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WORKSPACE AND SINGULARITY ANALYSIS OF 3/3-RRRS PARALLEL MANIPULATOR

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ABSTRACT

The workspace of manipulator can be defined as the operational area of the end effector. Because the moving platform of the parallel manipulator with six degree-of-freedom have six independence movement(movement in any direction and rotation around any direction), it means the workspace has six-dimensional, the six-dimensional workspace is difficult to be directly calculate and unable to graphic description. For the project of this article-3/3-RRRS parallel manipulator, this article will analyze the workspace of the manipulator in two cases. A discretization method is proposed for the computation of the reachable position/orientation workspace of the 3/3-RRRS parallel manipulator, respectively. Four examples of a 3/3-RRRS parallel manipulator are given to demonstrate these theoretical results; change rules are discussed in detail. As a special position and inherent attributes of the mechanism, singularity has a serious impact on the mechanism's motion control performance and drive performance. The method of searching algorithm in three-dimensional space is applied to the singularity analysis, coordinate of all possible stable positions are substituting into the Jacobian, position-singular points under given orientation condition are conformed.

Keywords: 3/3-RRRS Parallel Manipulator, Workspace Analysis, Singularity Analysis

1. INTRODUCTION

The size and shape of the workspace is an important index to measure the performance of the mechanism and the important process of the end effector's design [1]. And as a special position and inherent attributes of the mechanism, singularity has a serious impact on the mechanism's motion control performance and drive performance. Much work has been done at home and abroad during these years.

In terms of the application of numerical method, Fichter fixed three orientation parameters in six location parameters and a position parameter of the parallel manipulator and set the remaining two position parameters as variables. Then the numerical method is applied to the study of the workspace of six degree-of-freedom Stewart parallel manipulator [2]. Gosselin chooses to fix the orientation parameters of the parallel manipulator moving platform and use approach of arc intersects to determine the position workspace of the six degree-of-freedom parallel manipulator. Since the purpose of approach is solve the boundary of the workspace, the scanning is efficient and the volume of workspace can be work out[3]. Similarly, Harbin Institute of Technology, Professor Chen applied the

genetic algorithm to the problem of solving process of the six degree-of-freedom space parallel robot manipulator[4]. Hunt and Fichter first use the screw theory to analyze the singularity of two different types of Steward parallel manipulator [5] and so on[6-10].

2. WORKSPACE ANALYSIS OF 3/3-RRRS PARALLEL MANIPULATOR

3/3-RRRS parallel manipulator is a new type of realizing arbitrary three-dimensional spatial motion of the parallel manipulator. The manipulator consists of a moving platform and fixed platform as well as three completely identical branched chains, among them, both the moving platform and fixed platform are equilateral triangle, P is the centroid of the moving platform, O is the centroid of the fixed platform; Between the moving and fixed platform the three branched chain by A_iB_i , B_iC_i , C_iD_i (i=1 2 3) respectively in turn are connected together, between the fixed platform and A_iB_i, A_iB_i and B_iC_i , B_iC_i and C_iD_i , the connection of rotation pair; S_{i1},, S_{i2}, S_{i3} the rotation axis respectively, between C_iD_i and the moving platform the connection of spherical hinge pair, S_{i4}, S_{i5}, S_{i6} the rotation axis (see 3/3-RRRS parallel manipulator structure figure 1).

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Branched chain $A_iB_iC_iD_i$ are always whole rotation in the same plane round the rotation pair at the point A_i , the angle between centroid in moving and fixed platform and vertex ligature PD_i as well as OA_i , is 120° mutually and respectively.

