



GLOWWORM SWARM OPTIMIZATION FOR OPTIMIZATION DISPATCHING SYSTEM OF PUBLIC TRANSIT VEHICLES

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ABSTRACT

The intelligent schedule of vehicles operation is one of the problems which need to be solved in the dispatching system of public transit vehicles, it relates to the development of the city and civic daily life. In this paper, a transit vehicle scheduling model which balancing between the benefits of bus companies and passengers is proposed. The glowworm swarm optimization (GSO) with random disturbance factor, namely R-GSO is applied to the schedule of vehicles. Comparing with classic swarm intelligence algorithms, the simulation results show our algorithm has higher efficiency and is an effective way to optimize the public transit vehicle dispatching.

Keywords: *Public Transit Vehicle Dispatching, Glowworm Swarm Optimization (GSO), Random Disturbance Factor.*

1. INTRODUCTION

The scheduling problem is a classical multi-objective optimization question and dispatching system of public transit vehicles' optimization is an actual problem [1]. To design the reasonable and convenient road network planning according to the urban traffic actual situation, work out the reasonable and effective urban public transport vehicle scheduling list considering social, bus company benefits. The current study of transit operation is divided into two methods. One is to adopt the simulation model, optimized the objective fitness function constructing by the simulation model. The other is to apply some operational research theory established the mathematical model, and then using intelligent algorithm to solve [2-5], [14-15]. Dispatching system of public transit vehicles is defined target for nonlinear optimization problem. It still has a lot of problems such as multi-objective function weights are difficult to be determined, the raw data source is not accurate, and the algorithm convergence is insufficient ideal, etc.

Glowworm swarm optimization (GSO) [6-10] is a new method of swarm intelligence based algorithm for optimizing multi-modal functions

proposed by Krishnanad K. N. and Ghose D. in 2005. This algorithm becomes a new research hotspot of computational intelligence draw our sights on it. With the research deeper and deeper, it's been used at noisy text of sensor and simulating robots. This paper introduces the basic GSO and glowworm swarm optimization with random disturbance factor, namely R-GSO, then applied them to the schedule of vehicles. The experimental results show that the improved algorithm can get better effect in the convergence and calculation.

This paper is organized as follows. In Section 2, a basic glowworm swarm optimization is proposed. In Section 3, we will introduce our glowworm swarm optimization with random disturbance factor for dispatching system of public transit vehicle, followed by the experimental results and analysis in Section 4. The conclusions are given in Section 5.

2. GLOWWORM SWARM OPTIMIZATION

In GSO, each glowworm distributes in the objective function definition space. These glowworms carry own luciferin respectively, and



has the respective field of vision scope called local decision range. Their brightness concerns with in the position of objective function value. The brighter the glow, the better is the position, namely has the good target value. The glow seeks for the neighbor set in the local-decision range, in the set, a brighter glow has a higher attraction to attract this glow toward this traverse, and the flight direction each time different will change along with the choice neighbor. Moreover, the local-decision range size will be influenced by the neighbor quantity, when the neighbor density will be low, glow's policy-making radius will enlarge favors seeks for more neighbors, otherwise, the policy-making radius reduces. Finally, the majority of glowworm return gathers at the multiple optima of the given objective function.

Each glowworm i encodes the object function value $J(x_i(t))$ at its current location $x_i(t)$ into a luciferin value $l_i(t)$ and broadcasts the same within its neighbourhood. The set of neighbours $N_i(t)$ of glowworm i consists of those glowworms that have a relatively higher luciferin value and that are located within a dynamic decision domain and updating by formula (1) at each iteration.

Local-decision range update:

$$r_d^i(t+1) = \min\{r_s, \max\{0, r_d^i(t) + \beta(n_t - |N_i(t)|)\}\} \quad (1)$$

where $r_d^i(t+1)$ is the glowworm i 's local-decision range at the $t+1$ iteration, r_s is the sensor range, n_t is the neighbourhood threshold, the parameter β affects the rate of change of the neighbourhood range.

The number of glow in local-decision range:

$$N_i(t) = \{j : \|x_j(t) - x_i(t)\| < r_d^i; l_i(t) < l_j(t)\} \quad (2)$$

where, $x_i(t)$ is the glowworm i 's position at the t iteration, $l_i(t)$ is the glowworm i 's luciferin at the t iteration.; the set of neighbours of glowworm i consists of those glowworms that have a relatively higher luciferin value and that are located within a dynamic decision domain whose range r_d^i is bounded above by a circular sensor range r_s ($0 < r_d^i < r_s$). Each glowworm i selects a

neighbour j with a probability $p_{ij}(t)$ and moves toward it. These movements that are based only on local information, enable the glowworms to partition into disjoint subgroups, exhibit a simultaneous taxis-behavior toward and eventually co-locate at the multiple optima of the given objective function.

