right) (\varphi_{rd} \cdot \varphi_{sq} - \varphi_{rq} \cdot \varphi_{sd}) - \frac{f}{J} \Omega - \frac{C_r}{J} \quad (26)$$

With the application the principles of rotor flux orientation:

$$\begin{cases} \varphi_{sd} = 0 \\ \varphi_{rq} = 0 \end{cases} \quad (27)$$

It results in the following expression:

$$\dot{e}_\Omega = \dot{\Omega}_{ref} - \left(\frac{P(1-\sigma)}{J \cdot \sigma \cdot M}\right) (\varphi_{rd} \cdot \varphi_{sq}) + \frac{f}{J} \Omega + \frac{C_r}{J} \quad (28)$$

Subsequently we define the Lyapunov function of the form:

$$V_1 = \frac{1}{2} e_\Omega^2 \quad (29)$$

Its derivative gives:

$$\begin{aligned} \dot{V}_1 &= e_\Omega \dot{e}_\Omega \\ &= e_\Omega \left( \dot{\Omega}_{ref} - \left(\frac{P(1-\sigma)}{J \cdot \sigma \cdot M}\right) (\varphi_{rd} \cdot \varphi_{sq}) + \frac{f}{J} \Omega + \frac{C_r}{J} \right) \end{aligned} \quad (30)$$

Using the Backstepping design method, to ensure the stability of the sub system, for this we need to make equation (29) more negative, we consider the flux  $\varphi_{rd}$ ,  $\varphi_{sq}$  as virtual inputs of our system (22) and define the following equations:

$$\begin{cases} \varphi_{rd\_ref} = \varphi_r \\ \varphi_{sq\_ref} = \frac{1}{\left(\frac{P(1-\sigma)}{J \cdot \sigma \cdot M}\right) \cdot \varphi_{rd\_ref}} \left( K_\Omega e_\Omega + \frac{f}{J} \Omega + \frac{C_r}{J} \right) \end{cases} \quad (31)$$

With  $K_\Omega$  this is a positive constant.

We substitute equation (30) in the derivative of the Lyapunov function equation  $V_1$  (29) and assuming that  $\dot{\Omega}_{ref}$  is constant we have the negativity of the function as:

$$\dot{V}_1 = -K_\Omega e_\Omega^2 \leq 0 \quad (32)$$

Hence the asymptotic stability of the origin of the equation system (22)

### 3.3 Backstepping Controller flux

The objective of the section is the elimination of the flux regulators by calculation of the control voltages and for this we define the following errors:

$$\begin{cases} e_1 = \varphi_{rd\_ref} - \varphi_{rd} \\ e_2 = \varphi_{rq\_ref} - \varphi_{rq} \\ e_3 = \varphi_{sd\_ref} - \varphi_{sd} \\ e_4 = \varphi_{sq\_ref} - \varphi_{sq} \end{cases} \quad (33)$$

With:

$$\begin{cases} \varphi_{rq\_ref} = 0 \\ \varphi_{sd\_ref} = 0 \\ \varphi_{rd\_ref} = \varphi_r \\ \varphi_{sq\_ref} = \varphi_s \end{cases} \quad (34)$$