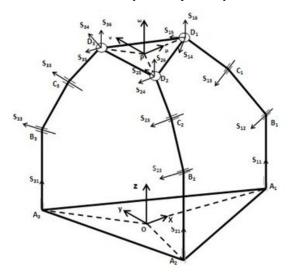


Figure 1 3/3-RRRS Parallel Manipulator Structure
Diagram

3. THE INFLUENCING FACTORS OF THE WORKSPACE

The constraint of drive rotation angle directly affects the workspace of the manipulator. The six revolute joint in A_i and B_i serve as drive pair of the 3/3-RRRS parallel manipulator. Constituting the links of each of the drive pairs A_iB_i and B_iC_i are the crankshaft type structure. So that the range of the rotation angle of the drive pairs can be expanded. So, in the solving process of workspace, define range of the rotation angle of six drive pairs γ_i , α_i and constraint as follow:

$$\gamma_{\text{imin}} \le \gamma_{\text{i}} \le \gamma_{\text{imax}}, \alpha_{\text{imin}} \le \alpha_{\text{i}} \le \alpha_{\text{imax}}$$
 (1)

In the formula γ_{imin} , γ_{imax} and α_{imin} , α_{imax} are given limit angle in engineering practice.

Set the vector $\,$ as the direction vector which is a vertical plane of the moving platform, to indicate the vector about Euler angles $\eta, \, \phi$ and δ of the moving platform location:

$$\overline{Nvp} = \begin{pmatrix} \sin\delta \cdot \sin\eta + \cos\delta \cdot \cos\eta \cdot \cos\phi \\ -\sin\delta \cdot \cos\eta + \cos\delta \cdot \sin\eta \cdot \sin\phi \\ \cos\delta \cdot \cos\phi \end{pmatrix}^{T}$$
(2)

According to the geometry relationship, rotation angle β_i of the spherical hinge is:

$$\beta_i = a\cos(\det(\overrightarrow{Nvp}, \overrightarrow{C_iD_i}) / norm(\overrightarrow{C_iD_i}))$$
 (3)

In the equation, dot, acos and norm are all function language of MATLAB. dot indicates dot product between vector \overline{Nvp} and vector $\overline{C_iD_i}$ acos indicates to return to the arccosine. norm indicates the modulus of the vector $\overline{C_iD_i}$.

Then the spherical hinge should meet the follow constraints:

$$\beta_{\text{imin}} \le \beta_{\text{i}} \le \beta_{\text{imax}} \tag{4}$$

In the formula, β_{imin} , β_{imax} are the limiting rotation angle given for engineering practice.

According to the kinematics analysis of 3/3-RRRS parallel manipulator, the manipulator structure parameters has little influence to drive. It's not the emphasis.

4. THE SOLVING METHOD OF THE WORKSPACE

By the symbolic solution of location inverse solution, we can obtain the drive joint variables corresponding to the output location of the moving platform quickly. And judge the obtained joint variables with the constrains to search out the manipulator's workspace boundary. It means that we can obtain the drive input $\alpha_i(\alpha_i)$ has two solution), $\gamma_i(i=1\ 2\ 3)$ what the point P's position variables a, b, c and orientation variable η, ϕ, δ on the moving platform is homologous by position inverse solution. The location point can be judged whether it belong to the workspace by judging whether $\alpha_i, \gamma_i, \beta_i$ consistent with the constrains of formula 1 and 4 at the same time.

The three-dimensional limit boundary of the parallel manipulator workspace searching shows follow:

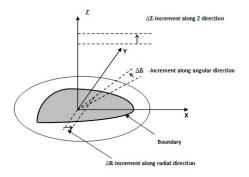


Figure 2 Workspace Limit Boundary Searching Diagram

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5. SOLVING THE POSITION WORKSPACE

Set the structural parameters of the manipulator as: the circumcircle radius of the fixed platform R=200mm, the circumcircle radius of the moving platform r=200mm. The length of each links are: $\left|A_{i}B_{i}\right|=200mm \quad , \quad \left|B_{i}C_{i}\right|=150mm \quad , \quad \left|C_{i}D_{i}\right|=100mm \quad .$ Set the solid league coordinate system origin P on the moving coordinate system as the research object, and the position coordinates of the point P meets the equation 5:

$$\begin{cases}
X=R_1 \cdot \cos \sigma \\
Y=R_1 \cdot \sin \sigma \\
Z=Z
\end{cases}$$
(5)

In the equation, R_1 , α , Z are respectively inner loop variables, middle loop variable and outer loop variable of the three-dimensional search.

