

## PAPR REDUCTION TECHNIQUES IN OFDM SYSTEMS USING DCT AND IDCT

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### ABSTRACT

Orthogonal frequency division multiplexing (OFDM) has gained much popularity in the field of wireless communication because of its ability to transfer the data at higher rate, high bandwidth efficiency and its robustness to multipath. Since OFDM has high Peak to Average Power Ratio (PAPR) as major limitation, many techniques were proposed to reduce it. In this paper, a DCT based modified selective mapping (SLM) technique is proposed to reduce the PAPR of the transmitted signal and its PAPR reduction performance compared with that of IFFT based modified SLM technique, IDCT based modified SLM technique and IDST based modified SLM technique. The proposed technique for PAPR reduction grants an improvement over the existing IFFT.

**Keywords:** OFDM, PAPR, Selective Level Mapping, Discrete Cosine Transform, IDCT, IDST.

### 1. INTRODUCTION

Orthogonal Frequency Division Multiplexing (OFDM) is a multi-carrier modulation technique for high data rate wireless communication because of its robustness to frequency selective fading, high spectral efficiency and less computational complexity [1, 2]. OFDM separates the available spectrum into a number of overlapping but orthogonal narrowband sub-channels as shown in Figure 1, and hence the OFDM converts a frequency selective channel into a non-frequency selective channel. The prime advantage of OFDM lies in its ability to cope with severe frequency-selective fading due to multi-path without complex equalization filters. One of the major drawbacks of OFDM transmission is high Peak to Average Power Ratio (PAPR).

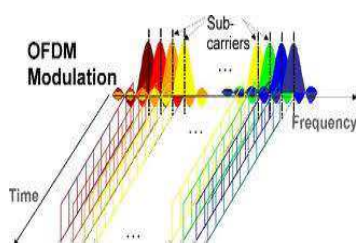


Figure: 1 OFDM modulation

High PAPR signals are usually undesirable for it usually strains the analog circuitry. A large PAPR brings disadvantage like an increased complexity of

the analog to digital conversion and digital to analog conversion and reduces the efficiency of RF

Power amplifier PAPR of OFDM signal increases with increase in the number of subcarriers which causes poor efficiency and degrades the system performance of power amplifier [3]. To overcome such effect, many PAPR reduction technique such as coding distortion and distortion less techniques have been proposed for OFDM signals [4]. Distortion less techniques such as Selective Level Mapping (SLM) [5] and Partial Transmit Sequence (PTS) [6] can improve the PAPR statistics with only a small data rate loss but has no inherent error control.

In the SLM, the input data bit sequences are multiplied by each of the phase sequences to generate alternative input symbol sequences. Each of these alternative input data sequences is made the Inverse Fast Fourier Transform (IFFT) operation, and then the one with the least PAPR is selected for transmission [7]. Although some techniques of PAPR reduction have been summarized in [8], an effective PAPR reduction technique should be given the best trade-off between the capacity of PAPR reduction and transmission power. In OFDM system if the subcarriers are of large value the real and imaginary value of complex base band signal become Gaussian distribution and the amplitude of OFDM signal has Rayleigh distribution and exhibits strong fluctuations. Therefore, the resultant PAPR can be high. In the worst case, PAPR of an OFDM system

with N sub channels may reach up to a value of N. High PAPR value has some disadvantages for

OFDM modulation. High PAPR results from the nature of the modulation where multiple subcarriers and sinusoids are added together to the signal to be transmitted. When N sinusoids add, the peak magnitude would have a value of N, where the (rms) average might be quite low due to destructive interference between the sinusoids.

