

AN ARTIFICIAL BEE COLONY ALGORITHM WITH MODIFIED SEARCH STRATEGIES FOR GLOBAL NUMERICAL OPTIMIZATION

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ABSTRACT

The Artificial Bee Colony (ABC) algorithm based on swarm intelligence is a more competitive algorithm than other Evolution Algorithm (EA). The results of recent studies indicate that the ABC algorithm has many advantages but it has two major weaknesses: one is slower convergence speed; the other is getting trapped in local optimal value early. Inspired by differential evolution (DE), different with other improved ABC algorithm based Differential Evolution (DE), we propose a modified ABC algorithm, named it ABC/current-to-best/1, by introducing the best food source (the best solution) and randomly choosing food source (the random solution). Experiments are conducted on a group of 24 benchmark functions. The results testify the performance of ABC/current-to-best/1 algorithm better than original ABC and some pre-existing improved ABC algorithm.

Keywords: *Artificial Bee Colony, Global Numerical Optimization, Search Strategy, Differential Evolution*

1. INTRODUCTION

Population-based algorithm can be mainly classified into two types: Evolutionary Algorithm (EA) and Swarm Intelligence Algorithm (SIA). The two population-based algorithms have a common feature: all possible solutions in population can be moved toward the optimized solution by applying some operators based on the fitness value. In EA, The popular algorithms include Genetic Algorithm(GA)[1], Genetic Programming(GP)[2], Evolution Strategy(ES)[3] and Evolution Programming(EP)[4]. Since the late 1990s, Differential Evolution (DE) has emerged as a competitive EA algorithm [5-6]. From then on, DE has been applied in tackling multimodal, multiobjective, constrained and dynamic optimization problems extensively and has got better experimental results than other EAs. As for swarm intelligence-based algorithm, Bonabeau has defined the swarm intelligence as "...any attempt to design algorithms or distributed problem-solving devices inspired by the collective behavior of social insect colonies and other animal societies..." [7]. The classical examples of swarm intelligence algorithms include Ant Colony Optimization(ACO) algorithm which simulates foraging behavior of ants[9], Particle Swarm Optimization (PSO) algorithm which is composed of birds and simulates the social behavior of bird flocking[9], Virtual bee algorithm(VBA)[10], Artificial bee colony (ABC) algorithm[11] and so on. Moreover some hybrid

methods based EA and SIA have been proposed to compensate some drawbacks in using EA or SIA alone [12-15].

In this paper, we will pay more attention to how to make use of ABC algorithm to solve global numerical optimization problem effectively by modifying the searching strategies. As we all know, exploration and exploitation should be carefully balanced in all population-based algorithms in order to achieve better solution. Exploration means independent searching for search space while exploitation means searching process according to collected information move toward objective. In fact, the two above contradict to each other sometimes. To achieve better performance, we should make balance between exploration and exploitation. There are similar problems in the ABC algorithm, as well. The major problems facing the ABC algorithm and all population-based algorithms include slower convergence speed in solving unimodal problems and easier getting trapped in local optima in solving multimodal problems [16]. In ABC algorithm, the searching strategies are more stressing exploration than exploitation and there by some important variants about ABC algorithm have been proposed to achieve better global optimization ability by balancing exploration and exploitation [13, 14, 15, 17]. These improved algorithms which are using either EA or PSO to ABC's searching strategies enhance exploitation in some sense but getting into local optimized solution easier.

In order to balance exploration and exploitation well, inspired by DE [4], we propose a new modified searching strategy which is not only improving exploitation but also avoiding getting trapped into local optimization early.

The rest of this paper is organized as follows. In section 2, we outline classical ABC algorithm and some important variants of ABC algorithm. Section 3 proposes modified ABC algorithm, explaining improved searching strategies in detail. The experimental parameters settings and results are described in section 4. Section 5 concludes this paper with a discussion.

