

SIMULATION FOR VEHICLE ACTIVE SUSPENSION CONTROL BASED ON DIFFERENT FEEDBACK PARAMETERS

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ABSTRACT

A half-car model with four DOF was established to simulate the system. On the basis of this model, Self-adapt Parameters Fuzzy-PID control method of the active suspension system is described. In such a model, vehicle speed, vehicle body vertical acceleration, suspension dynamic deflection, the body vertical acceleration and suspension dynamic deflection integrated feedback were used respectively as the integrated feedback. The simulation results show that active suspension Self-adapt Parameters Fuzzy-PID control with the body vertical acceleration and suspension dynamic deflection as comprehensive feedback parameters compared with passive suspension can improve the ride comfort and driving stability in random excitation.

Keywords: *Vehicle, Active Suspension, Fuzzy PID Control, Ride Comfort*

1. INTRODUCTION

At present, vehicle suspension has obtained high performance damping effect by using optimal control method. Industrial countries have begun to study an active, semi-active suspension system based on vibration control in the 1970s. In the 1960s, foreign scholars have proposed the concept of active suspension. Industry developed in the 70's has been of active[1-2], semi-active[3-4] suspension system based on the active vibration control. Domestic and foreign scholars have applied optimal control[5-8], adaptive control[9-10], fuzzy control[11-12], artificial neural network[13-15] to vibration control of vehicle suspension system. Modern control theory has made vibration control technology of the suspension system more perfect.

In the paper, the 1/2 body with four degrees of freedom suspension model is established as the research foundation, because that the automobile active suspension system is time-varying and nonlinear characteristic. Based on classical PID control, the self-adapt parameters fuzzy-PID controller of active suspension is designed combined with fuzzy control theory. In the process of designing the control system, the feedback of control system makes use of the vehicle body acceleration and the suspension dynamic deflection as the integrated feedback input. The simulation

results show that this control method is better than the passive suspension.

2. MODEL OF SYSTEM

A simplified 1/2 model with four degrees of freedom is established to simulate the system as shown in figure 1. m_{1f} and m_{1r} are the front and back wheels quality; m_{2f} and m_{2r} are the front and rear axle assignment quality; m_2 is the vehicle body centroid allocated quality; z_{1f} and z_{2f} are the front and rear wheel displacement; z_{1r} and z_{2r} are the front and rear upper body displacement; z_c is the centroid displacement; z_{qf} and z_{qr} are the front and rear surface roughness displacement input; θ is the pitch angle; k_{1f} and k_{1r} are the front and rear elastic stiffness; k_{2f} and k_{2r} are the front, rear suspension spring stiffness; c_{2f} and c_{2r} are the front and rear suspension damping coefficient; L is the wheelbase; a is the distance of front axle to centroid; b is the distance of rear axle to centroid; u_f and u_r are the damping force generated by variable damping shock absorber.