High PAPR signals would require a large range of dynamic linearity from the analog circuits, which usually results in expensive devices, and higher power consumption/lower efficiency for example, power amplifier has to operate with larger back off to maintain linearity and needs to be reduced to an acceptable level. In the literature various methods are proposed for the purpose of PAPR reduction. It should be noted that most of the method are based on the same idea of selecting the time domain signal to be transmitted from a set of different representations with the constraint of minimization of PAPR which would degrade the performance of system. This technique can be categorised into Signal scrambling techniques and Signal distortion techniques. The fundamental principle of techniques is to scramble each OFDM signal with different scrambling sequences and select one which has the smallest PAPR value for transmission. This type of approach includes Selective Mapping (SLM) and Partial Transmit Sequences (PTS). SLM method applies scrambling rotation to all sub-carriers independently while PTS method only takes scrambling to part of the sub-carriers. Pepin Magnangana Zoko Goyoro, et al proposed a [3] scheme which consists of DCT matrix transform followed by the SLM using Riemann matrix for the phase sequence to reduce PAPR. However to reduce PAPR and computational complexity further DCT based modified SLM technique is proposed in this paper.

DCT based modified selective mapping technique is used to reduce the PAPR. This method combines Discrete Cosine Transform (DCT) with modified Selective Level Mapping (SLM). In DCT based modified SLM Inverse Discrete Sine Transform (IDST) and Inverse Discrete Cosine Transform (IDCT) are also used along with IFFT

The paper is organized as follows. Section 2 briefly introduces PAPR of OFDM signals, Section3 gives an overview of SLM technique is described. The detailed description of DCT based

OFDM technique is shown in Section 4 and 5. The discussions and simulation results are presented in

Section 6. Finally, conclusions are given in Section7.

## 2. PAPR OF OFDM SIGNALS

The PAPR of transmitted OFDM is defined as the ratio between the maximum instantaneous power and the average power, defined by:

$$PAPR = \frac{\max |x(t)|^2}{E [ |x(t)|^2 ]} \quad (1)$$

Where  $x(t)$  denotes an OFDM signals after IFFT, and  $E [.]$  denotes expectation. Let us denote the data block of length N as a vector  $Y = [Y_0, Y_1, Y_2, \dots, Y_{N-1}]^T$  where N is equal to the number of subcarriers and  $(.)^T$  denotes transpose. The duration of a data symbol in X modulates one of a set of subcarriers,  $\{f_{m,m} = 0, 1, \dots, N-1\}$ . The N subcarriers are chosen to be orthogonal, that is  $f_m = m\Delta f$ , where  $\Delta f = 1/NT$  and NT is the duration of an OFDM data block. The complex envelope of the transmitted OFDM signal is given by

$$X(t) = \frac{1}{\sqrt{N}} \sum_{k=0}^{N-1} Y_k e^{j2\pi k \Delta f t} \quad (2)$$

where  $Y_k$  is the data symbol carried by the  $k^{\text{th}}$  subcarrier.

According to the limit central theorem, when N is large, both real and imaginary part of  $s(t)$  is Gaussian distributed. The Cumulative Distributed Function (CDF) of the signal is

$$F(z) = 1 - e^{-z} \quad (3)$$

If there are N subcarriers in an OFDM system, and all the sampling values are complete independent, the CDF of the system is given by the equation:

$$P(PAPR \leq z) = F(z)^N = (1 - \exp(-z))^N \quad (4)$$

So in case of no over sampling, the Complementary Cumulative Distribution Function (CCDF), this is usually used as an important parameter to describe the PAPR of an OFDM signal which is written as follows

$$P(PAPR > PAPR_0) = 1 - (1 - e^{-PAPR_0})^N \quad (5)$$

where  $PAPR_0$  is the clipping level. This equation is read as the probability that the PAPR of a symbol block exceeds some clip level  $PAPR_0$ .

SLM is one of the probabilistic techniques adopted to reduce the PAPR of the OFDM signal. Hence it can achieve PAPR reduction without distorting the signal and will not cause any loss of data. The main disadvantage of SLM is that the complexity is high. Now there are many extension schemes for reducing the complexity of SLM [13-16].

### Selective Level Mapping

As shown in Figure 2, In SLM technique the input data is partitioned into  $Y$  data block of length  $N$ . Then the OFDM data block is multiplied element by element with phase sequence  $E^{(u)} = [e_{u,0}, e_{u,1}, \dots, e_{u,N-1}]^T$  where  $u=1, 2, \dots, U$ ,  $U$  phase rotated OFDM data block  $Y^u$  is obtained.