Probability distribution selects a neighbour:

$$p_{ij}(t) = \frac{l_j(t) - l_i(t)}{\sum_{k \in N_i(t)} l_k(t) - l_i(t)} \quad (3)$$

Movement update:

$$x_i(t+1) = x_i(t) + s \left(\frac{x_j(t) - x_i(t)}{\|x_j(t) - x_i(t)\|} \right) \quad (4)$$

Luciferin-update:

$$l_i(t) = (1 - \rho)l_i(t-1) + \gamma J(x_i(t)) \quad (5)$$

and $l_i(t)$ is a luciferin value of glowworm i at the t iteration, $\rho \in (0,1)$ leads to the reflection of the cumulative goodness of the path followed by the glowworms in their current luciferin values, the parameter γ only scales the function fitness values, $J(x_i(t))$ is the value of test function.

Each glowworm i selects a neighbour j with a probability $p_{ij}(t)$ and moves toward it. These movements that are based only on local information, enable the glowworms to partition into disjoint subgroups, exhibit a simultaneous taxis-behaviour toward and eventually co-locate at the multiple optima of the given objective function.

The basic GSO algorithm as follows [6]:

Set number of dimensions = m ;

Set number of glowworms = n ;

Let s be the step size;

Let $x_i(t)$ be the location of glowworm i at time t ;

Deploy_agents_randomly;

For $i = 1$ to n do $l_i(0) = l_0$

$r_d^i(0) = r_o$

Set maximum iteration number = iter_max;

While ($t < \text{iter_max}$) do



```

{
For each glowworm  $i$  do :%Luciferin-update
    phase
     $l_i(t) = (1 - \rho)l_i(t-1) + \gamma J(x_i(t))$ ; %See(1)
For each glowworm  $i$  do : %Movement-phase
{
 $N_i(t) = \{j : d_{ij}(t) < r_d^i(t); l_i(t) < l_j(t)\}$ ;
For each glowworm  $j \in N_i(t)$  do;
 $p_{ij}(t) = \frac{l_j(t) - l_i(t)}{\sum_{k \in N_i(t)} l_k(t) - l_i(t)}$ ; %See(2)
 $j = \text{select\_glowworm}(\bar{p})$ ;
 $x_i(t+1) = x_i(t) + st * \left( \frac{x_j(t) - x_i(t)}{\|x_j(t) - x_i(t)\|} \right)$ ; %See(3)
 $r_d^i(t+1) = \min\{r_s, \max\{0, r_d^i(t) + \beta(n_t - |N_i(t)|)\}\}$ 
    % See(4)
}
     $t \leftarrow t + 1$ ;
}
    
```

Implementation at the GSO at the individual agent level gives rise to two major phases at the group level: Formation of dynamic networks that results in splitting of the swarm into sub-swarms and local convergence of glowworms in each subgroup to the peak locations.

3. PUBLIC TRANSIT VEHICLES DISPATCHING BY R-GSO

In order to avoid glowworm swarm optimization into the local optimal, give it the ability to expand the search scope, explore new areas. We insert the random disturbance factor at the movement update stage, and the formula as below:

$$x_i(t+1) = x_i(t) + s \left(\frac{x_j(t) - x_i(t)}{\|x_j(t) - x_i(t)\|} \right) + \sigma * randn \tag{6}$$

where $randn$ a random number in is $[-1,1]$, σ is the weighting factor of random disturbance.

In a public transport vehicle scheduling system [11], the bus route length is L having M bus stations. Bus companies operating time is $[time_m, time_n]$, and divided into K stages, the $k \in [1, K]$ interval is Δt_k . Suppose in the route of the public transport vehicles on the same model, running at the same rate, arrive on time, each station passengers to obey the uniformly distributed, the bus fare passengers each of the same. From two aspects, the bus company earnings and passengers waiting time, according to one day each site and operation conditions of the passenger flow, solving the route of the vehicle running schedule.

First consider the interests of the bus company, the goal is to make the bus company run number at least, that is the bus company total operating costs minimum. We conclude that the bus company profits objective function as follows:

$$f_1(\Delta t_k) = AL \sum_{k=1}^K \frac{T_k}{\Delta t_k} \tag{7}$$

where $\Delta t_k, k \in \{1, 2, \dots, K\}$, is the interval, T_k is the time length of k ; A is the bus cost per kilometer, L is the bus route length.