6. POSITION WORKSPACE EXAMPLES

The accuracy and efficiency of workspace three-dimensional search greatly depend on the calculated step value. In order to obtain the position workspace of the 3/3-RRRS parallel manipulator quickly and effectively and ensure the accuracy of the position workspace, we set the steps respectively as ΔR_1 =1mm, $\Delta \alpha$ =3°, ΔZ =1mm. Might given to a group of moving platform orientation: η =0, φ =0, δ =0.

We propose two groups of range of the rotation angle of the drive angle.

The first group: $-\pi/4 \le \gamma_1 \le \pi/4$, $-7\pi/16 \le \gamma_2 \le 9\pi/16$, $-\pi/8 \le \gamma_3 \le 7\pi/16$; $-5\pi/8 \le \alpha_1 \le 5\pi/8$, $-5\pi/8 \le \alpha_2 \le 5\pi/8$, $-5\pi/8 \le \alpha_3 \le 5\pi/8$; $\beta_1 \le 3\pi/10$, $\beta_2 \le 3\pi/10$, $\beta_3 \le 3\pi/10$

And the second group is: $-3\pi/4 \le \gamma_1 \le 3\pi/4$, $-3\pi/4 \le \gamma_2 \le 3\pi/4$, $-3\pi/4 \le \gamma_3 \le 3\pi/4$, $-3\pi/4 \le \alpha_1 \le 3\pi/4$, $-3\pi/4 \le \alpha_2 \le 3\pi/4$, $-3\pi/4 \le \alpha_3 \le 3\pi/4$, $\beta_1 \le 7\pi/20$, $\beta_2 \le 7\pi/20$, $\beta_3 \le 7\pi/20$.

According to the above parameters and constraint conditions, using three-dimensional limit boundary search method, we can get the three-dimensional boundary contour figure of the manipulator position workspace. Shown as figure 3 and 4:

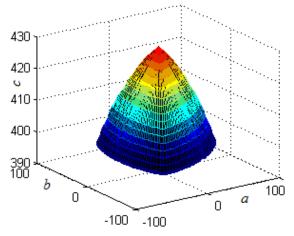


Figure 3 Position-Workspace Under The Constraints Of First Group

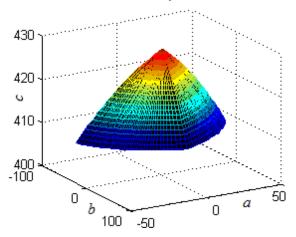


Figure 4 Position-Workspace Under The Constraints Of Second Group

7. SOLVING THE ORIENTATION WORKSPACE

Keeping the manipulator's structure parameters accordance with former article, set the solid league coordinate system origin P on the moving coordinate system as the research object, and the position coordinates of the point P meets the equation 6:

$$\begin{cases}
\eta = R_1 \cdot \cos \sigma \\
\varphi = R_1 \cdot \sin \sigma \\
\delta = \delta
\end{cases} \tag{6}$$

In the equation, R_1 , α , Z are respectively inner loop variables, middle loop variable and outer loop variable of the three-dimensional search.

As well, in order to obtain the orientation workspace of the 3/3-RRRS parallel manipulator quickly and effectively and ensure the accuracy of

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the orientation workspace, we set the steps respectively as $\Delta R_1 = 0.001$ mm, $\Delta \alpha = 3^{\circ}$, $\Delta \delta = \pi/360$.

8. ORIENTATION WORKSPACE EXAMPLES

We propose two groups of the workspace and range of the rotation angle of the drive angle as follow:

The third group: the moving platform location: a=0,b=0,c=410. The range of the rotation angle of the drive angle: $-\pi/4 \le \gamma_1 \le 3\pi/4$, $\pi/12 \le \gamma_2 \le 7\pi/12$, $5\pi/12 \le \gamma_3 \le 11\pi/12$, $-3\pi/4 \le \alpha_1 \le 5\pi/8$, $-3\pi/4 \le \alpha_2 \le 3\pi/4$, $-3\pi/4 \le \alpha_3 \le 3\pi/4$, $\beta_1 \le 7\pi/20$, $\beta_2 \le 7\pi/20$, $\beta_3 \le 7\pi/20$