2. CLASSICAL ABC ALGORITHM AND IMPORTANT VARIANTS

Artificial Bee Colony(ABC) algorithm introduced by karaboga was first used to find an optimal solution in numerical optimization by simulating the behavior of foraging selection[11].The collective intelligence in ABC is composed of three components: food sources, employed bees, unemployed bees(only onlooker bees, scout bees) and two behavior models: recruitment and abandonment. The whole algorithm's structure is described as follows:

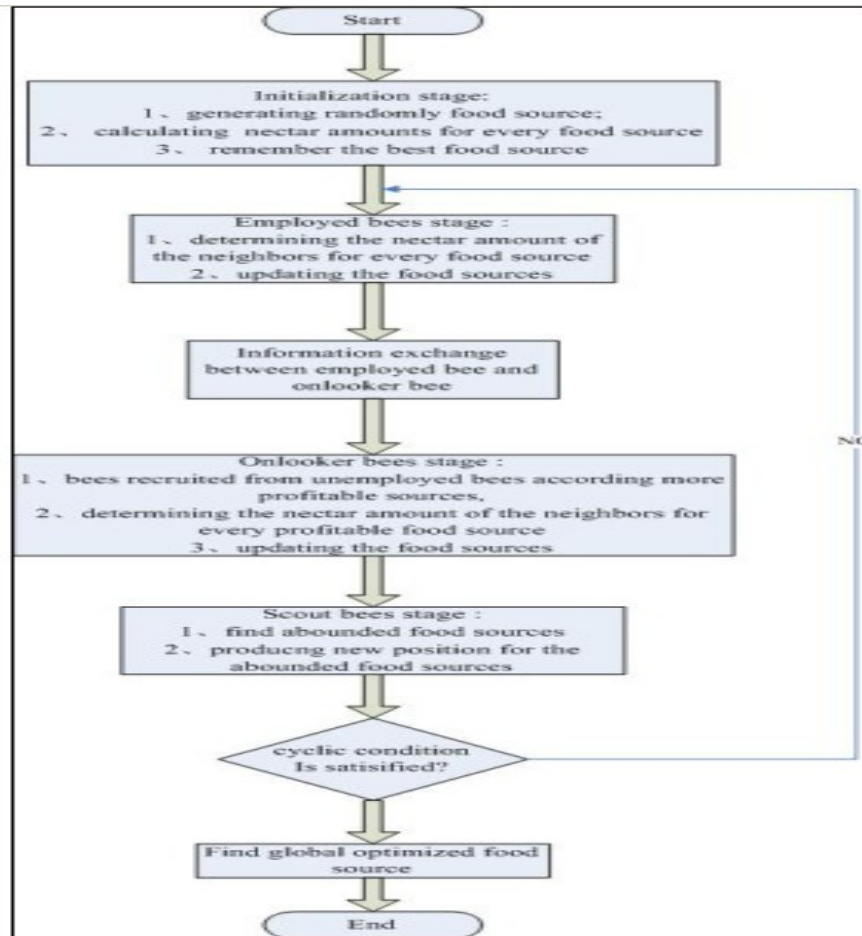


Figure 1: Flowchart Of The Classical ABC Algorithm

In reference [11], a detailed explanation was made for classical ABC algorithm. In this section, we outline the major idea of the algorithm. As we can see from Figure 1, three major stages are included into ABC algorithm, employed bees stages, onlooker bees stages and scout bees stages respectively.

2.1 Initialization Stage

In ABC algorithm, every food source position $X_i = (x_{i,1}, x_{i,2}, \dots, x_{i,D})$, where D is the number of problem

dimension, representing a possible solution. The initial population should contain the range as much as possible by uniformly randomizing individuals within the search space. This operation is defined as in [16]:

$$x_i^j = x_{\min}^j + rand(0,1)(x_{\max}^j - x_{\min}^j) \quad (1)$$

Where, x_i^j is the jth component of the ith food source position (vector), x_{\min}^j and x_{\max}^j are the minimum and the maximum of the jth dimension respectively.



pectively. In ABC algorithm, the amount of nectar in a food source represents the quality of the solution. In practice, the amount of nectar can be expressed with the optimal value of the objective function. So, the final step in initialization stage is to calculate the fitness value according to the objective functions optimized.