Then, from the point of view of passengers, make all the time, all passenger car minimum to ensure that the interests of the passengers, that is, the cost of car passengers loss minimum. We concluded that the cost of objective function passengers lost as follows:

$$f_2(\Delta t_k) = B \sum_{k=1}^K \sum_{j=1}^J m_k \left(\frac{\rho_{kj} \Delta t_k^2}{2} \right) \tag{8}$$

where $\Delta t_k, k \in \{1, 2, \dots, K\}$, is the interval, B is each passenger cost per minute for waiting, J is the total number of the stations $j \in \{1, 2, \dots, J\}$, where ρ_{kj} is the probability of passengers arriving at k time j station (supposing passenger arrives at the station obedience uniform distribution, $\frac{\Delta t_k}{2}$ is the average waiting time at k time), m_k is the total number of buses at k time.

Considered that the public transportation



company and the passenger both sides benefit, we establish the multi-objective functions to be as follows:

$$F(\Delta t_k) = \alpha f_1(\Delta t_k) + \beta f_2(\Delta t_k) \quad (9)$$

where α, β is the expense weighting factor of the bus companies and passengers. $\alpha + \beta = 1$. We will take $F(\Delta t_k)$'s value as the objective sufficiency in our algorithm.

4. EXPERIMENTAL RESULTS AND ANALYSIS

The algorithms are coded in MATLAB7.0 and implemented on Intel Core2 T5870 2.00GHz machine with 2G RAM under windows 7 platform.

Let $L = 8, M = 10$, bus companies operating time is 6:00~21:00. Entire day will divide according to the passenger flow into the early peak, the morning, afternoon, the late peak, the night 5 time intervals carries on the solution. The time interval concrete division is as follows: (6:00~8:30), (8:00~12:00), (12:00~16:00), (16:00~19:00), (19:00~21:00), concrete time interval number of passenger like Table 1. where, S represent station.

Table 1: Number of Passengers at Various Time Section and Various Stations

Time	S1	S2	S3	S4	S5
6:00~8:30	506	168	417	209	26
8:30~12:00	330	165	187	174	67
12:00~16:00	127	64	60	58	116
16:00~19:00	344	172	254	224	177
19:00~21:00	60	32	45	43	17

(Continued Table.1)

Time	S6	S7	S8	S9	S10
6:00~8:30	23	20	19	10	2
8:30~12:00	66	141	140	40	12
12:00~16:00	110	158	132	20	6
16:00~19:00	178	162	150	70	24
19:00~21:00	14	45	42	15	3

The set of R-GSO's parameters are as below: $n = 50$, max of iteration $\max t = 200$,

$\rho = 0.4$, $\gamma = 0.6$, $\beta = 0.08$, moving step $s = 0.03$, $n_i = 5$ and initialization of luciferin $l_0 = 5$, disturbing weight factor $\sigma = 2$. The expense of unit lose set $A = B = 1$. Carries on 10 times optimization tests in view of 3 kind of different parameter α, β establishments, compare with ASFA[12][13], PSO, GSO. In case 1, let $\alpha = 0.2, \beta = 0.8$, the operation result is $\min(F(\Delta t_k)) = 3419.6$, $\Delta t = (1, 3, 3, 1, 4)$ the unit is the minute. Optimized result comparison as Table 2, curves of the objective function value as Figure 1.

Table 2: When $\alpha = 0.2, \beta = 0.8$, optimized result comparison

Algorithm	Best value	Worst value	Average value
ASFA	6.5392414659e+003	8.0282100194e+003	7.9106708299e+003
PSO	5.0156880000e+003	6.9534666667e+003	6.0795177333e+003
GSO	5.1235200000e+003	8.9461725238e+003	7.5998462619e+004
R-GSO	3.4196000003e+003	4.5863950000e+003	3.8940825004e+003

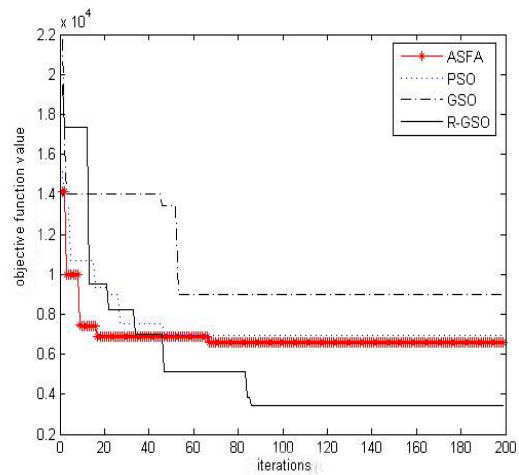


Figure 1: The curves of objective function value ($\alpha = 0.2, \beta = 0.8$)

In case 2, let $\alpha = 0.5, \beta = 0.5$, the operation result is $\min(F(\Delta t_k)) = 3893.40$, $\Delta t = (2, 4, 3, 3, 2)$ the unit is the minute. Optimized result comparison as Table 3, the curves of the objective function value as Figure 2.