The fourth group: the moving platform location: a=0,b=0,c=415. The range of the rotation angle of the drive angle: $-\pi/4 \le \gamma_1 \le \pi/4$, $\pi/8 \le \gamma_2 \le 7\pi/12$, $-\pi/8 \le \gamma_3 \le 5\pi/12$, $-5\pi/8 \le \alpha_1 \le 5\pi/8$, $-5\pi/8 \le \alpha_2 \le 5\pi/8$, $-5\pi/8 \le \alpha_3 \le 5\pi/8$, $\beta_1 \le 3\pi/10$, $\beta_2 \le 3\pi/10$, $\beta_3 \le 3\pi/10$

According to the above parameters and constraint conditions, using three-dimensional limit boundary search method, we can get the three-dimensional boundary contour figure of the manipulator orientation workspace. Shown as figure 5 and 6:

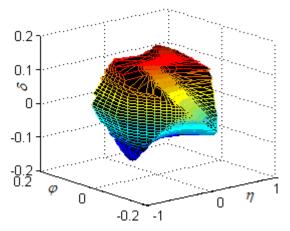


Figure 5 Orientation-Workspace Under The Constraints Of The Third Group

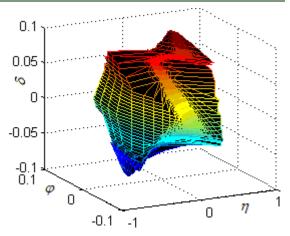


Figure 6 Orientation-Workspace Under The Constraints Of The Fourth Group

9. SINGULARITY ANALYSIS OF THE 3/3-RRRS PARALLEL MANIPULATOR

In this paper, on the basis of the kinematics analysis, according kinematics equals of the manipulator, we try to obtain Jacobian matrix's symbolic expressions about the six moving platform location parameters. Using the three-dimensional point searching method, traverse three-dimensional space completely covered by the functional requirements of the decision of all task trajectory point, obtain Jacobian matrix singular point, under the conditions of the given moving platform orientation, and draw out all the singular point in the MATLAB work environment.

As the description above, the drive input of the 3/3-RRRS parallel manipulator are α_i , γ_i (i=1 2 3). The motion parameters of the moving platform include positional parameters a,b,c, and orientation parameters η , φ , δ . These parameters are functions of time t. In the 3/3-RRRS parallel manipulator, according to the geometry relationship, there is:

Link length constraint equation:

$$\left|\overline{C_iD_i}\right|^2 = L_{2i}^2 \tag{7}$$

Two vector vertical equation:

$$\overline{C_iD_i} \cdot (\cos\gamma_i, \sin\gamma_i, 0) = 0$$
 (8)

Where in the coordinates of each of the hinge point D_i in the fixed coordinate system O-xyz can be expressed as D_i : $(D_{iX},\,D_{iY},\,D_{iZ})$. Vector $(cos\gamma_i\,sin\gamma_i\,$,0) is the vertical vector about plane $A_iB_iC_iD_i.$

Might set:

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$$f_{i} = \left| \overline{C_{i}} \overline{D_{i}} \right|^{2} - L_{2i}^{2}$$

$$(9)$$

$$F_{i} = \overline{C_{i}} \overline{D_{i}} \cdot (\cos \gamma_{i}, \sin \gamma_{i}, 0)$$

$$(10)$$

Taking the partial derivative of the equation 9 and 10 with respect to time t and transpose, we can obtain the equation 11 and 12:

$$\frac{\partial f_{i}}{\partial a} a' + \frac{\partial f_{i}}{\partial b} b' + \frac{\partial f_{i}}{\partial c} c' + \frac{\partial f_{i}}{\partial \eta} \eta' + \frac{\partial f_{i}}{\partial \phi} \phi' + \frac{\partial f_{i}}{\partial \delta} \delta'$$