2.2 Employed Bees Stage

In this stage, every employed bee which is corresponding to a food source is in charge of two things. One is going on exploiting the food source which has already been there, the other is being responsible for exchanging information with onlooker bees. In ABC algorithm, exploiting means that employed bees produce a modification on the food source (solution) according to her memory of finding new food source and evaluate it. The ABC algorithm uses (2) for producing a candidate solution:

$$v_{ij} = x_{ij} + \Phi_{ij}(x_{ij} - x_{kj}) \quad (2)$$

Where $k \in \{1, 2, 3, \dots, SN\}$, SN is the size of population, $j \in \{1, 2, 3, \dots, D\}$, k is produced randomly which is different from i . Φ_{ij} is restricted in $[-1, 1]$ and determined randomly. v_{ij} is a modification to the food source x_{ij} which is remembered by employed bees. The perturbation on x_{ij} is determined by $\Phi_{ij}(x_{ij} - x_{kj})$. The amplitude of the perturbation is controlled by Φ_{ij} . The employed bee will remember the new food source and forget the old one according to the amount of nectar. Besides exploiting, employed bees carry some information (e.g. nectar amount) which is shared as onlooker bees. An unemployed bee can be recruited to an onlooker bee according to the probability value p_i , associated with that food source.

$$p_i = \frac{fit_i}{\sum_{k=1}^{SN} fit_k} \quad (3)$$

Where fit_i is the fitness value of the objective functions.

2.3 Onlooker Bees Stage

Onlooker bees are recruited to those food sources which is abundant in nectar amount depending on the information carried by employed bees. According to the probability formula (3), the onlooker bees can select a food source (position) which is rich in nectar amount (the best fitness value). When exchanging onlooker bees fly to the food source, exchanging they will also produce a modification just like employed bees doing so using (2) and then check the

nectar amount of the new food source. By comparing the amount of nectar of the new position with the old one, the onlooker bees remember the better food source and forget the other.

2.4 Scout Bees Stage

When a food source (position) can not be improved through predefined number which is the parameter called it "limit" in ABC algorithm, the old food source (position) will be abandoned and replaced by a new food source (position) by the scout bees according to (1).

So, from the explanation above, we can see that there are many advantages in ABC algorithm, such as a few control parameters, including population size (NP), the value Limit, the max cycle number (MCN) and robust searching process. In robust search progress, exploitation and exploration must be carried out together. Employed and Onlooker bees carry out exploitation while Scout bees are in charge of exploration.

However, like the other EA, there are some problems in ABC algorithm. As indicated in reference [13], the two major problems are slowing convergence speed in handling unimodal and easier getting in local optima in solving multimodal. So, a number of variants have been proposed to improve original ABC by balancing exploration and exploitation and to enhance the searching ability in solving complex global optimized questions [13, 15, 17]. For example, GABC, inspired by PSO [13] improves the exploitation ability by introducing the information of global best solution to searching space. CABC which is taking advantage of chaotic idea to improve ABC [15] and ABC/best, inspired by DE [17], and the like.

To achieve the two above goals, exploration and exploitation, inspired by DE, we propose a new modified searching strategy to improve ABC algorithm, named it ABC/rand-to-best/1 which is different from reference [17]. In the following section, the proposed improved ABC will be explained in detail.

3. ABC/CURRENT-TO-BEST/1 ALGORITHM

Differential Evolution [5] is a simple and very effective EA. The performance of DE is dependent on the mutation strategies, crossover scheme and selection. The family of DE mainly contains some different mutation strategies, such as, DE/rand/1, DE/rand/2, DE/current-to-best/1, DE/best/1, and so on [18]. Different search strategies result in different mutation scheme. The following mutation strategy is used in the literature about DE:



$$DE / current - to - best / 1: \bar{V}_{i,G} = \bar{X}_{i,G} + F \cdot (\bar{X}_{best,G} - \bar{X}_{i,G}) + F \cdot (\bar{X}_{r1,G} - \bar{X}_{r2,G}) \quad (4)$$

Where the indices $r1, r2$ are mutually exclusively integers randomly selected from $[1 \dots NP]$ and different with i , NP is the size of the population. The factor F is a controlling parameter which is used to scale the difference vector. $\bar{X}_{i,G}$ and $\bar{V}_{i,G}$ are known as target vector and donor vector. $\bar{X}_{best,G}$ is the best individual at the generation G which is the minimum objective function value in the minimum problem. The best solution is introduced to the current generation in (4), which guides the searching progress. It is beneficial to discover rapidly the best solution [6].

