

# DANGEROUS GOODS OF RAILWAY TRANSPORT ROUTE OPTIMIZATION BASED ON MULTI-OBJECTIVE PROGRAMMING AND IMMUNE ALGORITHM

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## ABSTRACT

The dangerous goods transportation plays a great role in the area of railway transportation research, the whole process of dangerous goods transport involving multiple assignments links, which interplays with each other. The existing path optimization is one of important means to ensure transportation safety. This paper through the analysis of the characteristic of dangerous goods and the special operation process in the railway transportation, putting forward to three objective functions to reducing safety coefficient and transportation time and improving transport income, creating 0-1 integer nonlinear multiple objective programming model, using immune algorithm to find the solution to the model. At last, through an example using the method effectively selecting a specific route and optimizing the process of railway dangerous goods transportation.

**Keywords:** 0-1 Nonlinear Integer Multi-objective Programming Model, Immune Algorithm, Specific Route

## 1. INTRODUCTION

With China's rapid economic growth and people's living standard unceasing enhancement, the need to transport dangerous goods' varieties and quantity is increasing rapidly and all kinds of transportation accident increases year by year. So, ensuring the safety of dangerous goods is vital important. Dangerous goods transport path optimization is an important measure to improving the safety.

Considering the special organization model of the dangerous goods railway transportation (prior to set the dangerous goods into direct or through train, keep on running without any adaptation operations), so the transportation route choice will become very important.

At present, domestic scholars mainly research on the problem of route optimization of dangerous goods rail transportation. Literature[1] optimizes the route using multi-objective programming method, setting the path length, time, cost, risk, sensitive target number as target functions.

Literature[2] has a quantitative research on the railway transport risk, creating the accident

probability model and listing seven influencing factors of the transport ways and distance, the accident probability of loaded car section per kilometer, every train compositions truck number, the number of freight cars marshalling in a train, the number of dangerous goods cars, the leakage probability, the area of leakage influence and the population density in the influential area.

Literature[3] creates evaluation system using the fuzzy layer comprehensive evaluation method, considering the factors of cost in the process transport route selection, accident risk, accident hazards, accident repair ability.

Literature[4] have a conclusion that leak in the process of transportation is divided into two kinds, traffic accidents cause by the leakage and the leakage caused by traffic accidents, and points out the leak rate in the two cases showing a greater difference.

The references [1-4] optimize the route of dangerous goods railway transportation, creating 0-1 integer nonlinear model and using multi-objective programming method.

## 2. ANALYSIS OF PROBLEM

Railway transportation route falls into three kinds according to the distance: the shortest route, the specific route and the circuitous route; according to the economic benefit division into economic route and non-economic route. Considering the safety of dangerous goods transportation, need us to select specific cuts. Specific route choice generally needs special criteria.

Safety is the most important in the dangerous goods railway transportation. Safety is a evaluation criteria of much homework and many index. All kinds of regulations and organizational measures of dangerous goods is to reduce the operation link, or replace one risk factor of high operation. In choosing route first concern is the interval operating condition; In addition, is influence, once dangerous goods leak, keeping the accident harm to the minimum.

Secondly, ensuring the highest income. Income here refers to the unit weight of dangerous goods. transport process of an income. Income of Dangerous goods comes from transportation. The operation cost is the result of spending indexes adding (the calculation of income here refers to the transportation in the safe situation).

Finally, requiring the dangerous goods transportation in the interval operation and transfer station operation time more short more good from the view of running time. At present, as long as the loading to the station of arrival traffic group number, then in the dangerous goods basic will into direct or through train. However, when loading station to landing station without traffic group number, there are two points needing to pay attention: the first, in one adjustable transit operation to reach the station as far as possible; the second, choice technical operation time at least or less technical stations do the adjustable transit operation.

## 3. CREATING MODELS

### 3.1 Format of Manuscript

$I$  —the set of all dangerous goods types which can deal with railway transport .

$J$  —the interval set of all paths from the station of departure to the terminal.

$L$  —the interval path length set of dangerous goods transportation.

$D$  —the set of all technical stations except the terminal station on the path.

$U$  — the set of traffic group number in technology station.

$T$  —the time set of dangerous goods in the interval operation.

$T'$  — the time set of Various technical operations for dangerous goods in D.