The results of the derivative of equation (32) are

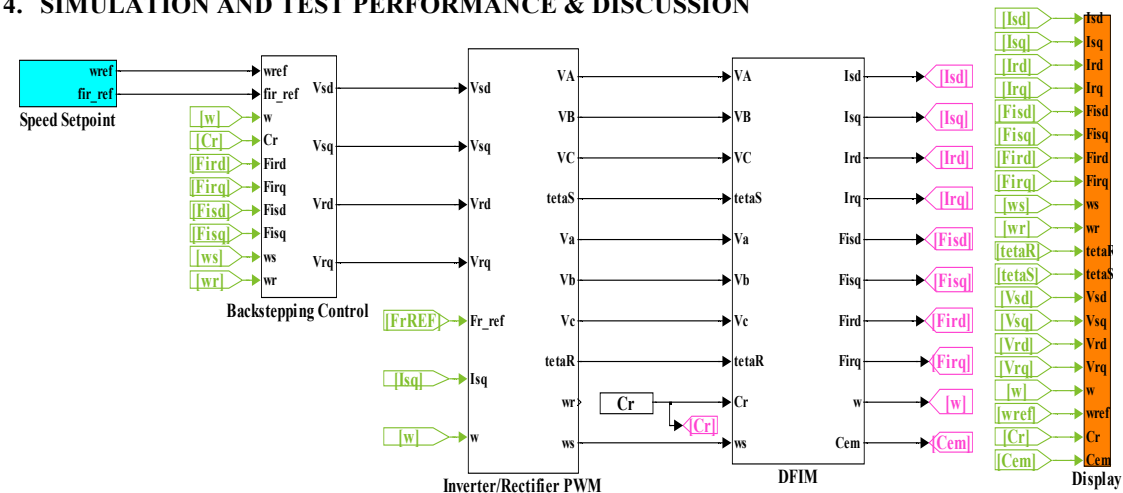
$$\begin{cases} \dot{e}_1 = \dot{\varphi}_r - V_{rd} - \left( \frac{R_r M}{\sigma L_s L_r} \right) \varphi_{sd} + \left( \frac{R_r}{\sigma L_r} \right) \varphi_{rd} - \omega_r \cdot \varphi_{rq} \\ \dot{e}_2 = -V_{rq} - \left( \frac{R_r M}{\sigma L_s L_r} \right) \varphi_{sq} + \left( \frac{R_r}{\sigma L_r} \right) \varphi_{rq} + \omega_r \cdot \varphi_{rd} \\ \dot{e}_3 = -V_{sd} - \left( \frac{R_s M}{\sigma L_s L_r} \right) \varphi_{rd} + \left( \frac{R_s}{\sigma L_s} \right) \varphi_{sd} - \omega_s \cdot \varphi_{sq} \\ \dot{e}_4 = \dot{\varphi}_s - V_{sq} - \left( \frac{R_s M}{\sigma L_s L_r} \right) \varphi_{rq} + \left( \frac{R_s}{\sigma L_s} \right) \varphi_{sq} + \omega_s \cdot \varphi_{sd} \end{cases} \quad (34)$$

The laws of real machine control are  $V_{sd}$ ,  $V_{sq}$ ,  $V_{rd}$  and  $V_{rq}$  appear in equation (33), then to analyze the stability of this system, we define a new Lyapunov final function  $V_2$  is given by the following form:

$$V_2 = \frac{1}{2} (e_\Omega^2 + e_1^2 + e_2^2 + e_3^2 + e_4^2) \quad (35)$$

The result of the derivative of equation (34) is:

#### 4. SIMULATION AND TEST PERFORMANCE & DISCUSSION



$$\begin{aligned} \dot{V}_2 &= -K_\Omega e_\Omega - K_1 e_1 - K_2 e_2 - K_3 e_3 - K_4 e_4 + \\ & e_\Omega \left( K_\Omega \dot{e}_\Omega - \left( \frac{P(1-\sigma)}{J \cdot \sigma M} \right) \varphi_r \cdot \varphi_s \right) + \frac{f}{J} \Omega + \frac{C_r}{J} + \\ & e_1 \left( K_1 \dot{e}_1 + \dot{\varphi}_r - V_{rd} - \left( \frac{R_r M}{\sigma L_s L_r} \right) \varphi_{sd} + \left( \frac{R_r}{\sigma L_r} \right) \varphi_{rd} - \omega_r \cdot \varphi_{rq} \right) + \\ & e_2 \left( K_2 \dot{e}_2 - V_{rq} - \left( \frac{R_r M}{\sigma L_s L_r} \right) \varphi_{sq} + \left( \frac{R_r}{\sigma L_r} \right) \varphi_{rq} + \omega_r \cdot \varphi_{rd} \right) + \\ & e_3 \left( K_3 \dot{e}_3 - V_{sd} - \left( \frac{R_s M}{\sigma L_s L_r} \right) \varphi_{rd} + \left( \frac{R_s}{\sigma L_s} \right) \varphi_{sd} - \omega_s \cdot \varphi_{sq} \right) + \\ & e_4 \left( K_4 \dot{e}_4 + \dot{\varphi}_s - V_{sq} - \left( \frac{R_s M}{\sigma L_s L_r} \right) \varphi_{rq} + \left( \frac{R_s}{\sigma L_s} \right) \varphi_{sq} + \omega_s \cdot \varphi_{sd} \right) \end{aligned} \quad (36)$$