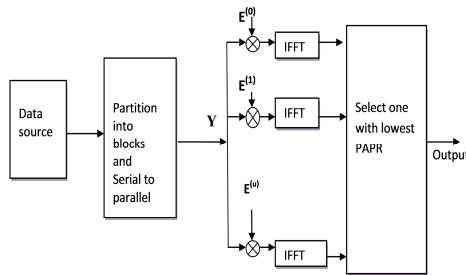


Figure.2 Selective level mapping scheme

All phase rotated OFDM data blocks represent the same information as the unmodified OFDM data block provided that the phase sequence is known.

$$Y(t) = \frac{1}{\sqrt{N}} Y_k e_m k e^{j2\pi k \Delta f t} \quad (6)$$

Among the phase rotated OFDM data blocks one with the lowest PAPR is selected and transmitted. The information about the selected phase sequence should be transmitted to the receiver as side information. At the receiver, reverse operation should be performed to recover the unmodified OFDM data block. In ordinary SLM technique, there is no restriction on the construction of phase sequence  $s$ . However, we set a structural limitation on the phase sequence for modified SLM.

### 3.1 DCT Transform

The peak value of the auto correlation is the average power of input sequence. DCT conceptually extends the original  $N$ -point data sequence to  $2N$ -point sequence by doing mirror – extension of the  $N$ -point data sequence. Since the both end of data is always continuous in the DCT, the lower order of components will be dominated in the transform domain signal after converted by DCT. The DCT is a Fourier-like transform, which was first proposed by Ahmed et al. [17] [20]. The idea to use the DCT transform is to reduce the autocorrelation of the input sequence to reduce the peak to average power problem and the transmitted signal does not require any side information at the receiver. In the section, we briefly review DCT transform. The 1D discrete cosine transform (1D DCT)  $A[k]$  of a sequence  $a[n]$  of length  $N$  is defined as:

$$A[k] = a[k] \sum_{n=0}^{N-1} a[n] \cos \left[ \frac{\pi(2n+1)k}{2N} \right] \quad (7)$$

For  $k = 0, 1 \dots N-1$ , the inverse DCT is defined as

$$a[n] = \sum_{k=0}^{N-1} a[k] A[k] \cos \left[ \frac{\pi(2n+1)k}{2N} \right] \quad (8)$$

$n = 0, 1 \dots N-1$  where  $a[k]$  is defined as:

$$a[k] = \begin{cases} \sqrt{1/N} & \text{for } k=0 \\ \sqrt{2/N} & \text{for } k=1, 2, \dots, N-1 \end{cases} \quad (9)$$

The basis sequences of the 1D DCT are real, discrete-time sinusoids defined by:

$$C_N[n, k] = \cos \frac{\pi(2n+1)k}{2N} \quad (10)$$

The DCT basis consists of the following  $N$  real sequences.

$$C_N[n, 0], C_N[n, 1], \dots, C_N[n, N-1] \quad (11)$$

The equation (7) is expressed in matrix

$$A = C_N a \quad (12)$$

Where  $A$  and  $a$  are both the vector with  $N \times 1$  and  $C_N$  is a DCT transform matrix with  $N \times N$ .

The row (or column) of the DCT matrix  $C_N$  are orthogonal matrix vectors. Then we can use this property of the DCT matrix and reduce the peak power of OFDM signals. DCT can reduce the autocorrelation between the each component of

OFDM signal this is the root cause to reduce PAPR.

### 3.2 DCT with Modified Selective Level Mapping

DCT along with Selective Level Mapping become an efficient PAPR reduction technique by integrating SLM and DCT matrix transform. PAPR is reduced by modifying the OFDM signal without any distortion, but still the complexity of SLM is high. For every OFDM frame, SLM technique requires 'n' IFFT operation and this operation makes the system complicated. So as to prevail over system complexity of SLM, modified SLM is proposed. The modified SLM reduces IFFT block and also the PAPR. This technique comprises of an IFFT block at the transmitter end and the decision of selecting data with lowest PAPR is accomplished using a decision algorithm before IFFT. The algorithm for modified SLM is given as follows,