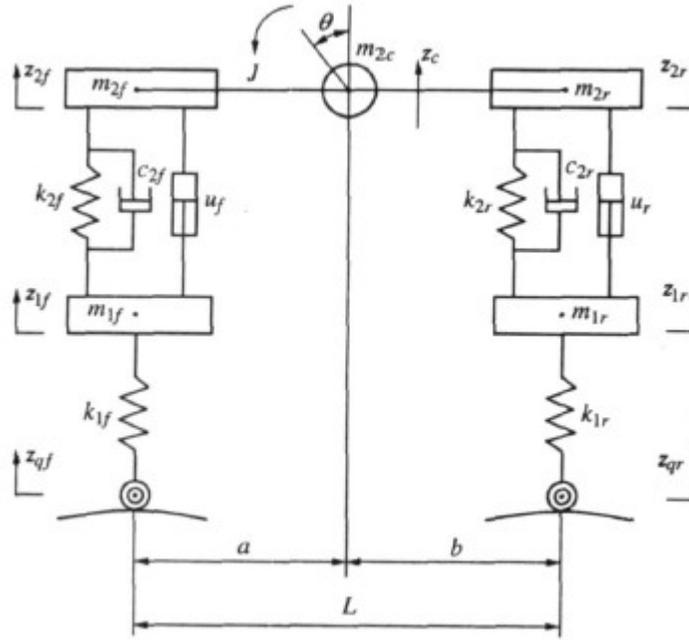


Figure 1: Model Of 1/2 Body With Four DOF

The dynamics equation of system are

$$\begin{cases} J\ddot{\theta} + b[k_{2r}(z_{2r} - z_{1r}) + c_{2r}(\dot{z}_{2r} - \dot{z}_{1r}) + u_r] - a[k_{2f}(z_{2f} - z_{1f}) + c_{2f}(\dot{z}_{2f} - \dot{z}_{1f}) + u_f] = 0 \\ m_2\ddot{z}_c + k_{2f}(z_{2f} - z_{1f}) + c_{2f}(\dot{z}_{2f} - \dot{z}_{1f}) + u_f + k_{2r}(z_{2r} - z_{1r}) + c_{2r}(\dot{z}_{2r} - \dot{z}_{1r}) + u_r = 0 \\ m_{1f}\ddot{z}_{2f} - k_{1f}(z_{1f} - z_{qf}) + c_{2f}(\dot{z}_{1f} - \dot{z}_{2f}) + k_{2f}(z_{1f} - z_{2f}) - u_f = 0 \\ m_{1r}\ddot{z}_{2r} - k_{1f}(z_{1r} - z_{qr}) + c_{2f}(\dot{z}_{1r} - \dot{z}_{2r}) + k_{2r}(z_{1r} - z_{2r}) - u_r = 0 \end{cases} \quad (1)$$

The equation of state and input equation are established as follows

$$\begin{cases} \ddot{X} = AX + BU \\ Y = CX + DU \end{cases} \quad (2)$$

In which

$$X = [\dot{z}_c \quad \dot{\theta} \quad z_{2f} - z_{1f} \quad z_{2r} - z_{1r} \quad z_{1f} \quad z_{1r} \quad \dot{z}_{1f} \quad \dot{z}_{1r}]^T,$$

$$U = [z_{qf} \quad z_{qr} \quad u_f \quad u_r]^T,$$

$$Y = [\dot{z}_c \quad \ddot{\theta} \quad z_{2f} - z_{1f} \quad z_{2r} - z_{1r} \quad k_{1f}(z_{1f} - z_{qf}) \quad k_{1r}(z_{1r} - z_{qr}) \quad \ddot{z}_{1f} \quad \ddot{z}_{1r}]^T.$$

$$A = \begin{bmatrix} \frac{-(c_{2f} + c_{2r})}{m_2} & \frac{-(ac_{2f} + bc_{2r})}{m_2} & \frac{-k_{2f}}{m_2} & \frac{-k_{2r}}{m_2} & 0 & 0 & \frac{c_{2f}}{m_2} & \frac{c_{2r}}{m_2} \\ \frac{ac_{2f} - bc_{2r}}{J} & \frac{-(a^2c_{2f} - b^2c_{2r})}{J} & \frac{ak_{2f}}{J} & \frac{-bk_{2r}}{J} & 0 & 0 & \frac{-ac_{2f}}{J} & \frac{bc_{2r}}{J} \\ 1 & -a & 0 & 0 & 0 & 0 & -1 & 0 \\ 1 & b & 1 & 0 & 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ \frac{c_{2f}}{m_{1f}} & \frac{-ac_{2f}}{m_{1f}} & \frac{k_{2f}}{m_{1f}} & 0 & \frac{-k_{1f}}{m_{1f}} & 0 & \frac{-c_{2f}}{m_{1f}} & 0 \\ \frac{c_{2r}}{m_{1r}} & \frac{bc_{2r}}{m_{1r}} & 0 & \frac{k_{2r}}{m_{1r}} & 0 & \frac{-k_{1r}}{m_{1r}} & 0 & \frac{-c_{2r}}{m_{1r}} \end{bmatrix};$$

$$B = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & \frac{k_{1f}}{m_{1f}} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{k_{1r}}{m_{1r}} \\ \frac{1}{m_2} & \frac{-a}{J} & 0 & 0 & 0 & 0 & \frac{1}{m_{1f}} & 0 \\ \frac{1}{m_2} & \frac{b}{J} & 0 & 0 & 0 & 0 & 0 & \frac{-1}{m_{1r}} \end{bmatrix};$$

$$D = \begin{bmatrix} 0 & 0 & 0 & 0 & -k_{1f} & 0 & \frac{k_{1f}}{m_{1f}} & 0 \\ 0 & 0 & 0 & 0 & 0 & -k_{1r} & 0 & \frac{k_{1r}}{m_{1r}} \\ \frac{1}{m_2} & \frac{-a}{J} & 0 & 0 & 0 & 0 & \frac{1}{m_{1f}} & 0 \\ \frac{1}{m_2} & \frac{b}{J} & 0 & 0 & 0 & 0 & 0 & \frac{-1}{m_{1r}} \end{bmatrix};$$