Inspired by the above mutation in DE and based on the characteristic of ABC algorithm, we modify the strategies in searching new food source by employed and onlooker bees, named it ABC/current-to-best/1. The expression is as follows:

$$ABC / current - to - best / 1: \bar{v}_{j,i,G} = \bar{x}_{j,i,G} + F_1 \cdot (\bar{x}_{j,best,G} - \bar{x}_{j,i,G}) + F_2 \cdot (\bar{x}_{j,r1,G} - \bar{x}_{j,r2,G}) \quad (5)$$

Where, $x_{j,i,G}$ is the j th component in the i th food source at the generation G . similarly, $x_{j,best,G}$ is the j th component of the best food source in the current generation. The definition $r1, r2$ is the same as the above in *DE/current-to-best/1*. The combination of $\bar{x}_{j,best,G} - \bar{x}_{j,i,G}$ and $\bar{x}_{j,r1,G} - \bar{x}_{j,r2,G}$ to perturb the target vector $\bar{x}_{j,i,G}$. The one difference $\bar{x}_{j,best,G} - \bar{x}_{j,i,G}$ indicates the distance between the current food source and the best food source in the current generate, which helps to fast discover optimized food source fast but exists some risk in getting trapped local optima; the other difference $\bar{x}_{j,r1,G} - \bar{x}_{j,r2,G}$ reflects some ra

ndom exploration in the neighbor of the old food source. So, the improved method we propose is not only keeping the search guide to the optimized solution rapidly but also keeps a certain stochastic exploration. The scaling factors $F1$ and $F2$ are controlling parameters for the two above differences and are generated as uniform random numbers in $[0, f1]$ and $[0, f2]$ respectively. It is noted that parameters $f1$ and $f2$ play an important role in producing candidate solution. By adjusting different group of $(f1, f2)$, we can achieve optimum searching process.

In this paper, we modify the search strategies that employed and onlooker bees stage in the original ABC algorithm, inspired by DE. Although some modifications about ABC based on DE are also made in reference [17], it is different from our modification. The modification in [17] increases the exploitation of ABC algorithm but gets trapped in local optimization early sometimes.

4. EXPERIMENTS

Some experiments are designed to illustrate our modification to ABC algorithm. We used 24 benchmark problems [16] including unimodal, multimodal, separable and non-separable in order to test the performance of ABC/current-to-best/1 algorithm. The 24 benchmark functions are listed in Table 1. Because the parameters $(f1, f2)$ play an important role in the algorithm we propose, we will test how to choose $f1$ and $f2$ to achieve better searching optimization ability in the first experiment. The second one is comparing between original ABC and ABC/current-to-best/1 algorithm we propose and the last group is done between pre-existing ABC algorithm (e.g. those improved) and that we propose



Table1. Benchmark Function Used In Experiments
 D: Dimension, C: Characteristic, U: Unimodal, M: Multimodal, S: Separable, N: Non-Separable