$H$  —the expenses set of dangerous goods transportation .

$H'$  — the cost set of dangerous goods transportation.

$T_0$  —the time limit for delivery.

$N$  — the ability of interval through(the number of the trains).

$K$  —the leakage accident in the interval.

$l_i^j$  —the interval length of the interval j.

$q_a(j)$  —the rate of the type of whether a in the interval j.

$r(j)$  —the population density of the interval j.

$p_i(j)$  — traffic accident probability of dangerous goods i in the interval j.

$p_i(j, k)$  —the leakage rate of dangerous goods i in the interval j.

$\alpha_j$  — the proportion of Passenger Cars to freight cars in the interval j.

$\sigma$  —the factor of Distance cost .

$K^*$  —the factor of time cost .

$w_n$  —the total number of ramp in intervals .

$w_0$  —the restricted ramp.

$g_i$  —the weight of interval dangerous goods i .

$t_0$  —the total time of dangerous goods staying between the loading and unloading station .

$t_{ij}$  —the operation time of dangerous goods  $i$  in the interval  $j$ .

$t'_{id}$  —the staying time of dangerous goods  $i$  in the adjustable transit technology station .

$t''_{id}$  —the staying time of dangerous goods  $i$  in the un-adjustable transit technology station .

$X_{ij}$  —is a 0-1 variable;

0 refers to dangerous goods  $i$  is not on the path  $j$ ;  
1 refers to dangerous goods  $i$  is on the path  $j$ ;

Among ,  $i=1,2,3\cdots m$  ,  $i \in I$  ;  $j=1,2,3\cdots n$  ,  $j \in J$  .

$y_{iu}$  —is a 0-1 variable;

0 refers to dangerous goods  $i$  do not enter into the traffic group  $j$ ;

1 refers to dangerous goods  $i$  enter into the traffic group  $j$ .

$y'_{iu}$  —is also a 0-1 variable;

0 refers to the traffic group  $j$  is not the arrival station of dangerous goods  $i$  ;

1 refers to the traffic group  $j$  is the arrival station of dangerous goods  $i$  ;

$u = 1,2,3\cdots e$  ,  $u \in U$  .

### 3.2 Objective Function

The first objective function is to keep the risk of safety as low as possible in the transport of dangerous goods. Safety risk is one of the most difficult factors to analysis, involving many aspects and multiple parameters, including the specific accident probability, the interval train logarithm, line length, the weather, traffic flow structure, line status and interval population density. Among them, the incident rate  $p_i(j)$  、  $p_i(j,k)$  and weather condition  $q_s(j)$  can calculate the probability through the way of probability statistics; line length  $l$  、 traffic structure  $\alpha_j$  、 interval population density  $r(j)$  getting through consulting relevant material; Line condition is the situation of road and bridge, culvert and curve slope on the path. Above-mentioned influence factors can be converted into additional gradient ramp.

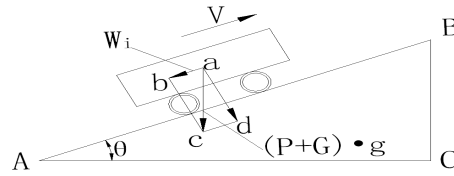


Figure 1: The Unit Additional Slope

As shown in figure 1, the unit additional slope as :

$$w_{\beta} = \frac{1000W_{\beta} \sin \theta}{g(P+G)} \quad (1)$$

Additional gradient curve is:

$$w_{\chi} = \frac{700}{R} , R \text{ is radius of curve} \quad (2)$$

Additional tunnel air slope is:

$$w_{\delta} = \begin{cases} 0.0001l_{\delta}v_{\delta}^2 & (\text{the limited scope}) \\ 0.13l_{\delta} & (\text{un-limited scope}) \end{cases} \quad (3)$$

Add ramp for  $w_{\eta} = w_{\beta} + w_{\chi} + w_{\delta}$  , the unit is per mille. The result of multiply all factors above is the risk factor  $f_1$  in a certain interval, which is the smaller the better.