$$C = \begin{bmatrix} \frac{-(c_{2f} + c_{2r})}{m_2} & \frac{-(ac_{2f} + bc_{2r})}{m_2} & \frac{-k_{2f}}{m_2} & \frac{-k_{2r}}{m_2} & 0 & 0 & \frac{c_{2f}}{m_2} & \frac{c_{2r}}{m_2} \\ \frac{ac_{2f} - bc_{2r}}{J} & \frac{-(a^2c_{2f} - b^2c_{2r})}{J} & \frac{ak_{2f}}{J} & \frac{-bk_{2r}}{J} & 0 & 0 & \frac{-ac_{2f}}{J} & \frac{bc_{2r}}{J} \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & k_{1f} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & k_{1r} & 0 & 0 \\ \frac{c_{2f}}{m_{1f}} & \frac{-ac_{2f}}{m_{1f}} & \frac{k_{2f}}{m_{1f}} & 0 & \frac{-k_{1f}}{m_{1f}} & 0 & \frac{-c_{2f}}{m_{1f}} & 0 \\ \frac{c_{2r}}{m_{1r}} & \frac{bc_{2r}}{m_{1r}} & 0 & \frac{k_{2r}}{m_{1r}} & 0 & \frac{-k_{1r}}{m_{1r}} & 0 & \frac{-c_{2r}}{m_{1r}} \end{bmatrix}.$$

3. MODEL OF SYSTEM

Fuzzy controller design mainly includes the structure choose of fuzzy controller, the fuzzy rules to selection, fuzzy controller and fuzzy method and the domain fuzzy of controller input and output variables.

3.1 Structure of Self-adapt Parameters Fuzzy-PID Controller

The paper selects the vehicle body vertical acceleration and the suspension dynamic deflection as the integrated feedback input. Fuzzy controller takes their deviation e , e_1 and its change

rate \dot{c} , \dot{c}_1 as input, correction parameters $\Delta k_p, \Delta k_I, \Delta k_D$ and $\Delta k_{p1}, \Delta k_{I1}, \Delta k_{D1}$ as output. The PID controller output parameters k_p, k_I, k_D and k_{p1}, k_{I1}, k_{D1} are shown in formula 3-5 and structure diagram is shown in figure 2.

$$k_p = k'_p + \Delta k_p, \quad k_{p1} = k'_{p1} + \Delta k_{p1} \quad (3)$$

$$k_I = k'_I + \Delta k_I, \quad k_{I1} = k'_{I1} + \Delta k_{I1} \quad (4)$$

$$k_D = k'_D + \Delta k_D, \quad k_{D1} = k'_{D1} + \Delta k_{D1} \quad (5)$$

3.2 Fuzzy Subset of Input and Output Variables

For input and output variables, fuzzy state is used by seven fuzzy sets, both for the {NB, NM, NS, ZE, PS, PM, PB}. The fuzzy domain e and e_1 are (-0.5,0.5). The fuzzy domain of error change rate c and c_1 are (-0.5, 0.5). The fuzzy domain $\Delta k_p, \Delta k_{p1}, \Delta k_{I1}$ and $\Delta k_I, \Delta k_D, \Delta k_{D1}$ are in (-0.5, 0.5). Fuzzy subsets of input variable and output variable use triangular membership functions.

3.3 Fuzzy control rule

The fuzzy control rules are an important component of fuzzy controller. It is described by means of the input and output of a controller relationship between them, namely, the fuzzy relationship between them. The fuzzy control rule is based on people's thinking, with the method of fuzzy reasoning is given. In the paper, the fuzzy controller with 2 inputs is described by 2 language fuzzy sets, forming 49 control rules. The fuzzy control rule table of three parameters are shown in figure 4.1-4.3 ($\Delta k_{p1}, \Delta k_{I1}$ and Δk_{D1} are samed as $\Delta k_p, \Delta k_I$ and Δk_D).