With  $K_1$ ,  $K_2$ ,  $K_3$  and  $K_4$  are positive constants. Extracted from equation (35) expressions the controls voltages  $V_{sd}$ ,  $V_{sq}$ ,  $V_{rd}$  and  $V_{rq}$  as following:

$$\begin{cases} V_{rd} = \left( K_1 \dot{e}_1 + \dot{\varphi}_r - \left( \frac{R_r M}{\sigma L_s L_r} \right) \varphi_{sd} + \left( \frac{R_r}{\sigma L_r} \right) \varphi_{rd} - \omega_r \cdot \varphi_{rq} \right) + \\ V_{rq} = e_2 \left( K_2 \dot{e}_2 - \left( \frac{R_r M}{\sigma L_s L_r} \right) \varphi_{sq} + \left( \frac{R_r}{\sigma L_r} \right) \varphi_{rq} + \omega_r \cdot \varphi_{rd} \right) + \\ V_{sd} = e_3 \left( K_3 \dot{e}_3 - \left( \frac{R_s M}{\sigma L_s L_r} \right) \varphi_{rd} + \left( \frac{R_s}{\sigma L_s} \right) \varphi_{sd} - \omega_s \cdot \varphi_{sq} \right) + \\ V_{sq} = e_4 \left( K_4 \dot{e}_4 + \dot{\varphi}_s - \left( \frac{R_s M}{\sigma L_s L_r} \right) \varphi_{rq} + \left( \frac{R_s}{\sigma L_s} \right) \varphi_{sq} + \omega_s \cdot \varphi_{sd} \right) \end{cases} \quad (37)$$

This equation (36) implies the negativity of the following Lyapunov function  $V_2$ :

$$V_2 = -K_\Omega e_\Omega - K_1 e_1 - K_2 e_2 - K_3 e_3 - K_4 e_4 \leq 0 \quad (38)$$



Figure 3: Simulation scheme of the non-adaptive Backstepping Control on Matlab & Simulink environment

To verify the performance and the asymptotic stability of the non-adaptive Backstepping control, The DFIM is object to the tests of robustness for varying conditions of functioning at a nominal charge, rated speed, variation in speed, machine parameters and load change. We implemented the system in Matlab / Simulink environment according to the scheme following principle (Fig.3).

The values of the gains of the non-adaptive Backstepping control are selected after several tests adjustment ( $K_{\Omega}=550$ ;  $K_I=700$ ;  $K_2=500$ ;  $K_3= 800$ ;  $K_4= 900$ ). The different results of simulation tests obtained are subsequently exposed.

#### 4.1 Followed of the trajectory with constant speed

The study makes for a constant speed  $\Omega_{ref}=150rad/s$  to  $0s$ ,  $\varphi_{rd,ref}=10wb$  and  $C_r = 0N.m$ . the following figures (4, 5, 6) show the performance of the control input and output linearization.