$$= -\left(\frac{\partial f_{i}}{\partial \alpha_{i}} \alpha_{i}' + \frac{\partial f_{i}}{\partial \gamma_{i}} \gamma_{i}'\right)$$
(11)
$$\frac{\partial F_{i}}{\partial a} a' + \frac{\partial F_{i}}{\partial b} b' + \frac{\partial F_{i}}{\partial c} c' + \frac{\partial F_{i}}{\partial \eta} \eta' + \frac{\partial F_{i}}{\partial \phi} \phi' + \frac{\partial F_{i}}{\partial \delta} \delta'$$

$$= -\left(\frac{\partial F_{i}}{\partial \alpha_{i}} \alpha_{i}' + \frac{\partial F_{i}}{\partial \phi} \gamma_{i}'\right)$$

(12)

Put the velocity equations of all three branch chains on the 3/3-RRRS parallel manipulator together, written in matrix form, there is equation 13:

$$\begin{pmatrix} \partial_a f_1 & \partial_b f_1 & \partial_c f_1 & \partial_\eta f_1 & \partial_\varphi f_1 & \partial_\delta f_1 \\ \partial_a F_1 & \partial_b F_1 & \partial_c F_1 & \partial_\eta F_1 & \partial_\varphi F_1 & \partial_\delta F_1 \\ \partial_a f_2 & \partial_b f_2 & \partial_c f_2 & \partial_\eta f_2 & \partial_\varphi f_2 & \partial_\delta f_2 \\ \partial_a F_2 & \partial_b F_2 & \partial_c F_2 & \partial_\eta F_2 & \partial_\varphi F_2 & \partial_\delta F_2 \\ \partial_a f_3 & \partial_b f_3 & \partial_c f_3 & \partial_\eta f_3 & \partial_\varphi f_3 & \partial_\delta f_3 \\ \partial_a F_3 & \partial_b F_3 & \partial_c F_3 & \partial_\eta F_3 & \partial_\varphi F_3 & \partial_\delta F_3 \end{pmatrix} \begin{pmatrix} a' \\ b' \\ \eta' \\ \phi' \\ \delta_a F_3 & \partial_b F_3 & \partial_c F_3 & \partial_\eta F_3 & \partial_\varphi F_3 & \partial_\delta F_3 \end{pmatrix} \begin{pmatrix} a' \\ b' \\ \eta' \\ \phi' \\ \delta' \end{pmatrix}$$

$$= - \begin{pmatrix} \partial_{\alpha_{1}} f_{1} & \partial_{\gamma_{1}} f_{1} & 0 & 0 & 0 & 0 \\ \partial_{\alpha_{1}} F_{1} & \partial_{\gamma_{1}} F_{1} & 0 & 0 & 0 & 0 \\ 0 & 0 & \partial_{\alpha_{2}} f_{2} & \partial_{\gamma_{2}} f_{2} & 0 & 0 \\ 0 & 0 & \partial_{\alpha_{2}} F_{2} & \partial_{\gamma_{2}} F_{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & \partial_{\alpha_{3}} f_{3} & \partial_{\gamma_{3}} f_{3} \\ 0 & 0 & 0 & 0 & \partial_{\alpha_{3}} F_{3} & \partial_{\gamma_{3}} F_{3} \end{pmatrix} \begin{pmatrix} \alpha_{1} \\ \gamma_{1} \\ \alpha_{2} \\ \gamma_{2} \\ \alpha_{3} \\ \gamma_{3} \end{pmatrix}$$

$$(13)$$

For convenience of description, might set:

