

# MODIFIED PARTICLE SWARM OPTIMIZATION FOR OPTIMIZATION PROBLEMS

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## ABSTRACT

In the paper a modified particle swarm optimization (MPSO) is proposed where concepts from firefly algorithm (FA) are borrowed to enhance the performance of particle swarm optimization (PSO). The modifications focus on the velocity vectors of the PSO, which fully use beneficial information of the position of particles and increase randomization item in the PSO. Finally, the performance of the proposed algorithm is compared with that of the PSO-TVIW. Simulation results demonstrate the effectiveness of the proposed algorithm.

**Keywords:** *Particle Swarm Optimization; Firefly Algorithm; Meta-Heuristic Algorithm*

## 1. INTRODUCTION

The optimization problems frequently arise in almost every field of the natural sciences and the engineering technology. During the last few decades, Nature-inspired Meta-heuristic algorithms have been proposed for solving the optimization problems. There are many different meta-heuristic algorithms for the optimization problems, such as differential evolution (DE) [1], ant colony optimization (ACO) [2], firefly algorithm [3-4], and so on.

Particle swarm optimization (PSO), proposed by Kennedy and Eberhart [5-6] in 1995 is a new, self-adaptive global optimization algorithm based on the swarm behavior of birds and fish. In the PSO, a potential solution for a given problem is considered as a particle, a particle flies through a D-dimensional, real-valued search space and adjusts its position vector according to its own experience and other particles'. The PSO approach is becoming very popular due to its simplicity of implementation and ability to quickly converge to a reasonably good solution; it has been successfully applied in a vast range of problems [5-8]. To improve the performance of the PSO, Hong-qi Li et al. [9] proposed a novel hybrid particle swarm

optimization algorithm combined with harmony search for high dimensional optimization problems, O. Begambre et al. [10] proposed a hybrid particle swarm optimization – simplex algorithm for structural damage identification, Changsheng Zhang et al. [11] proposed a novel hybrid differential evolution and particle swarm optimization algorithm for unconstrained optimization.

Firefly algorithm (FA) is a new meta-heuristic algorithm which is inspired from social behavior of fireflies in nature. This algorithm was developed recently by Xin-She Yang at Cambridge University. It uses three idealized rules: All fireflies are unisex and can be attracted by other fireflies; attractiveness of each firefly is proportional to their brightness and brightness of each firefly is determined by evaluating objective function. Further details about the FA are given in [3-4].

In order to improve the search capability of PSO, the purpose of this paper is to present a PSO based on the part thought of firefly algorithm (MPSO). To show the performance of this algorithm, MPSO is applied to four standard benchmark functions. Numerical results reveal that the proposed algorithm is a powerful search algorithm for optimization problems.



The remainder of the paper is organized as follows: Section 2 describes the PSO. The proposed approach (MPSO) is presented in Section 3. Results of the experiments are presented and discussed in Section 4. Finally, Section 5 concludes the paper.

**2. THE PARTICLE SWARM ALGORITHM**

In PSO, every particle has a position vector  $x = (x_1, x_2, \dots, x_D)$  and a velocity vector  $v = (v_1, v_2, \dots, v_D)$ .

At each time step  $t$ , the velocity of particle  $i$  is updated according to Eq.1 and then its position is updated according to Eq.2.

$$v_i(t+1) = \omega v_i(t) + c_1 r_1 (pbest_i - x_i(t)) + c_2 r_2 (gbest - x_i(t)) \tag{1}$$

$$x_i(t+1) = x_i(t) + v_i(t+1) \tag{2}$$

Where  $w$  is the inertial weight, and  $c_1$  and  $c_2$  are positive acceleration coefficients used to scale the contribution of cognitive and social components, respectively.  $pbest_i$  is the best position that particle  $i$  has been visited.  $gbest$  is the best position found by all particles in the swarm.  $r_1$  and  $r_2$  are uniform random number in  $[0,1]$ ,  $v_{id} \in [-V_{max}, V_{max}]$ , and  $V_{max}$  specify maximum of velocity.

PSO can be summarized as the pseudo code shown in Figure 1.

```

begin
initialize the particle population  $x_i$  ( $i=1,2,\dots,n$ ) and  $v_i$ 
while ( $t < \text{Max number of Generations}$ )
evaluate the fitness  $f(x)$ ,  $x = (x_1, \dots, x_D)$ 
update  $pbest_i$  and  $gbest$ 
calculate new velocity according to Eq.1
update the position according to Eq.2
end while
end
    
```

Figure 1 Particle Swarm Optimization

**3. THE MODIFIED PARTICLE SWARM ALGORITHM**

In this section, the part thought of FA is used in the PSO to accelerate convergence speed and also

to enhance its capability for handling optimization problems.

