

## A METHOD FOR QUALITY POWER PROVIDER TO OPERATE IN DISTORTED SUPPLY CONDITION

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### ABSTRACT

Power Quality is a major concern within power industry and consumers. Poor quality of supply will affect the performance of customer equipment such as computers, microprocessors, adjustable speed drives, power electronic controllers, life saving equipment in hospitals, etc. and result in heavy financial losses to customers due to loss of production or breakdown in industries or loss of life in a hospital. The two major power quality disturbances are voltage sag and harmonic distortion. In this paper, a Quality Power Provider (QPP) based on voltage source inverter is modeled by simulation to compensate the power quality disturbances such as voltage sag and voltage harmonics in the distorted supply condition. The phase locked loop (PLL) is an important control unit of the QPP control scheme. To obtain accurate phase information and frequency of the input supply, the dqPLL method has been proposed. Simulation results based on MATLAB and PSCAD software are presented to verify the performance of the proposed QPP. QPP has improved the quality of power supply at the sensitive load end.

**Keywords:** *Voltage Sag, Harmonics, PLL, Dqpll, Double Frequency Component.*

### 1. INTRODUCTION

The main causes of voltage disturbances in power system are due to insulation failure, tree falling, bird contact, lightning or a fault on an adjacent feeder. These disturbances may be in the form of voltage sags, swells, interruptions and harmonics. However, harmonic distortion in power system is caused by non-linear loads [1]. Voltage disturbances will cause problems to the industrial equipments ranging from malfunctioning of equipments to complete plant shutdowns [2]. A QPP is designed based on three single-phase IGBTs H-bridge inverters which are connected to the distribution system by three injection transformers. The QPP is connected at the point of common coupling in series with the sensitive load and in parallel with a three-phase uncontrolled bridge rectifier acting as a non-linear load. The PLL is an important control unit used with the QPP, to obtain the phase and frequency information of the input supply voltage. The PLL is used to generate unit sine and cosine signals to compute the feedback and modulating control signals. It is difficult for the PLL to generate these unit vectors when the input supply voltage is distorted like unbalanced, presence of

harmonics, voltage sag and phase jump. The PLL has to track the phase information accurately under distorted supply conditions. Some methods have been proposed in the literature as in [3][4][5] for accurate phase angle tracking in distorted supply conditions. Each method has its own drawbacks. In this paper, the dqPLL method based on the dq method is developed to improve the performance of the PLL and QPP under distorted supply conditions. The performance of QPP is investigated in balanced and unbalanced fault conditions, harmonics distortion, and balanced and unbalanced fault conditions together with harmonics. Simulation results indicate an improved performance by the QPP.

### 2. MATHEMATICAL MODELING OF PLL

The PLL technique has been used, to synchronize with the incoming supply voltages and to maintain synchronization in spite of distortion or variations in the supply voltage frequency. The basic functional structure of PLL as shown in Fig. 1, comprises of a phase detector

(PD), a loop filter (LF), and a voltage-controlled oscillator (VCO). As shown in Fig. 1, VCO is represented as an integrator and  $e_{rr}$  is the error signal. Denoting the instantaneous phase as  $\theta$ ,

$$\frac{d\theta}{dt} = \omega$$

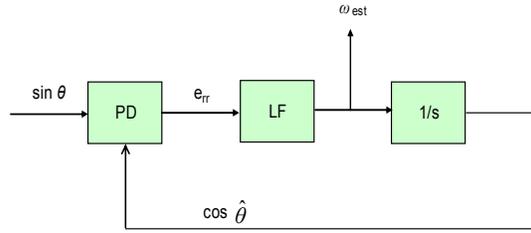


Fig. 1: Basic PLL functional structure

$$f = \frac{1}{2\pi} * \frac{d\theta}{dt}$$

Conversely, the phase is the integral of frequency, thus

$$\theta = \int \omega * dt = \int 2\pi f * dt$$

The three-phase balanced supply voltage is represented as in equation (1)

$$V_{sabc} = V_m \begin{bmatrix} \cos \theta \\ \cos(\theta - \frac{2\pi}{3}) \\ \cos(\theta + \frac{2\pi}{3}) \end{bmatrix} \quad (1)$$

where  $V_{sabc} = [V_{sa}, V_{sb}, V_{sc}]^T$

Transforming the source voltage equation (1) into stationary reference frame as in equation (2),

$$V_{\alpha\beta} = T_s * V_{sabc} \quad (2)$$

where  $V_{\alpha\beta} = [V_\alpha \ V_\beta]^T$ ,  $V_\alpha$  and  $V_\beta$  are the two-phase stationary reference frame voltages, and  $T_s$  is transform matrix given as in equation (3)

$$T_s = \frac{2}{3} \begin{bmatrix} 1 & -0.5 & -0.5 \\ 0 & -0.866 & 0.866 \end{bmatrix} \quad (3)$$

or

$$T_s = \begin{bmatrix} \frac{2}{3} & -\frac{1}{3} & -\frac{1}{3} \\ 0 & -\frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} \end{bmatrix}$$