No	Function	Search Range	C	D	Formulation	Min
1	Step	[-100,100]	US	30/60	$f(x) = \sum_{i=1}^n (\lfloor x_i + 0.5 \rfloor)^2$	0
2	Sphere	[-100,100]	US	30/60	$f(x) = \sum_{i=1}^n x_i^2$	0
3	SumSquares	[-10,10]	US	30/60	$f(x) = \sum_{i=1}^n ix_i^2$	0
4	Quartic	[-1.28,1.28]	US	30/60	$f(x) = \sum_{i=1}^n ix_i^4 + random[0,1)$	0
5	Beale	[-4.5,4.5]	UN	5	$f(x) = (1.5 - x_1 + x_1x_2)^2 + (2.25 - x_1 + x_1x_2^2)^2 + (2.625 - x_1 + x_1x_2^3)^2$	0
6	Easom	[-100,100]	UN	2	$f(x) = -\cos(x_1)\cos(x_2)\exp(-(x_1 - \pi)^2 - (x_2 - \pi)^2)$	-1
7	Matyas	[-10,10]	UN	2	$f(x) = 0.26(x_1^2 + x_2^2) - 0.48x_1x_2$	0
8	Colville	[-10,10]	UN	4	$f(x) = 100(x_1^2 - x_2)^2 + (x_1 - 1)^2 + (x_3 - 1)^2 + 90(x_3^2 - x_4)^2 + 10.1((x_2 - 1)^2 + (x_4 - 1)^2) + 19.8(x_2 - 1)(x_4 - 1)$	0
9	Trid10	[-D ² ,D ²]	UN	10	$f(x) = \sum_{i=1}^n (x_i - 1)^2 - \sum_{i=2}^n x_i x_{i-1}$	-210
10	Schwefel2.22	[-10,10]	UN	30/60	$f(x) = \sum_{i=1}^n x_i + \prod_{i=1}^n x_i $	0
11	Rosenbrock	[-30,30]	UN	3/4	$f(x) = \sum_{i=1}^{n-1} [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$	0
12	Dixon-Price	[-10,10]	UN	30/60	$f(x) = (x_1 - 1)^2 + \sum_{i=2}^n i(2x_i^2 - x_{i-1})^2$	0
13	Bohachevsky1	[-100,100]	MS	2	$f(x) = x_1^2 + 2x_2^2 - 0.3\cos(3\pi x_1) - 0.4\cos(4\pi x_2) + 0.7$	0
14	Booth	[-10,10]	MS	2	$f(x) = (x_1 + 2x_2 - 7)^2 + (2x_1 + x_2 - 5)^2$	0
15	Rastrigin	[-5.12,5.12]	MS	30/60	$f(x) = \sum_{i=1}^n [x_i^2 - 10\cos(2\pi x_i) + 10]$	0
16	Schwefel	[-500,500]	MS	30/60	$f(x) = n * 418.982887 - \sum_{i=1}^n (x_i \sin(\sqrt{ x_i }))$	0
17	Schaffer	[-100,100]	MN	2	$f(x) = 0.5 + \frac{\sin^2(\sqrt{x_1^2 + x_2^2}) - 0.5}{(1 + 0.001(x_1^2 + x_2^2))^2}$	0
18	Six Hump Camel Back	[-5,5]	MN	2	$f(x) = 4x_1^2 - 2.1x_1^4 + \frac{1}{3}x_1^6 + x_1x_2 - 4x_2^2 + 4x_2^4$	-1.03163
19	Bohachevsky2	[-100,100]	MN	2	$f(x) = x_1^2 + 2x_2^2 - 0.3\cos(3\pi x_1)\cos(4\pi x_2) + 0.3$	0
20	Bohachevsky3	[-100,100]	MN	2	$f(x) = x_1^2 + 2x_2^2 - 0.3\cos(3\pi x_1 + 4\pi x_2) + 0.3$	0
21	Goldstein-Price	[-2,2]	MN	2	$f(x) = \left[\frac{1 + (x_1 + x_2 + 1)^2}{(19 - 14x_1 + 13x_1^2 - 14x_2 + 6x_1x_2 + 3x_2^2)} \right] * \left[\frac{30 + (2x_1 - 3x_2)^2}{(18 - 32x_1 + 12x_1^2 + 48x_2 - 36x_1x_2 + 27x_2^2)} \right]$	3
22	Griewank	[-600,600]	MN	30/60	$f(x) = \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos(\frac{x_i}{\sqrt{i}}) + 1$	0
23	Ackley	[-32,32]	MN	30/60	$f(x) = -20 \exp(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}) - \exp(\frac{1}{n} \sum_{i=1}^n \cos(2\pi x_i)) + 20 + e$	0
24	Penalized2	[-50,50]	MN	30/60	$f(x) = 0.1 \left\{ \sum_{i=1}^{n-1} (x_i - 1)^2 [1 + \sin^2(3\pi x_{i+1})] + (x_n - 1)^2 [1 + \sin^2(2\pi x_n)] \right\} + \sum_{i=1}^n u(x_i, 5, 100, 4)$ $u(x_i, a, k, m) = \begin{cases} k(x_i - a)^m, & x_i > a \\ 0, & -a \leq x_i \leq a \\ k(-x_i - a)^m, & x_i < -a \end{cases}$	0



4.1 Influence of Parameters in ABC/Current-to-Best/1

Different from original ABC and other improved ABC algorithms, the parameter ($f1, f2$) plays an important role in ABC/current-to/best/1 algorithm. So, we make use of several typical benchmark functions to see how the parameters ($f1, f2$) influence the ability of ABC/current-to-best/1 algorithm. The result

is listed in Table 2. The arrangement of the parameters is the same as GABC [13].

From Table 2, as a whole, ABC/current-to-best/1 displays excellent performance when parameters ($f1, f2$) are (1.6, 0.4) rough. Here, the result on the Griewank and Rastrigin is better than the two others.