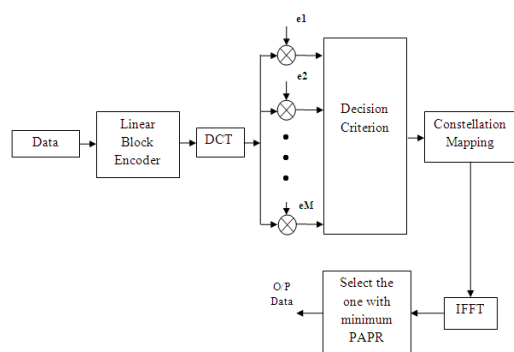


Figure. 3 Modified SLM with IFFT

#### Algorithm

- i. Let  $X_1, X_2, \dots, X_n$  be the Binary information blocks.
- ii. Assume  $W$  as the encoding code word.
- iii. Every block is encoded into  $w$  using Hamming encoder.
- iv. A control bit is appended to  $w$  and extended hamming code of 8-bits is calculated.
- v. The error table and coset leader is computed.
- vi. Vectors  $w+e1, w+e2, \dots, w+e16$  are constructed for (every code word)  
Calculate  $A = X^2 + Y^2 + Z^2$ .
- vii. Code word that has minimum  $A$  is chosen and transformed into OFDM signal through constellation mapping and IFFT.

The block diagram of DCT with modified SLM using IFFT is shown in Fig. 2 and the corresponding output signal is described by assume,  $s = [s_0, s_1 \dots s_{n-1}]^T$  as a discrete time OFDM signal vector. Then, the IFFT of vector  $s$  takes the form as,

$$s = QS \tag{13}$$

where,  $Q$  symbolizes the IFFT matrix and it can be represented as, [13]

$$Q = \begin{bmatrix} 1 & 1 & \dots & 1 \\ 1 & e^{j2\pi/n} & \dots & e^{j2\pi(n-1)/n} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & e^{j2\pi(n-1)/n} & \dots & e^{j2\pi(n-1)(n-1)/n} \end{bmatrix} \tag{14}$$

Thus, as column matrix IFFT matrix  $Q$  can be expressed as,

$$Q = [Q_0 \ Q_1 \ \dots \ Q_{n-1}] \tag{15}$$

In this proposed system, DCT with modified selective level mapping technique is considered to reduce the PAPR in OFDM system. The sequence of process is given below.

- i. At the transmitter end, the source data is forwarded to the linear block encoder
- ii. To the outcome of encoder DCT is applied and the transformed data is processed by modified SLM unit
- iii. The modified algorithm illustrated in algorithm-1 is invoked
- iv. The information with low PAPR is selected and output is generated

### 3.3. LINEAR BLOCK CODES

When the error control coding and OFDM modulation process work together such system is called COFDM. The purpose of taking adjacent bits in the source data is to spread them out across multiple subcarriers. One or more subcarriers may be lost or impaired due to a frequency null and this loss would cause a continuous stream of bit error. Such an error is a burst of errors would typically be hard to correct. The main purpose of the modified SLM technique is to reduce PAPR and IFFT, IDCT block. There is only one IFFT and one IDCT block at transmitter. The sequence which is the lowest

PAPR can be obtained out by a decision algorithm before IFFT and IDCT.

Consider an  $[n, k]$  Linear code  $C$  with parity-check matrix  $H$ , where  $n$  is the length and  $k$  is the dimension of  $W$ . Since  $Hw^t=0$  for any codeword  $w \in W$ , any vector  $X \in e+w$  has the same syndrome as  $e$ , that is [2]

$$Hx^t = H(e+w)^t = He^t \quad (16)$$

A binary information sequence is divided into blocks of 4 bits. Each message block is encoded into a codeword  $W$  which is 7 bits by a  $[7, 4]$  hamming encoder. The parameters of the binary hamming codes are typically expressed as a function of a single integer  $u \geq 2$  (for  $u=3$ , we have a  $(7, 4)$  Hamming code) not necessarily prime, it is any positive integer. A hamming code on  $GF(2)$  has code length  $n=2^u-1$ , message length  $k=2^u-1-u$ , redundancy  $n-k=u$  and error correcting capability  $t=1$ bit.