In the synchronous reference frame with output  $\hat{\theta}$

$$V_{dq} = T(\hat{\theta}) * V_{\alpha\beta} \quad (4)$$

where  $V_{dq} = [V_d \ V_q]^T$  and  $T(\hat{\theta})$  is the rotating transformation matrix as in equation (7)

$$T(\hat{\theta}) = \begin{bmatrix} \cos \hat{\theta} & -\sin \hat{\theta} \\ \sin \hat{\theta} & \cos \hat{\theta} \end{bmatrix} \quad (5)$$

The d-axis voltage is derived and represented as  $u$  as in equation (6)

$$V_d = E_m \sin \delta = u \quad (6)$$

where  $E_m = -V_m$  and  $\delta = (\theta - \hat{\theta})$ . The angular frequency of PLL is represented as in equation (7)

$$\hat{\omega} = \frac{d\hat{\theta}}{dt} = G * u \quad (7)$$

where  $G$  is the gain of the loop filter. Assuming the phase difference  $\delta$  as small, and then simplifying equation (6) as in equation (8)

$$u \approx E_m \delta \quad (8)$$

The PLL is able to track the supply frequency  $\omega$  and the phase angle  $\theta$  accurately with properly design loop filter.

### 3. ANALYSIS OF SUPPLY IN UNBALANCED CONDITION

As shown in Fig. 1, the sinusoidal-based PD is essentially a signal multiplier. These PDs will generate an error signal based on the trigonometric relationship between the products of the two system measurements. This produces a steady-state error. This steady-state error includes the double frequency ripple. To filter out this double frequency ripple, loop bandwidth should be narrow. This also limits the noise. To filter out the double frequency term, the frequency response is important. To account for this double frequency term at steady-state, an additional low-pass filter is added before the LF to suppress this noise signal. The main drawback is a low value of phase margin of the loop which increases the tracking time and lowers the dynamic response. The phase margin indicates the robustness of the stability of the closed loop.

Normally, the phase margin should be around 60 degrees [6]. This means that the frequency at which the open and close loop gains meet, the phase angle is -120 degrees. That is,  $(-120^0 - (-180^0))$  equals 60 degrees. A phase margin of  $60^0$  allows fastest time when attempting to follow step input. Also, if the input supply voltage is distorted and unbalanced in a 50 Hz system, a ripple frequency of 100 Hz will appear in the d and q axis of the dq method along with the dc quantities which will result in error estimation of  $\theta$ .

#### 4. NEW PROPOSED dqPLL TECHNIQUE

The unbalanced supply phase voltages in symmetrical components are represented as in equation (9)

$$\bar{V}_{sabc} = \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} V_{a+} \\ V_{b+} \\ V_{c+} \end{bmatrix} + \begin{bmatrix} V_{a-} \\ V_{b-} \\ V_{c-} \end{bmatrix} + \begin{bmatrix} V_{a0} \\ V_{b0} \\ V_{c0} \end{bmatrix} \quad (9)$$

Using  $\alpha\beta$  transform,  $T_{\alpha\beta}$

$$\bar{V}_{\alpha\beta} = \begin{bmatrix} V_\alpha \\ V_\beta \end{bmatrix} = T_{\alpha\beta} \bar{V}_{abc} \quad (10)$$

$$\bar{V}_{\alpha\beta} = T_{\alpha\beta} \begin{bmatrix} V_{a+} \\ V_{b+} \\ V_{c+} \end{bmatrix} + T_{\alpha\beta} \begin{bmatrix} V_{a-} \\ V_{b-} \\ V_{c-} \end{bmatrix} + T_{\alpha\beta} \begin{bmatrix} V_{a0} \\ V_{b0} \\ V_{c0} \end{bmatrix} \quad (11)$$

representing

$$V_{a+} = V_+ \sin\theta_+; \quad V_{b+} = V_+ \sin(\theta_+ - \frac{2\pi}{3}); \quad V_{c+} = V_+ \sin(\theta_+ + \frac{2\pi}{3})$$