Table 2 . The Analysis Of The Performance Of Parameters In ABC/Current-To-Best/1

(C1,C2) Fun	(0.0, 2.0)	(0.4, 1.6)	(0.6, 1.4)	(0.8, 1.2)	(1.0, 1.0)
Sphere	1.3043e-005(mean) (5.6479e-005) (std)	1.3208e-58 (1.1728e-58)	1.1729e-78 (8.2620e-79)	3.3911e-97 (3.0445e-97)	2.3591e-116 (3.2080e-116)
Griewank	0.0121 (0.0124)	7.5658e-07 (4.1393e-06)	0 (0)	0 (0)	0 (0)
Rastrigin	0.0097 (0.0162)	6.0583e-010 (3.3181e-009)	0 (0)	0 (0)	0 (0)
Ackley	1.2475e-004 (2.0417e-004)	3.5468e-14 (3.9510e-15)	3.4284e-14 (4.6275e-15)	3.1442e-14 (3.3118e-15)	3.0731e-14 (2.0010e-15)
	(1.2, 0.8)	(1.4, 0.6)	(1.6, 0.4)	(1.8, 0.2)	(2.0, 0)
Sphere	1.4067e-130 (1.4790e-130)	2.1038e-137 (4.2126e-137)	4.5502e-140 (9.0476e-140)	6.2978e-140 (1.1991e-139)	7.7552e-134 (1.1756e-133)
Griewank	0 (0)	0 (0)	0 (0)	1.4297e-08 (7.8310e-08)	2.4898e-04 (0.0013)
Rastrigin	0 (0)	0 (0)	0 (0)	0 (0)	0 (0)
Ackley	2.9665e-14 (2.3511e-15)	2.9428e-14 (2.7174e-15)	2.9428e-15 (1.9755e-15)	3.0020e-14 (2.1681e-15)	3.0139e-14 (1.7906e-15)

4.2 Comparison Between ABC/Current-To-Best/1 And Original ABC

In the second experiment, parameters are arranged below: population size SN is 100, limit is SN/2*D. All benchmark functions listed in Table 1 are conducted for different dimensions. Each of the experiments was run 30 times independently. The means and standard deviations of the experiments comparing original ABC with that of we propose are reported in Table 3.

From the Table 3, we can see clearly that ABC/current-to-best/1 displays preferable ability of searching optimization in most cases through the searching space. In order to explain convergence speed more visually, we choose several benchmark functions to illustrate it in Figure 2 - 7.

4.3 ABC/Current-To-Best/1 Vs. Other Pre-Existing Improved ABC

In this part, we will assess the performance of what we propose with GABC [13], ABC/best/1, ABC/best/2[17], EABC [19]. The setting of parameters is the same as [13]. The result of the experiment is listed in Table 4 below.

It is distinct that there is better result on Rosebrock and Sphere test functions and the others keep similarly consequence. As a whole, ABC/current-to-best/1 has been demonstrated as good performance compared with original ABC algorithm in Table 4.