Table 3: $\alpha = 0.5, \beta = 0.5$, Optimized Result Comparison

Algorithm	Best value	Worst value	Average value
ASFA	4.1531628190e+003	5.3329199363e+003	4.7430413776e+003
PSO	4.3350000000e+003	6.4919377976e+003	5.4134688988e+003
GSO	5.1012500000e+003	9.9330857142e+003	7.5171678571e+003
R-GSO	3.8929999999e+003	4.3030500000e+003	3.9880250000e+003

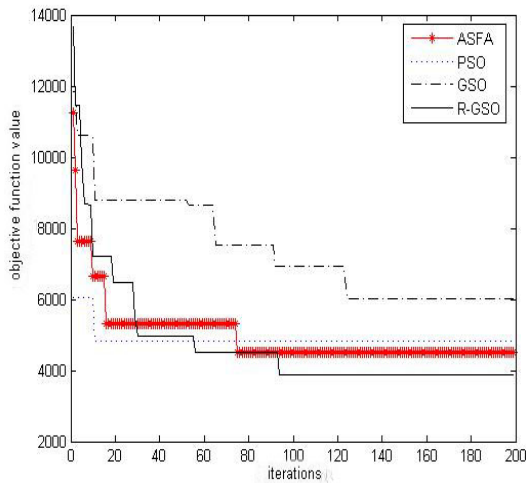


Figure 2: The Curves Of Objective Function Value ($\alpha = 0.5, \beta = 0.5$)

In case 3, when $\alpha = 0.8, \beta = 0.2$ the operation result is $\min(F(\Delta t_k)) = 4946$, $\Delta t = (3, 2, 5, 1, 14)$ the unit is the minute. Optimized result comparison as Table 4, curves of the objective function value as Figure 3.

Table 4: When $\alpha = 0.2, \beta = 0.8$ optimized result comparison

Algorithm	Best value	Worst value	Average value
ASFA	6.0764312047e+003	7.2334575519e+003	6.6549443783e+003
PSO	6.3720819999e+003	8.8179683333e+003	7.5950251666e+003
GSO	8.1924999999e+003	9.9124562857e+003	8.5524781428e+003
R-GSO	4.9459999999e+003	5.0541999999e+003	4.9824443809e+003

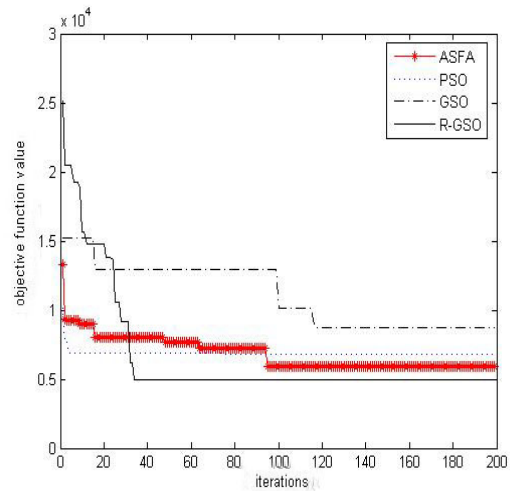


Figure 3: The Curves Of Objective Function Value ($\alpha = 0.8, \beta = 0.2$)

Looking from the simulation result, in the early peak and in the late peak time interval, the computed result departure frequency is also high, tallies with the daily life situation. The weight value α, β has certain influence to the experimental result, but no matter in situation 1, 2 or 3 R-GSO all can make the good progress. In practical life application, the weight value α, β , is decided with policy-maker's tendency direction.

5. CONCLUSIONS

This article proposed glowworm swarm optimization with random disturbance factor, namely R-GSO and applied it into public. Has carried on the comparative analysis in the simulation experiment with ASFA, PSO and GSO,



R-GSO has obtained the good result in the convergence rate and the computational accuracy aspect. Calculated that machine the simulation experiment showed that this article proposed the algorithm can the effective application in the urban public transportation dispatching system, to manage solves public transit vehicles dispatching problem with the policy-maker to have the reference value.

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