



MULTI-METHOD INTEGRATED ON SOC ESTIMATION OF LI-ION BATTERY

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ABSTRACT

The Li-ion battery is studied base on its equivalent circuit model. The discrete state space equation is established using Ah counting method and OCV method. The filtering algorithm is set up under the noisy environments according to the principle of extended Kalman filter and simulated. The simulation results showed that the integrated of three algorithms could very well remove the environments noise, so the accurate estimate of Li-ion battery SOC value can be gained.

Keywords: *Li-ion battery, SOC estimation, Ah counting method, OCV method; EKF*

1. INTRODUCTION

State of charge (SOC) is defined as the ratio between the stored energy available and the energy available in a fully charged state. SOC estimation correctly can not only avoid the danger of over-charging or over-discharging which may damage the battery but also provide the strategy for vehicle control to use the battery energy reasonable. So that the electric vehicles (EV) can control and predict the driving range effectively and ultimately achieve the purpose of energy saving, environmental protection, and to extend the life of the battery pack.

SOC value can't be measured directly. But it can be estimated by some physical characteristics like terminal voltage, current, temperature etc. combining with battery external characteristic and working status. The estimation precision is influenced by voltage, charge-discharge rate, power, temperature, cycle life, internal resistance, the internal pressure, self-discharge rate, etc. Environmental noise can't be ignored.

The main method of battery SOC estimation includes discharge experiment method, ampere-hour (Ah) counting method, open circuit voltage (OCV) method, load voltage method, electrochemical impedance spectrum method, the internal resistance method, the linear model method, neural network method and Kalman filter(KF) method. The discharge experiment method is the most reliable method, however battery should be stop working for experiment. So

it is only suitable for cell maintenance. The OCV method is very accurate, but it needs a rest time to estimate the SOC and thus cannot be used in real time. Ah counting method is a kind of open-loop test, which is simple and easy to utilize. It can be used in real time, however it is so sensitive to external interference that an initial value error and accumulated error will increases by time. Load voltage method, electrochemical impedance spectrum method, the internal resistance method is only suitable for low SOC estimation because it is too sensitive to environment noise. The neural network method and KF method requires a suitable battery math model, it is difficult to determine the internal parameters [1-4].

In this study, the Li-ion battery is for research. The battery equivalent circuit model was set up. According to the equivalent model, the state-space equations are used to describe the system performance. And then, three method, Ah counting method, OCV method, extended Kalman filter (EKF) method, are integrated to be a kind of new algorithm which is used to estimate the battery SOC in noisy environments. Finally, the simulation is conducted for verification.

1. PROPOSED APPROACH

1.1 AH Counting Method

Ah counting, which is the most common method of battery SOC estimation, is easy and reliable. It is actually a method based on the principle of the "black box", the battery is seen as

a “black box”, by integrating the current flows into and out of the battery, the change of the battery charge can be gained. So it is unnecessary to consider the battery internal state of the change or other factors. In this case, at every instant of time, the SOC would be equal to:

$$SOC(t_k) = SOC(t_0) + \int_{t_0}^{t_k} \frac{\eta i(t)}{C_0} dt \quad (1)$$

Where $SOC(t_0)$ is supposed the initial state of charge, $SOC(t_k)$ is SOC at t_k times, $i(t)$ is the battery current, η is the efficiency of charge or discharge, C_0 is the battery rated capacity.

As the equation (1) shows, the initial condition for the SOC can't be determined from the integration of the current, therefore, $SOC(t_0)$ should be confirmed using other method. The other disadvantage is that the measurement of the current can be affected by noisy environment. When the current signal is sampled, thereby introducing discretization errors [3].

1.2. OCV Method

The open circuit voltage is defined as the voltage measured at the battery terminals when no load is applied and all internal processes are completely relaxed. It is equal to the electromotive force of the battery under the conditions of long standing. Meanwhile, the electromotive force of the battery has a relatively fixed functional relationship with SOC, so it can be estimated based on the open-circuit voltage.

$$U_{ocv} = f(SOC) \quad (2)$$

Where U_{ocv} is open circuit voltage.

The functional relationship of the U_{ocv} -SOC is obtained by measuring the open-circuit voltage at each SOC. The relationship cannot be exactly the same for every battery. Thus, the use of the relationship among batteries may cause an unacceptable error in the SOC estimation [1].

1.3. EKF Method

KF is an optimal recursive data processing algorithm. It is applied to the linear system with the noise statistical properties been known. Using recursive iterative algorithm and having no requirement in system signal' stability and time invariance, KF is the most efficient and effective method to many problems. After linearization, KF is also used to recursive calculation to nonlinear systems. This method is also known as the EKF.