Hamming codes are only single error correcting. To improve the error detection and connection capability by adding parity check digit. The resulting code is called the extended binary hamming code. Suppose that  $w$  is a code over the alphabet  $\{0,1\}$ . Let  $w$  be the code obtain by adding a single character to the end of each word in  $w$  in such a way that every word in  $w$ . has even weight. The parity check matrix of  $[8, 4]$  extended hamming code  $w$  is  $H$ :

$$H = \left[ \begin{array}{c|c} H & \begin{matrix} 0 \\ \vdots \\ 0 \end{matrix} \\ \hline \begin{matrix} 1 \dots 1 \end{matrix} & 1 \end{array} \right] \quad (17)$$

According to the formula  $S = eH^T$ , the syndromes which are corresponding to the non-error and one error patterns could be obtained. And other seven two errors patterns could be obtained from the other syndromes. So the standard array of  $c$ . is constructed. The standard array an  $[n, k]$  binary linear code  $C$  is a  $X \times Y$  array and for extended array an  $[8, 4]$  for binary linear code  $c$ . is also  $X \times Y$  array. where  $X=2u-K$ ,  $Y=2K$ . At last sixteen vectors are constructed as  $w + e_1, w + e_2 \dots w + e_{16}$ , where  $e_1 = 0$  and  $e_1, e_2, \dots, e_{16}$  are properly selected as the coset leaders of the standard array in terms of their PAPR. Then the Decision criterion is used to calculate the value of  $A$ . Finally, the scrambled codeword with the

minimum  $A$  is selected and then transformed to an OFDM signal by constellation mapping and IFFT.

Table 1 Standard array of  $[n, k]$  linear code

	$e_1 = w_1$	$w_2$	...	$w_N$
Zero codeword	$e_2$	$w_2 + e_2$	...	$w_N + e_2$
Coset leader	$e_3$	$w_2 + e_3$	...	$w_N + e_3$
	.	.	.	.
	.	.	.	.
	$e_u$	$w_2 + e_u$	...	$w_N + e_u$

In this array there are  $M$  rows and each row is a coset  $w$  denotes the codeword and  $e$  denotes the error in transmission. This criterion is used for each codeword to calculate the value. Finally the codeword with the minimum value is selected and then transformed to an OFDM signal by constellation mapping and IFFT. At the receiver, the received signal is converted into  $r$  by FFT and constellation de-mapping. The syndrome calculated from  $r$  is used for estimating the coset leader  $e$  chosen at the transmitter. The codeword  $c$  is obtained by calculating  $w = e+r$  and then is converted into a message sequence of  $k$  bits.

The block diagram is shown in Figure 2. Instead of using the modified SLM with IFFT, the proposed technique examines the performance enhancement of modified SLM with IDCT.

**3. MODIFIED SLM WITH INVERSE DISCRETE COSINE TRANSFORM**

OFDM system is employed considering orthogonal basis of complex exponential function set. But, OFDM can also be implemented using a single set of Cosinusoidal function as an orthogonal basis. This Cosinusoidal function is integrated along with a DCT, and hence this scheme is termed as DCT-OFDM and the output signal is given as, [2]

$$x(n) = \sqrt{\frac{2}{n}} \sum_{i=0}^{n-1} ds_i D_i \cos\left(\frac{i\pi n}{T_s}\right) \quad (18)$$

In equation (18)  $ds_0, ds_1, \dots, ds_{n-1}$  represent the independent data symbols that are attained as of a



modulation constellation.  $T_s$  symbolize the sampling interval.  $D_i$  takes the value as,

$$D_i = \begin{cases} 1/2 & i = 0 \\ 1 & i = 1, 2, \dots, n-1 \end{cases} \quad (19)$$

The system that uses modified SLM with Inverse Discrete Cosine Transform (IDCT) is picturized in Fig. 3.