$$V_{a-} = V_- \sin\theta_-; \quad V_{b-} = V_- \sin(\theta_- + \frac{2\pi}{3}); \quad V_{c-} = V_- \sin(\theta_- - \frac{2\pi}{3})$$

then

$$\bar{V}_{\alpha\beta} = \begin{bmatrix} V_\alpha \\ V_\beta \end{bmatrix} = \begin{bmatrix} V_+ \sin\theta_+ + V_- \sin\theta_- \\ -V_+ \cos\theta_+ + V_- \cos\theta_- \end{bmatrix} \quad (12)$$

performing

dq Transform,  $T_{dq}(\hat{\theta})$  on  $\alpha\beta$

$$\bar{V}_{dq} = T_{dq}(\hat{\theta}) \bar{V}_{\alpha\beta}$$

$$= T_{dq}(\hat{\theta}) \begin{bmatrix} V_+ \sin\theta_+ + V_- \sin\theta_- \\ -V_+ \cos\theta_+ + V_- \cos\theta_- \end{bmatrix}$$

$$= \begin{bmatrix} \cos\hat{\theta} \sin\hat{\theta} \\ -\sin\hat{\theta} \cos\hat{\theta} \end{bmatrix} \begin{bmatrix} V_+ \sin\theta_+ + V_- \sin\theta_- \\ -V_+ \cos\theta_+ + V_- \cos\theta_- \end{bmatrix} \quad (13)$$

$$= \begin{bmatrix} V_+ \sin(\theta_+ - \hat{\theta}) + V_- \sin(\theta_- + \hat{\theta}) \\ -V_+ \cos(\theta_+ - \hat{\theta}) + V_- \cos(\theta_- + \hat{\theta}) \end{bmatrix}$$

The estimated phase angle =  $\hat{\theta}$

Assuming, that the PLL successfully track the phase at  $\hat{\theta} = \theta_- = \theta_+$ , then

$$\bar{V}_{dq} = \begin{bmatrix} V_- \sin 2\hat{\theta}_+ \\ -V_+ + V_- \cos 2\hat{\theta}_+ \end{bmatrix} \quad (14)$$

$2\hat{\theta}_+$  is the double frequency, to be eliminated.

Ideally it is necessary to obtain  $\bar{V}_{dq} = \begin{bmatrix} 0 \\ -V_+ \end{bmatrix}$

To eliminate the double frequency component, a new technique is introduced. An all pass function is used to introduce  $+90^0$  shift on the d-q values to eliminate the double frequency component. This is implemented with the proposed dqPLL schematic circuit as shown in Fig. 2.

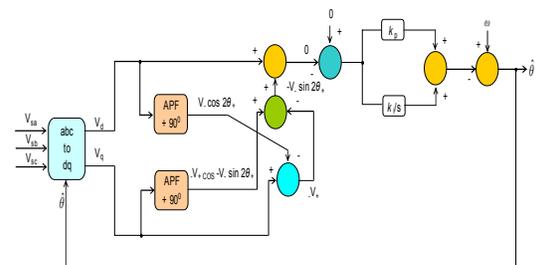


Fig. 2: Proposed dqPLL

An evaluation of the synchronization algorithms described above is explained in the following example: Consider a simulation with SLGF voltage sag of 20 %, the unbalanced supply voltage as  $V_{sa} = 184$  V,  $V_{sb} = 220$  V and  $V_{sc} = 230$  V and  $\omega = 2\pi * 50$  rad/s. The

parameters of the dqPLL are adjusted as  $k_p = 1.536$  and  $k_i = 272$ , where  $k_p$  is proportional gain and  $k_i$  is integral time constant.

The proposed technique is tested in PSCAD and in MATLAB / SIMULINK. The simulation results are discussed in section 7.

### 5. TRANSIENT ANALYSIS OF PLL

The stability condition of the PLL is obtained by investigating the PLL transfer function. The second-order transfer function of PLL linearized model is

$$\frac{\hat{\theta}(s)}{\theta(s)} = \frac{2\zeta\omega_n s + \omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \quad (15)$$

Let the input  $\theta(t)$  be a unit step,  $u(t)$ , so that  $\theta(s) = 1/s$ ,