As far as Li-ion battery is concerned, EKF algorithm can not only give the amended SOC , but also to reflect the confidence of the estimated value. So, it has high application value for the situation that electric vehicles have changing current in actual operation. And the inconsistencies between single cell in the battery pack also can be forecasted early. In practical application, the Li-ion battery pack is always taken as a complete dynamic system, SOC is used as one of the system state variables. Then, error caused by system noise and measurement can be effective suppressed through updating the system state parameters based on the error between measured value and estimated value[4-7].

2. STATE-SPACE EQUATION ESTABLISHED

2.1. Battery Model Design

The best equivalent circuit model should be the simplest still capable of capturing all the relevant dynamics of the Li-ion battery system for the purposes of SOC estimation. The United States proposed equivalent circuit model of battery in the Partnership for a New Generation of Vehicles (PNGV) in 2001 named PNGV model as shown in Figure 1. It describes the internal resistance with ohmic resistance R_0 , the changes of electromotive force with C_0 , battery polarization with R_1, C_1 . The model has clear physical meaning and higher accuracy. It has good applicability to many work condition. Equation of state space could also be derived for analysis and application. So this model is now commonly used.

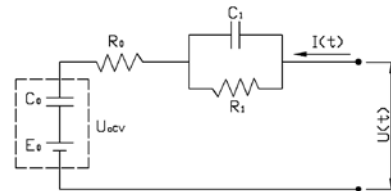


Figure 1. PNGV Model

To acquire data to identify the model parameters, a Hybrid Pulse Power Characterization (HPPC) test was conducted on the Li-ion battery. Discharge current pulse is taken as excitation, as shown in Figure 2. According to the response curve as shown in Figure 3, model parameters can be identified [8][9].

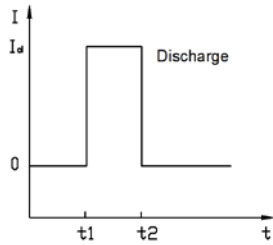


Figure 2. HPPC test profile

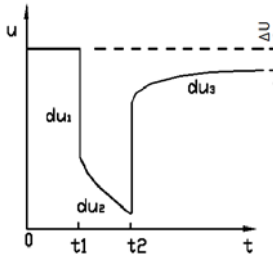


Figure 3. HPPC Voltage Response Curve

2.2. State-space equations

Using Kirchoff's current law and the definition of ideal capacitor, the differential equation is:

$$\frac{dU_{c1}}{dt} = -\frac{U_{c1}}{R_1 C_1} + \frac{I(t)}{C_1} \quad (3)$$

U_{ocv} describes the battery open circuit voltage according to OCV method, then the system output could be written as:

$$U(t) = U_{ocv} - U_{c1} - I(t)R_0 \quad (4)$$

Setting $X = [SOC(k) \ U_{c1}(k)]^T$ as state variables, and using Ah counting method, discrete state space equation could be written as:

$$\begin{bmatrix} SOC(k+1) \\ U_{c1}(k+1) \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & \exp(-T/(R_1 C_1)) \end{bmatrix} \begin{bmatrix} SOC(k) \\ U_{c1}(k) \end{bmatrix} + \begin{bmatrix} -\frac{\eta T}{C_0} \\ R_1(1 - \exp(-T/(R_1 C_1))) \end{bmatrix} I(k) + w \quad (5)$$

$$U(k) = U_{ocv}(k) - U_{c1}(k) - I(k)R_0 + v \quad (6)$$

Where T is sampling time, w is the input noise, v is the measurement noise.

3. THE INTEGRATED ALGORITHM ESTABLISHMENT BASED ON PNGV MODEL

3.1. Linearization Of The Parameters Of The State-Space Equation

According to the state equation as above equation (5), coefficient matrix could be written as follow:

$$A_k = \begin{bmatrix} 1 & 0 \\ 0 & \exp(-T/(R_1 C_1)) \end{bmatrix},$$

$$B_k = \begin{bmatrix} -\frac{\eta T}{C_0} \\ R_1(1 - \exp(-T/(R_1 C_1))) \end{bmatrix},$$

In the measurement equation as shown in equation (6), $U_{ocv}(k)$, which is fitted by SOC data from experiment, is a nonlinear function. So it needs to be linearization. Using the last iteration results as basis point, U_{ocv} is conducted Taylor series expansion along it. Taking the linear part, the coefficient of measurement equation could be obtained [5]:

$$C_k = \frac{\partial U(k)}{\partial X} = \begin{bmatrix} \frac{\partial U(k)}{\partial SOC} & \frac{\partial U(k)}{\partial U_{c1}} \end{bmatrix}$$

$$= \begin{bmatrix} \left. \frac{\partial f(SOC)}{\partial SOC} \right|_{soc=soc(k|k-1)} & -1 \end{bmatrix}$$

Where $SOC_{k|k-1}$ is one of the estimation of the state variable.