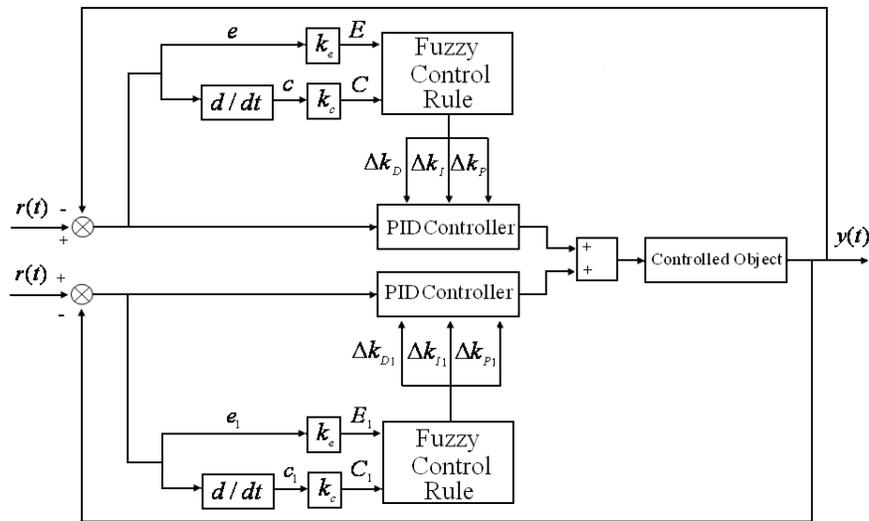


Figure 2: Self-Adapt Parameters Fuzzy-PID Control Principle Diagram

Table 1: Fuzzy Control Rule Table Of Δk_p

Δk_p	C						
	NB	NM	NS	ZO	PS	PM	PB
NB	PB	PB	PM	PM	PS	ZO	ZO
NM	PB	PB	PM	PS	PS	ZO	NS
NS	PM	PM	PM	PS	ZO	NS	NS
ZO	PM	PM	PS	ZO	NS	NM	NM
PS	PS	PS	ZO	NS	NS	NM	NM
PM	PS	ZO	NS	NM	NM	NM	NB
PB	ZO	ZO	NM	NM	NM	NB	NB

Table 2: Fuzzy Control Rule Table Of Δk_f

Δk_f		C						
		NB	NM	NS	ZO	PS	PM	PB
E	NB	NB	NB	NM	NM	NS	ZO	ZO
	NM	NB	NB	NM	NS	NS	ZO	ZO
	NS	NB	NM	NS	NS	ZO	PS	PS
	ZO	NM	NM	NS	ZO	PS	PM	PM
	PS	NM	NS	ZO	PS	PS	PM	PB
	PM	ZO	ZO	PS	PS	PM	PB	PB
	PB	ZO	ZO	PS	PM	PM	PB	PB

Table 3: Fuzzy Control Rule Table Of Δk_D

Δk_D		C						
		NB	NM	NS	ZO	PS	PM	PB
E	NB	PS	NS	NB	NB	NB	NM	PS
	NM	PS	NS	NB	NM	NM	NS	ZO
	NS	ZO	NS	NM	NM	NS	NS	ZO
	ZO	ZO	NS	NS	NS	NS	NS	ZO
	PS	ZO						
	PM	PB	NS	PS	PS	PS	PS	PB
	PB	PB	PM	PM	PM	PS	PS	PB

4. MODEL OF SYSTEM

The suspension parameters of SANTANA 2000 car are shown in table 4.

Table 4: Parameters Of SANTANA 2000

Name	Value	Company
m_{1f}	98	kg
m_{1r}	98	kg
m	975.37	kg
J	1647	kg · m ²
k_{1f}	604.69	kN/m
k_{1r}	985.97	kN/m
k_{2f}	45.48	kN/m
k_{2r}	52.29	kN/m
c_{2f}	2546.5	N · s/m
c_{2r}	2840.6	N · s/m
a	1.1135	m
b	1.5415	m

When the vehicle travels on grade B Road and $v=50\text{m/s}$, road roughness coefficient $S_q(n_0) = 64 \times 10^{-6} \text{m}^2 / \text{m}^{-1}$, $n_0 = 0.1 \text{m}^{-1}$, Velocity spectrum density is a white noise, $S_q(f) = (2\pi f)^2 S_q(f) = 4\pi^2 n_0^2 S_q(n_0) v$, The white noise input is regarded as random road displacement excitation. Simulation study on Self-adapt Parameters Fuzzy-PID control of active suspension with acceleration feedback(ACC), speed feedback(Speed), suspension dynamic

deflection feedback(SDD) and acceleration and suspension dynamic deflection comprehensive feedback(A+S). Body pitch angle acceleration response, the body acceleration, wheel dynamic load response, front suspension dynamic deflection response, rear wheel dynamic load response and rear suspension dynamic deflection are simulation. Simulation comparison results of response are shown in figures 3-8.