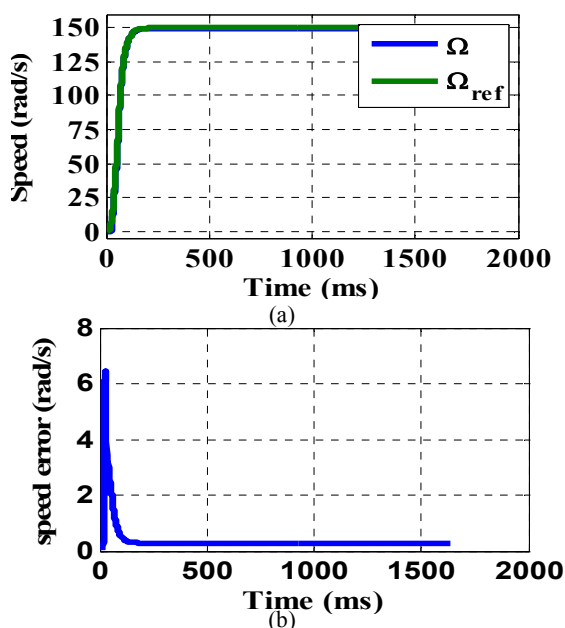


Figure 4: (a) Speed of Rotation; (b) Speed error.

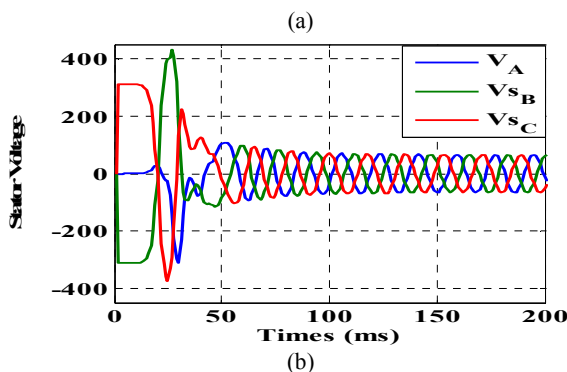
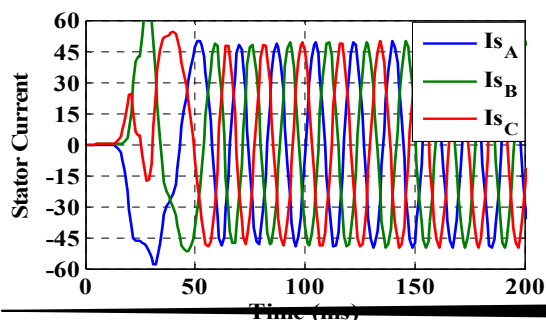


Figure 5: (a) Stator Current; (b) Stator Voltage

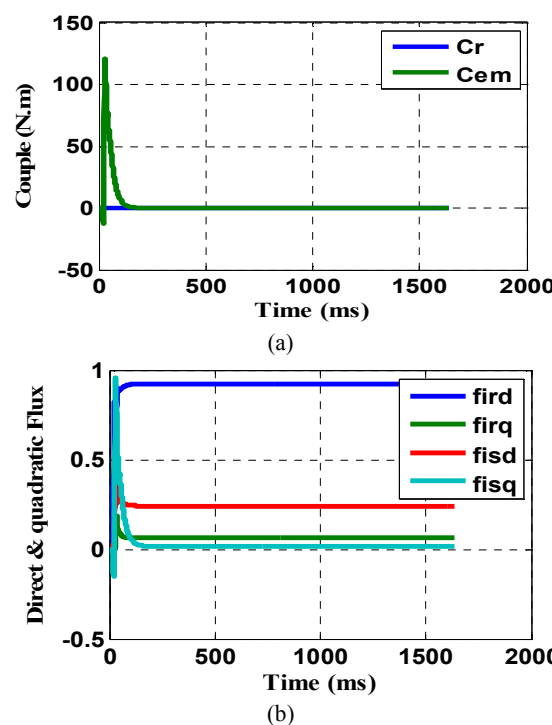


Figure 6: (a) Torque; (b) Direct and quadratic Flux

The results obtained by the application of non-adaptive Backstepping control of the DFIM show excellent performance and good pursuit speed to its reference.