The second objective function is to keep the transportation time as short as possible. Time can be represented by three parts, including adjustable transit time, through time without adjustment and interval operation time. The different between dangerous goods transportation and general cargo transportation is that the goal of dangerous goods transport is go do distance so far so good in one loading .( if the loading station is the station of arrival traffic group number, then dangerous goods enter into straight or direct train , else ,the requirements in the midway having adjustable transit times fewer is better). In the condition of the same time of adjustment, decrease car hours as far as possible in the transport of dangerous goods .  $S$  is a positive integer, represents the total of stations on the transportation path.

The third objective function is to keep the transportation income time as high as possible. Income = freight - costs, freight is an increasing function relative to the transport distance, while cost is a reducing function relative to the transportation function.



$$\min f_1 = \frac{\sum_{i=1}^m \sum_{j=1}^n x_{ij} \cdot p_i(j) \cdot p_i(j,k) \cdot N_j \cdot l_j \cdot w_\eta \cdot q_a(j) \cdot r(j) \cdot \alpha_j}{\sum_{i=1}^m \sum_{j=1}^n x_{ij}} \quad (4)$$

$$\min f_2 = \sum_{i=1}^m \sum_{j=1}^n x_{ij} t_{ij} + \sum_{d=1}^s \sum_{i=1}^m \sum_{u=1}^e y_{iu}^d y'_{iu} t'_{id} + (s-2 - \sum_{d=1}^s \sum_{i=1}^m \sum_{u=1}^e y_{iu}^d) t''_{id} + t_0 \quad (5)$$

$$f_{income} = f_{freight}(l_j) - f_{cost}(l_j) \quad (6)$$

As expression (6) shows, freight  $f_{cost}(l_j)$  is:

$$f_{freight}(l_j) = (h^i_{depart} + h^i_{running} \times l_j) \times g_i \quad (7)$$

According to the literature [7], it is known that the transportation cost as a function hard to be quantified, the influenced factors including traffic volume, structure of freight and passenger flow, transportation distance and freight balance. Railway transportation cost is mainly composed of originating and reach operating expenditure, transit operation expenditure and operation operating expenditure. The proportions of operating expenditure in these three parts is the largest, although the total operation cost will be decreased

with the increasing distance, the transfer cost and arrival and departure cost does not increase with the reducing unit cost. The operation process of each link is divided into different technical indicators, multiplied by the respective parameters, linear adding for the result of total cost. Due to the arrival and departure link's shunting locomotive operation cost combined with the vehicle operating cost; the locomotive operation interval distance combined with the distance and the interval locomotive running time cost combined with the vehicle running time cost, the calculation mentioned in this article for each ton-km costs, the total weight of goods will not be considered.

### 3.3 Constraint Conditions

The constraint conditions of objective functions (4)、(5)、(9) are :

$$f_{cost}(l_j) = \frac{\sum_{d=1}^s \sum_{i=1}^m \sum_{u=1}^e y_{iu}^d y'_{iu} t'_{id} + t_0 + (s-2 - \sum_{d=1}^s \sum_{i=1}^m \sum_{u=1}^e y_{iu}^d) t''_{id}}{l_j g_i} + \kappa \cdot \sum_{i=1}^m \sum_{j=1}^n x_{ij} t_{ij} + \sum_{i=1}^m \sum_{j=1}^n x_{ij} \frac{\sigma}{g_i} \quad (8)$$

The goal of the objective function three is for the highest unit profit in the rail transportation process of dangerous goods:

$$-\kappa \cdot \sum_{i=1}^m \sum_{j=1}^n x_{ij} t_{ij} - \frac{\sigma}{g_i} \quad (10)$$

$$x_{ij} \leq y_{iu} \quad (11)$$

$$t''_{id} \quad t'_{id} \quad (12)$$

$$\sum_{j=1}^m l_{j,d+1}^B \leq \sum_{j=1}^m l_{j,d}^B \quad (13)$$

$$p_i(j,k) \in [0,1], \forall j \quad (14)$$

$$p_i(j) \in [0,1], \forall j \quad (15)$$

$$a \in [1,b] \quad (16)$$

$$\kappa > 0, \sigma > 0 \quad (17)$$

$$l_j > 0 \quad (18)$$

$$w_\eta \leq w_0 \quad (19)$$

$b$  is the total of all kinds of adverse weather.