The MPSO has exactly the same steps as the PSO with the exception that velocity vector is modified as follows:

In the MPSO, the distance between  $x_i$  and  $pbest_i$ , respectively, is the Cartesian distance

$$r_{px} = \|pbest_i - x_i(t)\| = \sqrt{\sum_{k=1}^D (pbest_{i,k} - x_{i,k})^2} \tag{3}$$

The distance between  $x_i$  and  $gbest$ , respectively, is the Cartesian distance

$$r_{gx} = \|gbest - x_i(t)\| = \sqrt{\sum_{k=1}^D (gbest_k - x_{i,k})^2} \tag{4}$$

The velocity vectors  $v$  of the PSO is randomly mutated by using Eq.5.

$$v_i(t+1) = \begin{cases} \omega v_i(t) + c_1 r_1 (pbest_i - x_i(t)) + c_2 r_2 (gbest - x_i(t)), & r_3 \leq p_a \\ \omega v_i(t) + r_1 e^{(-r_{px}^2)} (pbest_i - x_i(t)) + r_2 e^{(-r_{gx}^2)} (gbest - x_i(t)) + \alpha(r - \frac{1}{2}) \\ , else \end{cases} \tag{5}$$

Where the third term is randomization with the control parameter  $\alpha$ , which makes the exploration of the search space more efficient.  $p_a$  is a mutation probability,  $r_3$  is uniform random number in  $[0,1]$ , the proposed algorithm fully uses beneficial information of the solutions to modify the velocity vector  $v$ . Intuitively, this modification allows the MPSO to work efficiently in both continuous and discrete problems.

**4. EXPERIMENTS**

**4.1 Benchmarks**

In this section, four well known benchmark functions for minimization are chosen to test the performance of MPSO in comparison with PSO-TVIW [7]. The test functions are listed below:

Sphere function

$$f(x) = \sum_{i=1}^D x_i^2 \tag{6}$$



Rosenbrock function

$$f(x) = \sum_{i=1}^{D-1} [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2] \quad (7)$$

Rastrigrin function

$$f(x) = \sum_{i=1}^D [x_i^2 - 10 \cos(2\pi x_i) + 10] \quad (8)$$

Griewank function

$$f(x) = \frac{1}{4000} \sum_{i=1}^D x_i^2 - \prod_{i=1}^D \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1 \quad (9)$$

Search space ranges of the above benchmark functions for the experiments are listed in Table 1.

Table 1 Search Space For Each Test Functions

Function	Search space
Sphere	$-5.12 \leq x_i \leq 5.12$
Rosenbrock	$-30 \leq x_i \leq 30$
Rastigrin	$-5.12 \leq x_i \leq 5.12$
Griewank	$-600 \leq x_i \leq 600$

#### 4.2 Algorithm's Settings And Experimental Results

To evaluate the performance of the proposed PSO, all common parameters of PSO-TVIV [7] and MPSO are set the same to have a fair comparison. All functions were implemented in 30 dimensions. The results reported in this section are mean and standard dev. over 50 simulations. The maximum number of generations (Ng) was set to 2,000 for two algorithms, it is good to limit the  $V_{max}$  to the upper value of the range of search,  $D=40$ . For the MPSO,  $p_a=0.9$ ,  $w = (0.9 - 0.4) \frac{Ng - t}{Ng} + 0.4$ ,

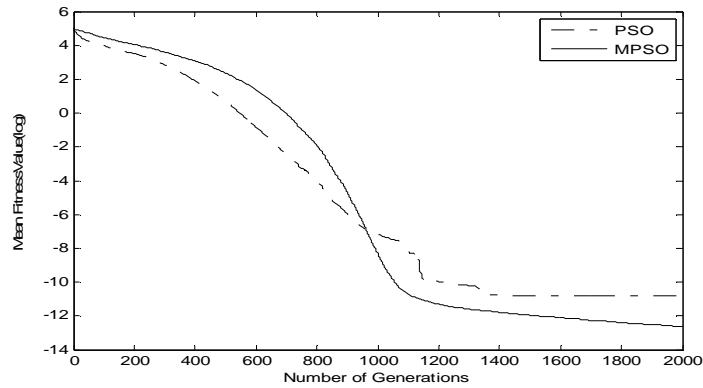
$$c_1 = c_2 = 2.$$

Table 2 summarizes value data obtained by applying the two approaches to the benchmark