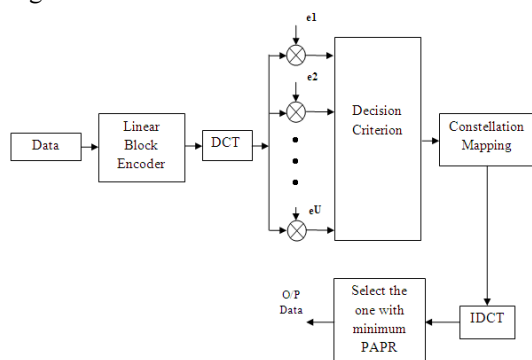


Figure 3: Modified SLM with IDCT

### 5. MODIFIED SLM WITH INVERSE DISCRETE SINE TRANSFORM (IDST)

The OFDM system can also be established via a single set of Sinusoidal functions as an orthogonal basis. This system is incorporated using a discrete Sine transform (DST). Therefore, this scheme is described as DST-OFDM scheme. According to this scheme the output signal can be elucidated as, [2]

$$x(n) = \sqrt{\frac{2}{n}} \sum_{i=0}^{n-1} ds_i D_i \sin\left(\frac{i\pi n}{T_s}\right) \quad (20)$$

The OFDM system that uses modified SLM with Inverse Discrete Sine Transform (IDST) is illustrated in figure-4

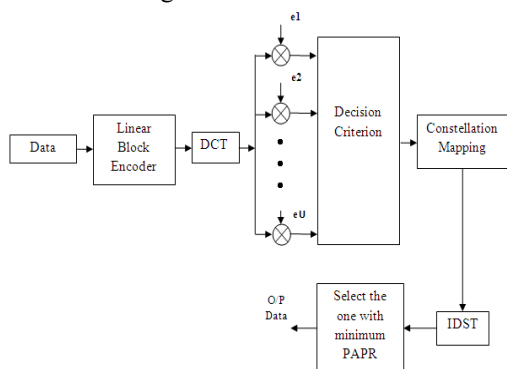


Figure 4: Modified SLM with IDCT

In this work, the data stream is transformed by DCT. It can linearly transform data into the frequency domain, where the data can be represented by a set of coefficients. The advantage of DCT is that the energy of the original data may be concentrated in only a few low frequency components of DCT depending on the correlation in the data. and then the transformed data is processed by the SLM unit where each data block is multiplied by  $C$  different number of phase sequence vectors.

If the data passed by DCT matrix before IDCT, the autocorrelation coefficient of IDCT input sequence is reduced with low complexity and no side information is required because the matrices can be generated to recover the original data at the receiver and the data is transmitted with lowest PAPR.

### 6. SIMULATION RESULTS AND DISCUSSION

The analysis of the modified SLM with DCT, IFFT, IDCT and IDST has been carried out using MATLAB software. The entire simulation parameters considered for this analysis is summarized in Table 1 as follows.

Table 2: Simulation parameters

Simulation parameter	Type/value
Number of subcarriers(N)	128,256,512,1024
Modulation Scheme	QAM
Phase weighting factor(e)	16,64
Coding technique	Linear block coding

In the OFDM System under consideration, modified SLM technique is applied to the uncoded information in the sub blocks, which is modulated by QAM modulation. The performance evaluation is done in terms of CCDF.

Fig. 5 shows the PAPR reduction performance using convention SLM method. In SLM the number of blocks present represents as the same information. As the number subblock (D) increases it is seen from the Fig.5 that the PAPR of the signal decreases from 9.6dB to 7.9dB.

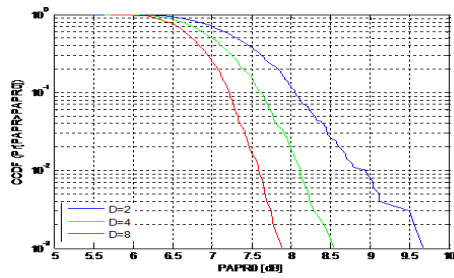


Figure 5: CCDF of PAPR of conventional SLM system

Figures 6, 7, 8 and 9 shows the performance of modified SLM with IFFT, IDCT and IDST for different subcarriers  $N=128, 256, 512$  and  $1024$ . It gives the better PAPR reduction at  $N=128$  compared to all other subcarriers. The Figure 6 shows the performance results of modified SLM with Linear coding for subcarrier when  $N=128$ . The graph shows the comparison of PAPR using three techniques IFFT= 4.1db, IDCT=2.3db and IDST=1.6db. From the result the performance of IDCT and IDST is improved when compared to IFFT. As the IDCT and IDST matrix are real and orthogonal. The symmetry of an orthogonal matrix indicates that algorithms for the forward and inverse transform computation will be the same. Hence it performs fast multiplication and reduces the complexity. The results of modified SLM with IFFT, modified SLM with IDCT and modified SLM with IDST are compared to find the best technique to obtain reduced PAPR OFDM system. It is observed that PAPR value is reduced using the proposed technique compared to existing technique.