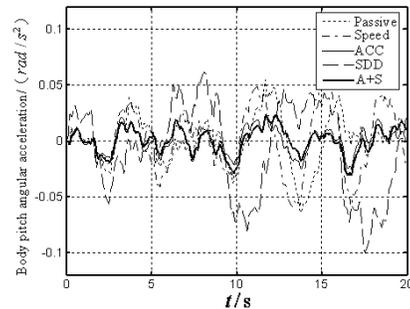


Figure 3: Time Course Diagram Of Body Pitch Angular Acceleration

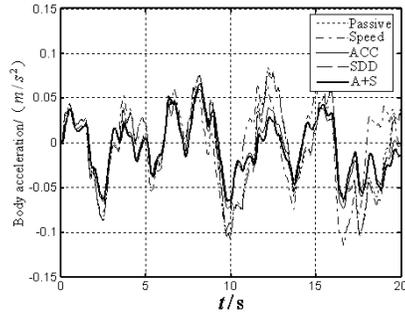


Figure 4: Time Course Diagram Of Body Acceleration

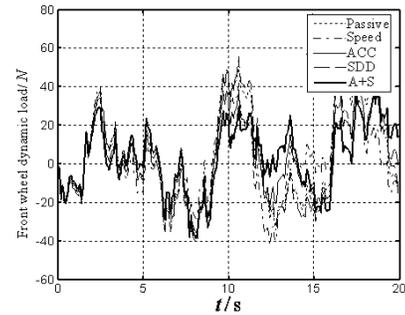


Figure 5: Time Course Diagram Of Front Wheel Dynamic Load

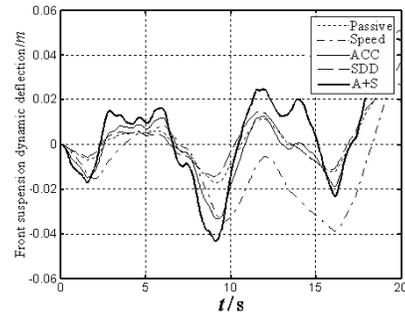


Figure 6: Time Course Diagram Of Front Suspension Dynamic Deflection

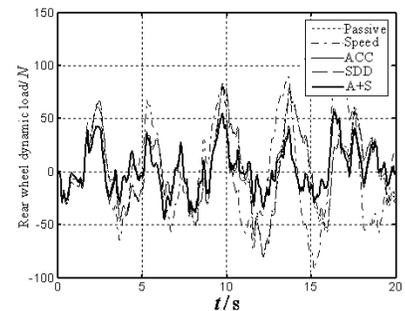


Figure 7: Time Course Diagram Of Rear Wheel Dynamic Load

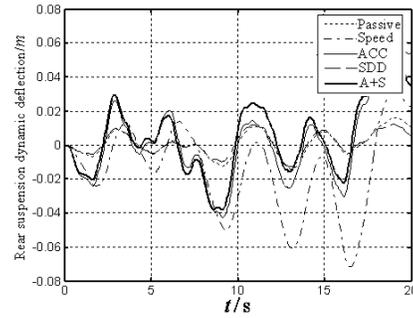


Figure 8: Time Course Diagram Of Rear Suspension Dynamic Deflection

Table 5: Performance Improvement Analysis

Performance parameters	Performance improvement analysis(A+S)
Maximum value of body pitch angular acceleration	58.74%
Standard deviation of body pitch angular acceleration	46.94%
Maximum value of body acceleration	17.76%
Standard deviation of body acceleration	31.62%
Maximum value of front wheel dynamic load	37.96%
Standard deviation of front wheel dynamic load	30.39%
Maximum value of rear wheel dynamic load	32.74%
Standard deviation of rear wheel dynamic load	38.80%

As can be seen from table 5, compared with passive suspension, body pitch angular acceleration, body acceleration, front wheel dynamic load, front wheel dynamic load and rear wheel dynamic load of Self-adapt Parameters Fuzzy-PID active suspension, are significantly reduced. The car's ride and handling stability is greatly improved. The defect is that front and rear suspension dynamic deflection has certain increases compared with passive suspension. The maximum are 0.053m and 0.049m. The limit of the car suspension travel is 0.07-0.09m. As long as the suspension dynamic deflection is in the limit travel of the suspension, the suspension dynamic deflection increases in exchange for other vehicle performance improved, such as ride comfort.

5. CONCLUSION

In the paper, body pitch angular acceleration, vehicle body vertical acceleration and wheel dynamic load were the main control objectives. Taking the body vertical acceleration and suspension dynamic deflection integrated feedback as a comprehensive feedback input is feasible and



effective, and the effect of the comprehensive control is good. Compared with the passive suspension, the design of active suspension self-adaptive fuzzy PID control can reduce the body pitch angular acceleration, body vertical acceleration, wheel dynamic load. The vehicle ride comfort and handling stability have been improved obviously, which has achieved the anticipated goal and effect.

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