3.2. The Integrated Algorithm Establishment

The integrated algorithm consists of three steps. The first step: using OCV method to determine the initial state variable. The second step: using EKF method to make the state variable converge to the true value. The third step: using Ah counting method to estimate the follow up state variable. According to the three steps, a set of equations can be obtained to achieve the algorithm. This set of equations combine two categories, one of which is the time update, which predicts the state variable and error covariance, and the other is the measurement update, which calibrate the state variable and error covariance.

1) Time update

$$\hat{X}_{k|k-1} = A_k X_{k-1} + B_k u \quad (7)$$

$$P_{k|k-1} = A_k P_{k-1} A_k^T \quad (8)$$

Where $\hat{X}_{k|k-1}$ is the predict value of state variable at k-1 step to k step. $P_{k|k-1}$ is the predict of error covariance at k-1 step to k step. P_{k-1} is the error covariance.

The two time update equations update the state variable and the predict error covariance from k-1 step to k step.

2) Measurement update

$$K_k = P_{k|k-1} C_k^T (C_k P_{k|k-1} C_k^T + R_k)^{-1} \quad (9)$$

$$\hat{X}_k = \hat{X}_{k|k-1} + K_k [U(k) - \hat{U}(k)] \quad (10)$$

$$P_k = (I - K_k C_k) P_{k|k-1} \quad (11)$$

Where K_k is the gain, R_k is the independent, zero-mean, Gaussian noise processes of covariance matrix. \hat{X}_k is the estimate value at k step. $U(k)$ is the measured value. \hat{U}_k is estimate value of measurement.

The measurement update equations compare measured value $U(k)$ with predicted value. The difference is used to correct the state estimations and covariance estimations. Through times of iteration, the estimation matches the real quantities [5][10].

The EKF algorithm iterative process for Li-ion battery SOC is shown in Figure 4:

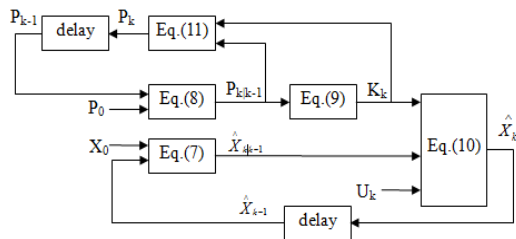


Figure 4. EKF algorithm flowchart

According to the iterative calculation process above, if the initial values including state variable X_0 , covariance P_0 and the measured value U_k are imported to system. The iterative process can constantly revise the estimate value according to measured values. Then, through continuous feedback correction like “prediction-validation-prediction”, the estimated value tends to match the real quantities.

4. EXPERIMENT AND SIMULATION ANALYSIS

To verify the algorithm, pulse discharge current is applied to the Li-ion battery pack as excitation. The initial SOC is 100%, the pulse amplitude $I_d = 20A$, the pulse duration is 20S. At the end of the pulse, 60s data sampling is continue. The collected data, which is used to estimate the state variable, is the measurement value of system output. The SOC estimate model is set up according to Equation 7 to 11 as well as the flowchart shown in Figure 4. The simulation results are shown in Figure 5.

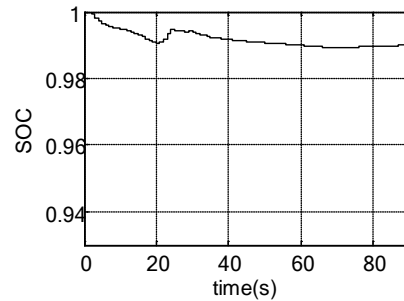


Figure 5. Result Of SOC Estimate Simulation

As we can see in Figure 5, the SOC estimate value through EKF algorithm simulation in the noise environment is 0.9911, at end of the 20s discharge duration. Meanwhile the SOC value according to theoretical calculation is 0.9926. Therefore, the error between simulation and theoretical calculation is only 0.15%. Although SOC value has a short wave after discharge stopping, it finally can be recovered to the estimation state though 40s duration. The results show that the EKF algorithm this paper proposed, which can eliminate the environment noise and measurement error, is fitted for Li-ion battery SOC estimation of electric vehicle.

5. CONCLUSION

SOC is an important parameter of electric vehicle battery. It is the important basis for providing strategy for vehicle control. In this paper, the li-ion battery is studied base on its equivalent circuit model. The discrete state space equation is established using Ah counting method and OCV method. The filtering algorithm is set up to research the problem of the battery’s SOC estimation under the noisy environments according to the principle of EKF. The simulation results showed that the integrated of three algorithms could very well remove the environments noise, so



the accurate estimate of Li-ion battery SOC value can be gained.

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