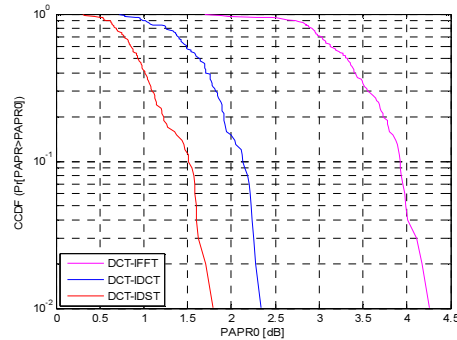


Figure 7: Comparison of CCDF of PAPR of OFDM system with modified SLM when  $N=256$

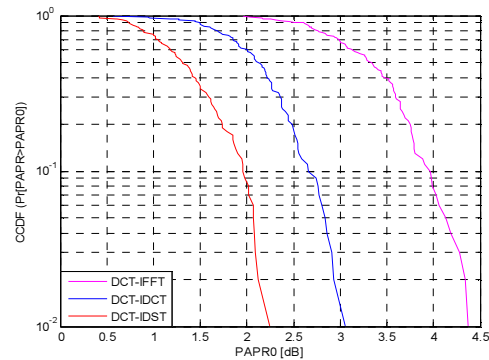


Figure 8: Comparison of PAPR of OFDM system with modified SLM when  $N=512$

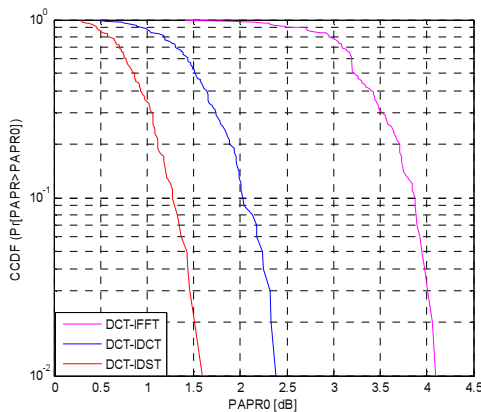


Figure 6: Comparison of CCDF of PAPR of OFDM system with modified SLM when  $N=128$

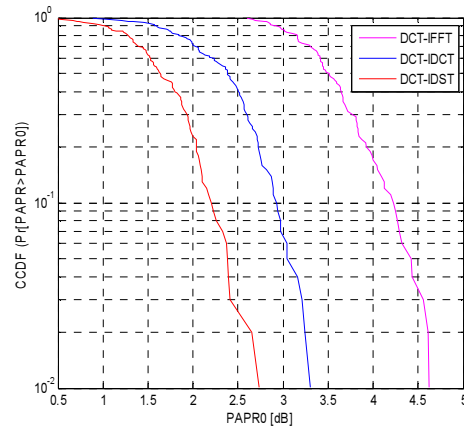


Figure 9: Comparison of PAPR of OFDM system with modified SLM when  $N=1024$

## 7. CONCLUSION

In this paper, PAPR analysis in DCT based OFDM is performed. This paper considered a Discrete

Cosine Transform (DCT) based modified Selective Level Mapping (SLM) as an effective technique to reduce Peak to Average Power Ratio (PAPR) in OFDM. In that, instead of using the modified SLM with Inverse Fast Fourier transform (IFFT), this technique examines the performance enhancement of modified SLM with Inverse Discrete Cosine Transform (IDCT) and Inverse Discrete Sine Transform (IDST). PAPR analysis is made using three techniques. The technique is simulated in MATLAB. Modified SLM technique with DCT improves the performance of OFDM signal with respect to PAPR. As there is an increasing demand for efficient frequency spectrum utilization, OFDM proves invaluable demand to next generation communication system.

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