$$\begin{split} \left[\mathbf{P}\right] = \begin{pmatrix} \partial_{a}f_{1} & \partial_{b}f_{1} & \partial_{c}f_{1} & \partial_{\eta}f_{1} & \partial_{\varphi}f_{1} & \partial_{\delta}f_{1} \\ \partial_{a}F_{1} & \partial_{b}F_{1} & \partial_{c}F_{1} & \partial_{\eta}F_{1} & \partial_{\varphi}F_{1} & \partial_{\delta}F_{1} \\ \partial_{a}f_{2} & \partial_{b}f_{2} & \partial_{c}f_{2} & \partial_{\eta}f_{2} & \partial_{\varphi}f_{2} & \partial_{\delta}f_{2} \\ \partial_{a}F_{2} & \partial_{b}F_{2} & \partial_{c}F_{2} & \partial_{\eta}F_{2} & \partial_{\varphi}F_{2} & \partial_{\delta}F_{2} \\ \partial_{a}f_{3} & \partial_{b}f_{3} & \partial_{c}f_{3} & \partial_{\eta}f_{3} & \partial_{\varphi}f_{3} & \partial_{\delta}f_{3} \\ \partial_{a}F_{3} & \partial_{b}F_{3} & \partial_{c}F_{3} & \partial_{\eta}F_{3} & \partial_{\varphi}F_{3} & \partial_{\delta}F_{3} \end{pmatrix} \end{split}$$

$$\begin{split} \left[Q\right] = \begin{pmatrix} \partial_{\alpha_{l}}f_{l} & \partial_{\gamma_{l}}f_{l} & 0 & 0 & 0 & 0 \\ \partial_{\alpha_{l}}F_{l} & \partial_{\gamma_{l}}F_{l} & 0 & 0 & 0 & 0 \\ 0 & 0 & \partial_{\alpha_{2}}f_{2} & \partial_{\gamma_{2}}f_{2} & 0 & 0 \\ 0 & 0 & \partial_{\alpha_{2}}F_{2} & \partial_{\gamma_{2}}F_{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & \partial_{\alpha_{3}}f_{3} & \partial_{\gamma_{3}}f_{3} \\ 0 & 0 & 0 & 0 & \partial_{\alpha_{3}}F_{3} & \partial_{\gamma_{3}}F_{3} \end{pmatrix} \end{split}$$

Then [P],[Q] are called Jacobian matrix of this manipulator. Therefore, the equation 13 can also be written as follows:

$$\begin{bmatrix} P \end{bmatrix} \begin{pmatrix} a' \\ b' \\ c' \\ \eta' \\ \phi' \\ \delta' \end{pmatrix} = - \begin{bmatrix} Q \end{bmatrix} \begin{pmatrix} \alpha_1' \\ \gamma_1' \\ \alpha_2' \\ \gamma_2' \\ \alpha_3' \\ \gamma_3' \end{pmatrix}$$

(16)

According to equation 16, we can define two types of singular points as follows:

The first kind of singular point: the point of meeting Det(P)=0 and $Det(Q)\neq 0$.

The second kind of singular point: the point of meeting Det(Q)=0 and $Det(P)\neq 0$.

10. SOLVING THE SINGULARITY

The solution process of singular configuration will be based on kinematics inverse solution and manipulator geometry relations, using the method of three-dimensional search, search method is shown in Figure 2. Similarly, since the taken step size of the calculate will decide whether all the singular points can be searched, in order to quickly and effectively obtain all singular points of the 3/3-RRRS parallel manipulator, might set the step as: ΔR_1 =0.01mm , $\Delta \alpha$ =3°, ΔZ =1mm.

In order to maintain the continuity of analysis of the 3/3-RRRS parallel manipulator, we might still

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set the manipulator structure parameters as above. And set the moving platform orientation η =0, ϕ =0, δ =0.

11. SOLVE THE FIRST KIND SINGULAR POINTS

By kinematics inverse solution, every group moving platform location corresponds to one group γ_i and eight groups α_i . That is, there are eight groups C_i coordinate combination. So according to the eight groups different C_i coordinate combination, we need to obtain eight different corresponding Jacobian matrixes, and work out the value of the corresponding Jacobian matrix's determinant. The obtained points which make Det(P)=0 are all singular points. The first kind singular points figure in 3/3-RRRS parallel manipulator is shown as figure 7:

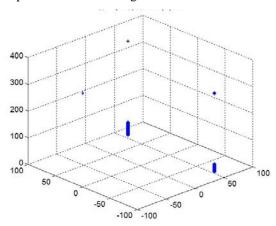


Figure 7 The First Kind Singular Points

Easy to know, each singular points above is not in the position workspace which is determined by the condition of the moving platform orientation η =0, φ =0, δ =0.