Table 3. The Performance Comparison Of ABC And ABC/Current-To-Best/l

Fun	D	G	ABC		ABC/current-to-best/l	
			(mean)	(std)	(mean)	(std)
F1	30	1000	0	0	0	0
	60	2000	0	0	0	0
F2	30	1000	6.99e-10	5.91e-10	1.5150e-030	1.1045e-27
	60	2000	1.94e-09	8.33e-10	4.8462e-025	2.4576e-24
F3	30	1000	5.1976e-13	4.3798e-13	1.4495e-025	9.6960e-026
	60	2000	4.4281e-12	3.3042e-12	1.2956e-023	8.0970e-024
F4	30	1000	1.01e-01	2.44e-02	0.0402	0.0081101
	60	2000	2.58e-01	2.92e-02	0.1179	0.012609
F5	5	2000	1.5026e-008	2.3103e-008	1.1409e-012	4.1795e-012
F6	2	2000	-1.0000	5.1531e-008	-1	5.1531e-09
F7	2	2000	2.9632e-016	2.0788e-016	3.3994e-048	1.4509e-047
F8	4	2000	1.17e-01	6.94e-02	0.1e-04	9.9096e-04
F9	10	2000	-209.9540	0.0372	-209.8984	0.0070
F10	30	1000	2.36e-06	8.32e-07	5.0520e-017	1.6848e-15
	60	2000	8.30e-06	8.93e-07	3.4634e-015	7.1907e-014
F11	3	1000	3.93e-02	3.11e-02	2.3661e-008	4.5290e-06
	4	2000	3.21e-02	3.26e-02	1.2443e-007	1.7276e-05
F12	30	1000	0.0153	0.0089	0.0103	0.14299
	60	2000	0.0335	0.0203	0.0214	0.32399
F13	2	2000	0	0	0	0
F14	2	2000	4.7386e-018	4.6731e-018	0	0
F15	30	1000	6.63e-03	1.71e-02	1.3074e-013	1.5380e-13
	60	2000	3.03e-01	4.53e-01	2.6441e-010	1.4324e-09
F16	30	1000	2.05e+02	1.63e+02	0	0
	60	2000	6.93e+02	1.39e+02	1.2164e-12	1.3436e-11
F17	2	2000	3.7007e-018	1.4084e-017	0	0
F18	2	2000	-1.0316	6.7122e-016	-1.0316	5.4546e-16
F19	2	2000	0	0	0	0
F20	2	2000	3.6822e-016	2.7793e-016	0	0
F21	2	2000	3.0000	1.5472e-015	2.6950	1.1662e-015
F22	30	1000	8.73e-09	1.47e-08	2.3700e-013	9.5669e-09
	60	2000	4.46e-09	6.68e-09	1.9114e-12	6.9137e-12
F23	30	1000	1.02e-05	4.15e-06	2.1521e-15	7.2099e-13
	60	2000	2.05e-05	5.54e-06	1.0075e-15	2.1603e-14
F24	30	1000	3.72e-09	1.79e-09	2.9044e-032	1.5136e-29
	60	2000	1.06e-08	6.25e-09	8.8286e-029	4.0155e-28