The good decoupling between the flux and Torque is maintained, the flux is similar to the nominal case. Voltages and currents present variations according to regime change, the static error rapidly converging to zero for this study profile.

4.2 Followed by the trajectory with variable speed and a change of rotation direction

In figures (7, 8, 9) following, the Flux is constant ( $\phi_{rd\_ref}=10wb$ ) and null load Torque ( $C_r=0N.m$ ), the DFIM accelerated to the nominal speed (150rad/s), Then, the machine decelerates and the direction of rotation is reversed (-150rad/s), after a moment the machine is accelerated again but at a low speed (50 rad/s).

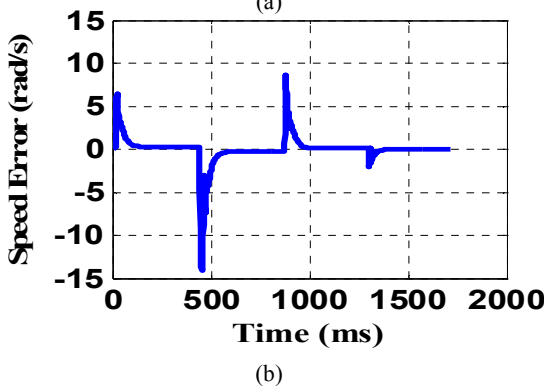
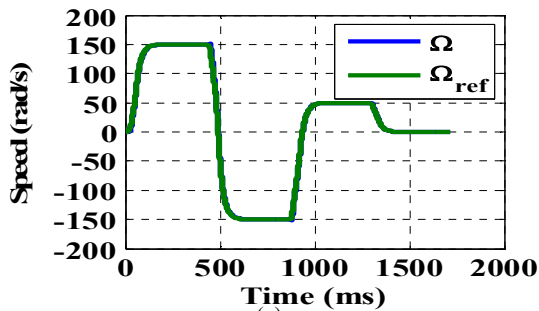
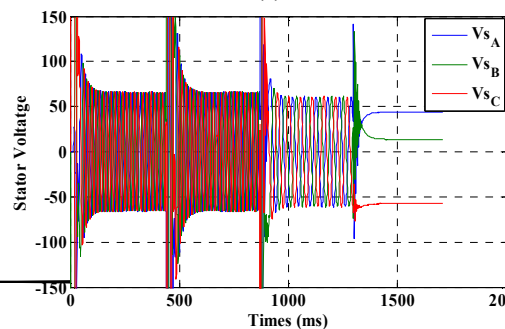
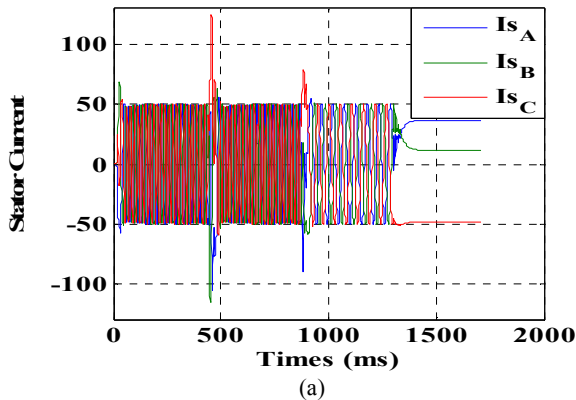


Figure 7: (a) Speed of Rotation; (b) Speed error.