Constraints (10) means that the transportation time

strictly control in the limit of freight transit period. Type (11) shows dangerous goods traffic must in an effective path. Type (12) indicates the time of no change through should be far less than adjustable transit. Constraints (13) is to prevent roundabout transport. Constraints (14) (15) (16) (17) (18) define all probability, cost factor, time and interval length greater than 0. Constraint(19)makes the the adding ramp cannot exceed r-rated ramp.

**3.4 Model Optimization**

The general method of multi-objective optimization model converts multiple objective function to single objective function(conversion the objective functions  $f_1$ 、 $f_2$ 、 $f_3$  to the single objective function) Give three different weighted values  $\lambda_1$ 、 $\lambda_2$ 、 $\lambda_3$  for the objective functions  $f_1$ 、 $f_2$ 、 $f_3$ , as following:

$$F = \lambda_3 f_3 - \lambda_1 f_1 - \lambda_2 f_2 \tag{20}$$

Give  $\lambda_1$ 、 $\lambda_2$ 、 $\lambda_3$  different values according to the importance in the process dangerous goods transport: first is the safety, then the highest income, and finally is the shortest time.

**4. ALGORITHM AND STEPS**

The model of dangerous goods railway transport path optimization in this paper uses 0-1 integer nonlinear model (MSLSLP) . Due to this kind problem including many variables and parameters, solve it by the traditional operational research method is very complex.

Step1:random generation initial father generation population, forming antibody;

Step2: more prior knowledge extraction vaccine;

Step3:current population in affinity calculation, memory cells begin to differentiation.If the current population contains the best individual, the algorithm stop running and output, otherwise continue;

Step4: cross operation for the father generation populations ;

Step5: mutation operation for the father generation population;

Step6: vaccinated operation for the current father generation population ;

Step7: immune selection operation for the current father generation population, updating the population to get new antibody, return to step 3;

**5. EXAMPLE ANALYSIS**

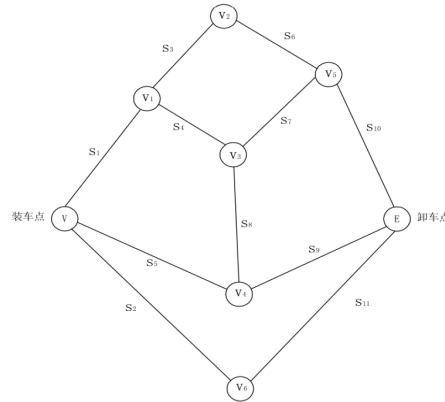


Figure 2 Example Network Diagram

Pictured above , network diagram  $S$  which composed by station and interval represents traffic interval ,  $V$  represents the station. The railway network totally composed by 8 stations and 11 intervals. All interval are double-line automatic block and the interval operation time includes avoiding time to passenger train and luggage train time. The railway network from  $V$  to  $E$  composed of 4 complex cross ring. ( the four rings respectively are:  $V - V_1 - V_3 - V_4$  ,  $V_1 - V_2 - V_5 - V_3$  ,  $V_3 - V_5 - E - V_4$  ,  $V - V_6 - E - V_4$  ) Dangerous goods are loaded in  $V$  ,carried to  $E$  ,then unloaded. Statistics of all kinds of factors influencing interval safety using forms mode , as is shown in table 1.

Interval accident rate  $p_i(j)$  is difficult to statistics in a specific interval. The average rate in the last ten years according to the statistical data, is three times per ton-km , accident leakage rate  $p_i(j,k)$  taking the average 30% and the sum of loading time and Truck assembly time in the loading station  $V$  is  $t_0 = 15$  hours with traffic group numbers directly. Among the stations



through from  $V$  to  $E$  adjustable transit time as shown in table 2.

The cost of arrival operation, departure operation and transit operation are decided by the quantity of work, which is to be calculated by the specific operation time. Take cost factor  $\kappa$ ,  $\kappa'$  and  $\sigma$  as

0.08 yuan per tons hour, 0.002yuan per tons hour, 0.005yuan per tons hour.

Dangerous goods is divided into nine categories by railway administration, the diffset screening one specific dangerous good from the nine categories and the commodity name and freight number as shown in table 3.