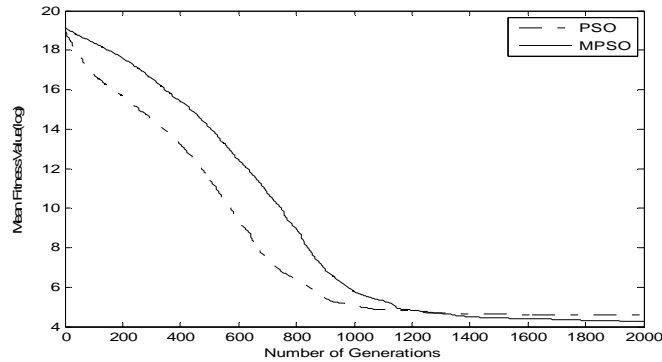
functions. As seen, for Sphere function, Rosenbrock function and Griewank function, the result generated by MPSO is better than those generated by PSO, for Rastigrin function, MPSO slightly outperformed PSO. It can be concluded that the MPSO outperformed PSO-TVIV in all four benchmark functions when the pre-defined number of generations is completed. The modified PSO that combines the distance information and randomization term is proved to be correct and effective in converging to the global optimal.

Table 2 Shows The Mean And STDEV. Of The Benchmark Function Optimization Results

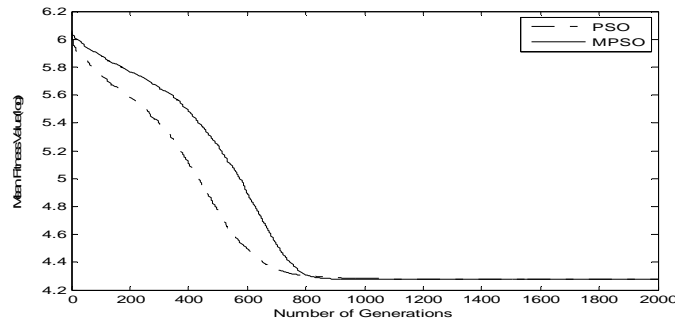
Function	Method	Mean	Stdev.
Sphere	PSO	2.01554830096	1.35034908313
	-	0248e-5	9055e-4
	TVI	3.27178869303	5.32115488952
	W	4994e-6	5446e-7
Rosenbrock	PSO	1.00029514893	1.18761895175
	-	9649e+2	5061e+2
	TVI	70.6183697610	1.10822347459
	W	29768	0161e+2
Rastigrin	PSO	72.2543077481	18.3263121401
	-	91820	93487
	TVI	72.1946469048	16.0408520628
	W	94668	08550
Griewank	PSO	0.10133779637	0.17678038033
	-	7739	0072
	TVI	0.06879507945	0.14498015321
	W	9886	4513
MPSO	PSO	0.10133779637	0.17678038033
	-	7739	0072
	TVI	0.06879507945	0.14498015321
	W	9886	4513



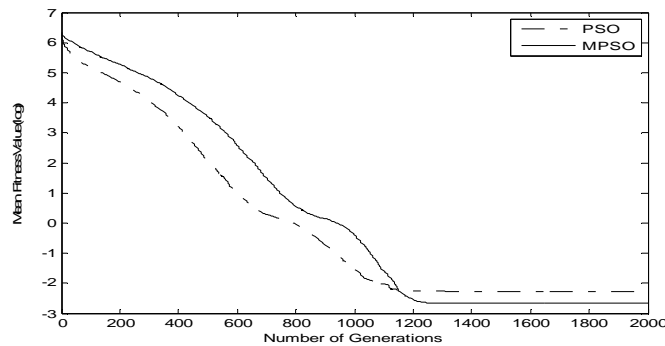
(a)



(b)



(c)



(d)

Figure 2 Variation Of The Mean That Are Best Fit With Time. (A) Sphere Function. (B) Rosenbrock Function. (C) Rastigrin Function. (D) Griewank Function.



Figure 2 show the search progress of the average values found by the two algorithms over 50 runs four functions, which plot the fitness values (log) against the number of generations. From Figure 2, it is clear that the MPSO converges significantly faster than PSO-TVIW for Sphere function, Rosenbrock function and Griewank function, the MPSO converges slightly faster than PSO-TVIW for Rastigrin function.

## 5. CONCLUSIONS

This paper proposes a new simple but effective and efficient modified PSO for continuous optimization problems. The results obtained show that by using the MPSO may yield better solutions than those obtained by using PSO-TVIW, and demonstrate the effectiveness and robustness of the proposed algorithm. In conclusion, my research work, therefore, suggests that the MPSO is potentially a powerful search and optimization technique for solving complex problems.

In this work, we only consider the unconstrained function optimization. Our future work consists on adding the diversity rules into MPSO for constrained optimization problems.

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