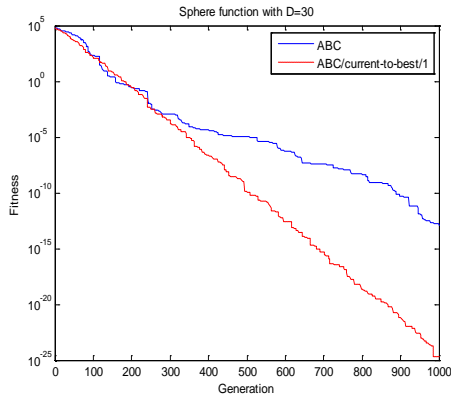


Figure 2: Convergence Curves For Sphere Function

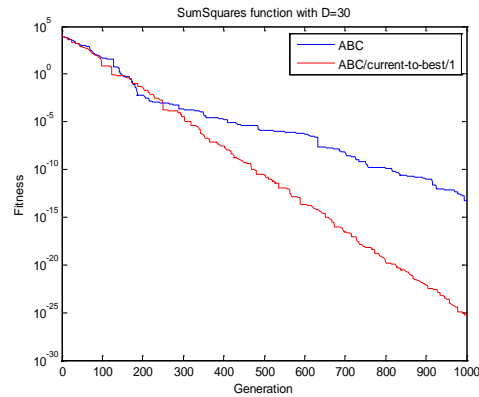


Figure 3: Convergence Curves For Sumsquares Function

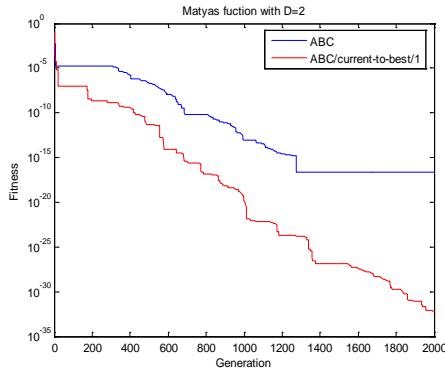


Figure 4: Convergence Curves For Matyas Function

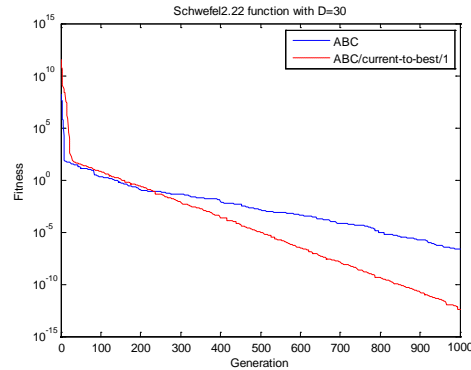


Figure 5: Convergence Curves For Schwefel2.22 Function

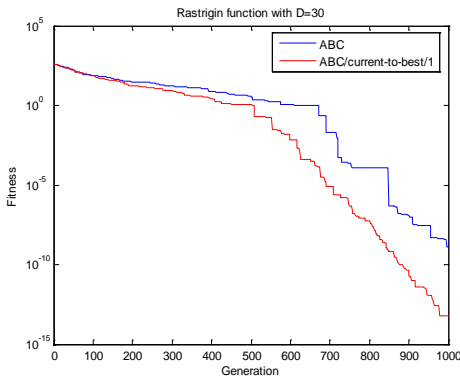


Figure 6: Convergence Curves For Rastrigin Function

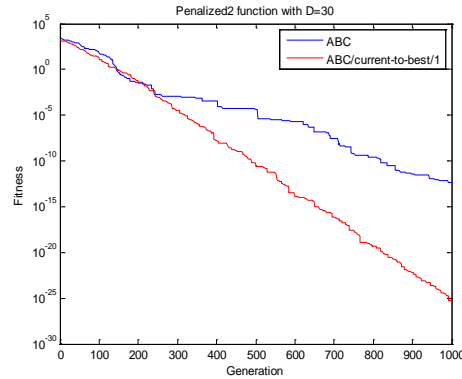


Figure 7: Convergence Curves For Penalized2 Function



Table 4. Performance Comparison Between ABC/Current-To-Best/1 And Pre-Existing Improved ABC

Algorithm	Schaffer				Rosebrock			
	D=2		D=3		D=2		D=3	
	Mean	Std	Mean	Std	Mean	Std	Mean	Std
GABC	0	0	1.85e-18	1.01e-17	1.68e-04	4.42e-04	2.65e-03	2.22e-03
EABC	0	0	2.79e-07	2.24e-07	4.63e-04	4.57e-04	1.20e-02	7.06e-03
ABC/best/1	0	0	0	0	4.99e-06	8.22e-06	5.52e-06	3.03e-06
ABC/best/2	0	0	3.56e-06	1.27e-06	4.42e-04	2.39e-04	9.90e-04	6.92e-04
ABC/current-to-best/1	0	0	0	0	3.50e-16	1.53e-15	3.34e-11	1.62e-10
	Sphere				Griewank			
	D=30		D=60		D=30		D=60	
	Mean	Std	Mean	Std	Mean	Std	Mean	Std
GABC	4.17e-16	7.36e-17	1.43e-15	1.37e-16	2.96e-17	4.99e-17	7.54e-16	4.12e-16
EABC	1.67e-16	2.70e-16	1.41e-15	1.82e-15	4.90e-14	7.31e-03	4.19e-14	9.05e-03
ABC/best/1	1.1e-150	1.4e-150	4.40e-69	2.56e-69	0	0	0	0
ABC/best/2	1.7e-126	2.7e-126	3.72e-58	2.67e-58	0	0	0	0
ABC/current-to-best/1	4.55e-160	9.05e-157	3.92e-72	3.13e-70	0	0	0	0
	Rastrigin				Ackley			
	D=30		D=60		D=30		D=60	
	Mean	Std	Mean	Std	Mean	Std	Mean	Std
GABC	1.32e-14	2.44e-14	3.52e-13	1.24e-13	3.21e-14	3.25e-15	1.66e-13	2.21e-14
EABC	9.97e-15	3.87e-15	7.51e-13	6.15e-13	1.22e-10	4.86e-11	1.55e-07	2.84e-08
ABC/best/1	0	0	0	0	1.72e-14	2.84e-15	6.62e-14	1.74e-15
ABC/best/2	0	0	0	0	2.50e-14	3.48e-15	7.12e-14	4.14e-15
ABC/current-to-best/1	0	0	0	0	2.94e-14	1.98e-15	7.34e-14	4.44e-15

5. CONCLUSION

In this paper, we modify the searching strategies of Artificial Bee Colony algorithm at the employed and onlooker bees' stage. The modification is inspired by DE and introduces not only the best solution at the current generation but also stochastic perturbation. We can get better balance between exploration and exploitation by adjusting the amplitude of the perturbation f_2 and f_2 . It is clear that the improved method we propose with suitable parameters can enhance the ability of searching optimization effectively by testing a group of 24 benchmark functions.

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