Table 1: Dangerous Goods Transportation Interval Related Information

Interval name $j$	Interval length $I_j$ (km)	Ratio of interval adverse weather $q_a(j)$	Average population density along the interval $r(j)$ ( person per km <sup>2</sup> )	Interval maximum conversion slope $w_\eta$ (%)	The number of interval train $N$ (pair/day)	Passenger proportion in the train $\alpha_j$	Average operation time in the interval $t_{ij}$ (hour)
$S_1$	246	036	265	13	83	0.98	4.1
$S_2$	424	0.22	118	6	76	0.18	7.1
$S_3$	176	0.42	289	10	83	0.81	2.7
$S_4$	152	0.39	450	12	136	0.59	2.6
$S_5$	316	0.32	476	14	146	0.43	4.4
$S_6$	186	0.23	218	6	139	0.31	2.6
$S_7$	198	0.11	98	9	76	0.11	3
$S_8$	240	0.25	402	5	170	0.6	4
$S_9$	288	0.34	314	10	105	0.71	5.2
$S_{10}$	278	0.33	146	19	75	0.29	4.6
$S_{11}$	414	0.09	103	8	55	0.16	6.9

Table 2: Vehicle Operation Schedule Of Stations

Station name	$V_1$	$V_2$	$V_3$	$V_4$	$V_5$	$V_6$
No adjustment through time $t_{id}''$ (minute)	13	10	15	20	16	12
adjustment time $t_{id}'$ (hour)	22	25	18	17	29	33

Table 3: Dangerous Goods Name Of Commodity And Freight number list

Classes	Explosive materials	Compress ed gases and liquefied gases	Flammabl e liquid	Flammable solid, items and spontaneous combustion in wet flammable items	Oxidizin g substanc es and organic peroxide s	Poisons and infectious substances	Radioacti ve substanc es	Corrosive s	Else
Name of Goods	detonatin g fuse	liquefied petroleum gas	gasoline	sulphur	oxydol	chloroform	Thorium sulfuric acid	nitric acid	castor bean
Freight number	5	5	6	5	5	5	5	5	5

The transportation fare of N0.5 arrival and departure basic price  $h^i_{发}$  is 10.40 yuan per ton, basic operation price  $h^i_{运行}$  is 0.0549 yuan per ton km. The transportation fare of N0.6 arrival and departure basic price  $h^i_{发}$  is 14.80 yuan per ton, basic operation fare  $h^i_{运行}$  is 0.0765 yuan per ton km.

In this diffset, defining loading station  $V$  as  $V_8$ , unloading station  $E$  as  $V_7$ , Other depot's subscript digital code unchanged.

Any path from loading station  $V_8$  to unloading station  $V_7$  constitutes the immune algorithm of antibodies. In this mathematical model, the objective function  $F$  is the antigen, crossover probability taking 0.7, mutation probability taking 0.02, Memory bank number for 20, the antibody population scale is 50, the largest number of un-optimization algorithm is 2000 times, finally, the output of program as following :

```

输出: Sort() 种群排序
i=1 pop[j].F_affective=2687.802704 pop[i].chrom=08470000
i=2 pop[j].F_affective=1352.402948 pop[i].chrom=08134700
i=3 pop[j].F_affective=297.720822 pop[i].chrom=08135700
i=4 pop[j].F_affective=48.562909 pop[i].chrom=08670000

免疫算法最优抗体:
适应值: best_antibody.F_value=2687.802704
抗体编码: best_antibody.chrom= 0 8 4 7 0 0 0 0
请按任意键继续. . .
    
```

Figure 3 Output Chart Of Immune Algorithm Program

The result show the optimal path is {0,8,4,7,0,0,0,0}, that the path  $V - V_4 - E$  is optimal. In order to adjust the objective function with every sub-function to be unified order of magnitude, taking  $\lambda_1$ 、 $\lambda_2$ 、 $\lambda_3$  as 0.5,0.15,0.35  $\times 10$ , The optimization function  $F = 2687.802704$ .

6. CONCLUSION

The paper analyses the dangerous goods railway transport path optimization problems in quantity , creating the model of 0-1 nonlinear integer multi-objective programming, using immune algorithm to computing the result. The result shows in dealing with this kind of problem the method can help quickly reaching the global optimal. This paper during the optimization model taking the

three objective function respectively as three weight value, their accuracy need to be further discussed.

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