(b)

Figure 8: (a) Stator Current; (b) Stator Voltage

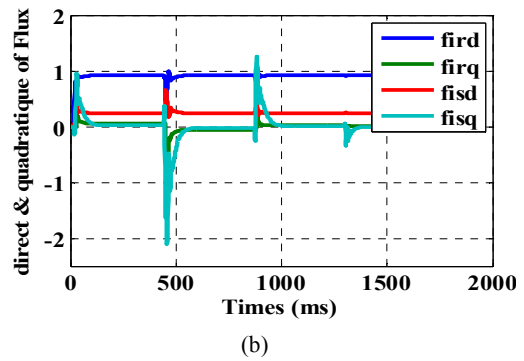
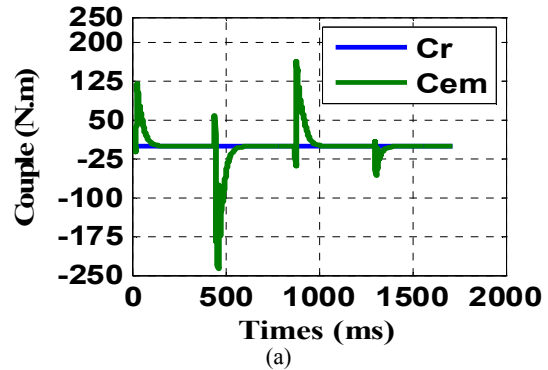


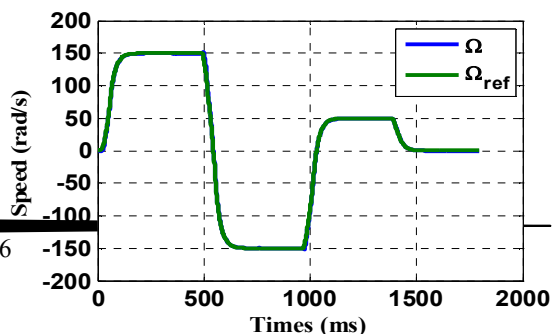
Figure 9: (a) Torque; (b) Direct and quadratic Flux

In this part of the profit studies are perfect, the modules of voltages and currents are constant, observed speed almost perfectly follows its reference.

The flux and Torque are constant modules, decoupling between the flux and the Torque is quite good.

4.3 Followed by the trajectory with a variation of the nominal load

In the same preceding conditions, the machine runs to a nominal variable speed, initially without load, at time  $t = 0.7s$  is applied to the machine a nominal load  $C_r=20N.m$ , then the Torque load demined to  $C_r=5N.m$  at time  $t = 1.5s$ .





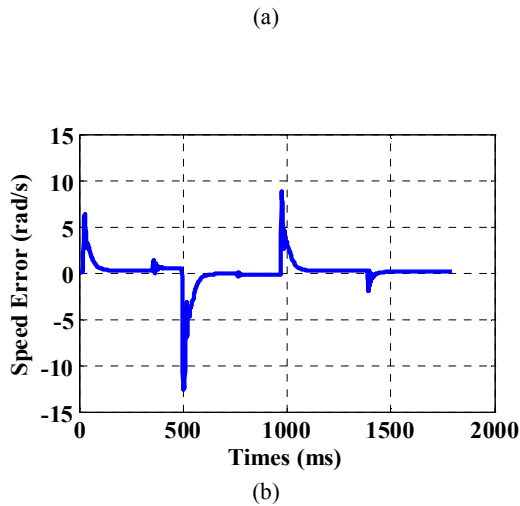


Figure 10: (a) Speed of Rotation; (b) Speed error.

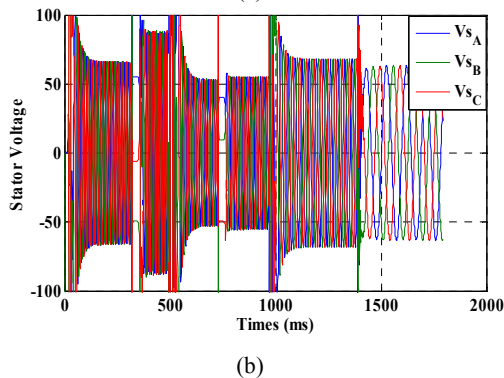
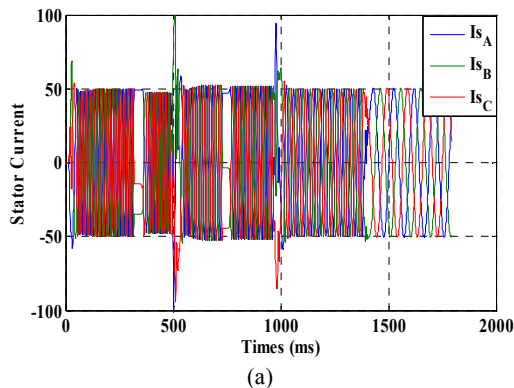