12. SOLVE THE SECOND KIND SINGULAR POINTS

Similar to the solving process of the first singular points, the position output value of the moving platform need to plugged in eight different Jacobian matrixes. The obtained points which make Det(Q)=0 are all singular points. The number of the second singular point of the 3/3-RRRS parallel manipulator is zero by solving.

We know, through the analysis of the singular figure in example, that almost all the corresponding singular points under the condition of the moving platform orientation η =0, ϕ =0, δ =0 are below the height of 100mm in the 3/3-RRRS parallel

manipulator. And the two straight lines formed by these points are both parallel to the Z axis, and these points are all not in the corresponding space of the orientation. Therefore, the workspace in the condition of meeting the preset constraints is the final actual workspace.

SUMMARY

This paper mainly analyses the workspace and singularity of the 3/3-RRRS parallel manipulator. In the different conditions of a given position and orientation, according to the different actuator angle constraint and other structural constraints, this paper has successfully solved the workspace figures having a certain geometry of the three-dimensional space. At the same time, all the singular point is obtained in this orientation, and shown in the three-dimensional figure.

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REFRENCES:

- [1] Anjan K D, Chen I-Ming, Song H Y. "Workspace generation and planning singularity-free path for parallel manipulators", *Mechanism and Machine Theory*, Vol. 40, No. 1, 2005, pp. 776-805.
- [2] Fichter E F. "A Stewart Platform-Based Manipulator: General Theory and Practical Construction", *The International Journal of Robots Research*, Vol. 5, No. 2, 2006, pp. 157-182.
- [3] Gosselin C M, Lavoie E. Toutant P. "Robotics Spatial Mechanisms and Mechanical systems", *Journal of Applied Mechanics*, Vol. 45, No. 1, 2002, pp. 323-328.
- [4] Z. L. Chen, X. S. Chen, T. Xie. "Solve the synthesis problem of the given workspace by Genetic Algorithm", *Chinese Mechanical Engineering*, Vol. 13, No. 3, 2002, pp. 187-190.

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- [5] Hunt K H, Primrose E J E. "Assemble configurations of some in parallel-actuated manipulators", *Mach Mech Theory*, Vol. 28, No. 1, 2003, pp. 31-42.
- [6] Yi Cao, Zhen Huang, Hui Zhou, Weixi Ji. "Orientation-Workspace Analysis of a Special Class of the Stewart-Gough Parallel Manipulators", *Robotica*, Vol. 28, No. 7, 2010, pp. 989-1000.
- [7] Yi Cao, Zhen Huang, Qiuju Zhang, Hui Zhou. "Orientation-Singularity and Nonsingular Orientation-Workspace Analysis of the Semi-Regular Stewart-Gough Platform Manipulator", *Advanced Robotics*, Vol. 24, No. 15, 2010, pp. 2119-2135.
- [8] Stewart D. "A Platform with six degrees of freedom", Proceedings of the Institution of Mechanical Engineers, Part A: Journal of Power and Energy, Vol. 180, No. 15, 1995, pp. 371-386
- [9] Chan Wing, Yan Jing. "Homotopy iteration method and applied to the positive position of the general 6-SPS parallel robot mechanism", *Mechanical Science and Technology*, Vol. 12, No. 2, 2007, pp. 404-422.
- [10] Yi Cao, Hui Zhou, Weixi Ji, Qiuju Zhang, Baokun Li. "Singularity Kinematics Principle and Position-Singularity Analyses of the 6-3 Stewart-Gough Parallel Manipulators". *Journal of Mechanical Science and Technology*, Vol. 25, No. 2, 2011, pp. 513-522.
- [11] Yi Cao, Hui Zhou, Qiuju Zhang, Weixi Ji. "The Research on Orientation-Singularity and Orientation-Workspace of a Class of the Stewart-Gough Parallel Manipulators". Proceedings of the Institution of Mechanical Engineers, Part K: Journal of Multi-Body Dynamics, Vol. 224, No. 1, 2010, pp. 19-32.