Figure 11: (a) Stator Current; (b) Stator Voltage

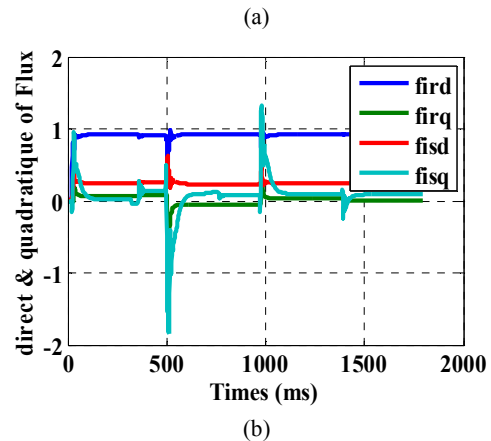
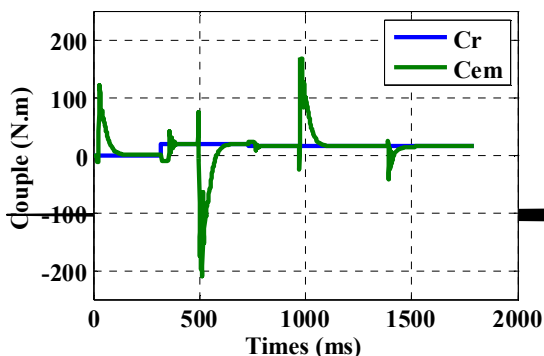


Figure 12: (a) Torque; (b) Direct and quadratic Flux

The simulation results show a good function of the machine in spite of the variation of the load, the voltage and the stator current experience an increase proportionally to that of the machine load, the speed and the Torque have a good track their set point, the decoupling of Torque and flux is always achieved.

We also note that the orientation of the rotor flux is perfectly realized and verified. This shows the perfect adaptation of the Backstepping control to the orientation of the rotor flux. In order to test the robustness of the controller, the electrical and the mechanical parameters are varied in the non-adaptive controller.

Indeed, the values of the resistor, the inductance changes are some percentages of the nominal value.

## 5. CONCLUSION

The aim of this work is devoted to modeling, development and simulation of non-adaptive Backstepping control for double-fed Induction Machine, connected directly to voltage converter PWM.

In the following, we highlight the improvement made by the non-adaptive Backstepping control on the dynamic performance of DFIM.

The originality of our work is to combine the simulation experiments of different control algorithms to define a control structure realizing the best value simplicity and performance.

Finally, we believe that the proposed solutions will improve the tracking performance of the trajectory and disturbance rejection load Torque

and parameter variations and also enhance stability through the robust look of the non-adaptive Backstepping control. The disadvantage of this control is that it is unable to eliminate the non-zero errors.

**ANNEXE**

Table 1: DFIM parameters used in simulation

|                                 |                           |
|---------------------------------|---------------------------|
| Stator resistance               | $R_s=1.2 \text{ m}\Omega$ |
| Rotor resistance                | $R_r=1.8 \text{ m}\Omega$ |
| Stator inductance               | $L_s = 0.1554 \text{ mH}$ |
| Rotor inductance                | $L_r = 0.1554 \text{ mH}$ |
| mutual inductance               | $M=0.15$                  |
| Inertia moment                  | $J=0.07 \text{ Kg.m}^2$   |
| Coefficient of viscous friction | $f=0.001$                 |
| Number of pairs of poles        | $P=2$                     |

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