Therefore,

$$\begin{aligned} \hat{\theta}(s) &= \frac{1}{s} \left( \frac{2\zeta\omega_n s + \omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \right) \\ &= \frac{1}{s} - \frac{s}{s^2 + 2\zeta\omega_n s + \omega_n^2} \\ &= \frac{1}{s} - \frac{s}{(s + \zeta\omega_n)^2 + \omega_n^2(1 - \zeta^2)} \\ &= \frac{1}{s} - \frac{s + \zeta\omega_n}{(s + \zeta\omega_n)^2 + [\omega_n\sqrt{1 - \zeta^2}]^2} - \frac{\zeta}{\sqrt{1 - \zeta^2}} \frac{\omega_n\sqrt{1 - \zeta^2}}{(s + \zeta\omega_n)^2 + [\omega_n\sqrt{1 - \zeta^2}]^2} \end{aligned}$$

In time domain,

$$\hat{\theta}(t) = \left[ 1 - e^{-\zeta\omega_n t} \cos(\omega_n\sqrt{1 - \zeta^2}t) - \frac{\zeta}{\sqrt{1 - \zeta^2}} e^{-\zeta\omega_n t} \sin(\omega_n\sqrt{1 - \zeta^2}t) \right] u(t)$$

From the analysis, it is observed that the second-order function is stable.

### 6. TUNING SECOND-ORDER PLL

From Fig. 3,

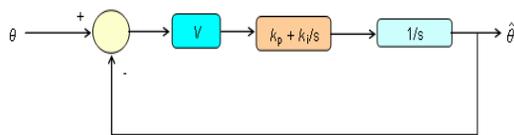


Fig. 3 : Linearized model of PLL

The closed loop transfer function of the linearized model of PLL is

$$\begin{aligned} G(s) &= \frac{\hat{\theta}(s)}{\theta(s)} = \frac{V(k_p + \frac{k_i}{s}) \frac{1}{s}}{1 + V(k_p + \frac{k_i}{s}) \frac{1}{s}} \\ &= \frac{k_p V s + k_i V}{s^2 + k_p V s + k_i V} \quad (16) \end{aligned}$$

Comparing equation (16) with the general form of second order transfer function

$$\begin{aligned} \frac{2\zeta\omega_n s + \omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \\ k_p V = 2\zeta\omega_n \quad k_i V = \omega_n^2 \\ k_p = \frac{2\zeta\omega_n}{V} \quad k_i = \frac{\omega_n^2}{V} \end{aligned}$$

The PLL must be tuned to get the desired transient performance. The gains of the PI controller are adjusted to obtain the desired performance. If the PLL is fast, the proportional gain must be high and the stability limit is reached. Slow response PLL is able to cope with phase-angle jump at the sensitive load end, but not suitable for QPP design. Slow response will not disturb the phase-angle jump at the sensitive load end but the PLL is not able to lock to the supply voltage during voltage sag. Hence, the PLL is tuned such that the loads are not disturbed during voltage sag. To achieve sufficient phase margin and higher bandwidth, value of  $k_p$  and  $k_i$  is adjusted accurately. Lower value of  $k_i$  will ensure fast tracking and value of  $k_p$  influences the phase margin and bandwidth.

### 7. RESULTS

Accurate three-phase reference voltage signals with controlled magnitudes, phase and frequency are generated from the PLL. Simulation is carried out for balanced and unbalanced faults, in presence of harmonics and balanced and unbalanced faults with harmonics. Fig. 4 shows the simulation in PSCAD and the results of phase angle estimation is shown in Fig. 5. Fig. 6 shows the simulation in MATLAB / SIMULINK and the results of the phase angle estimation and the double frequency elimination results are shown in

Fig. 7 and 8, respectively. Fig. 9 is a sample result for three-phase fault and restored voltage and Fig.10 is a sample result for three-phase fault with voltage harmonics compensation and restored voltage. The QPP is connected at 0.05 sec and off at 0.15 sec. Total simulation time with QPP is 0.1 sec and total simulation duration is 0.2 sec. QPP has restored the voltage at the sensitive load end to sinusoidal.

## 8. CONCLUSION

In this paper, the design of PLL with dqPLL technique, for improved performance of QPP in distorted supply condition is discussed.

The operation of the proposed scheme is verified by simulation using PSCAD and MATLAB / Simulink. The proposed system with dqPLL algorithm has superior performance and is able to operate in distorted supply conditions with high accuracy and has good dynamic time response. The simulation result shows the steady-state error is zero and the  $2\omega$  frequency oscillation error automatically goes to zero. Hence, this control approach achieves zero steady-state error voltage regulation. The proposed improvised technique is the most appropriate solution for the proposed control scheme for the QPP. The performance of the proposed dqPLL has been tested in all cases of voltage sags as well as with harmonics. The PI controller must be well tuned for optimum performance.

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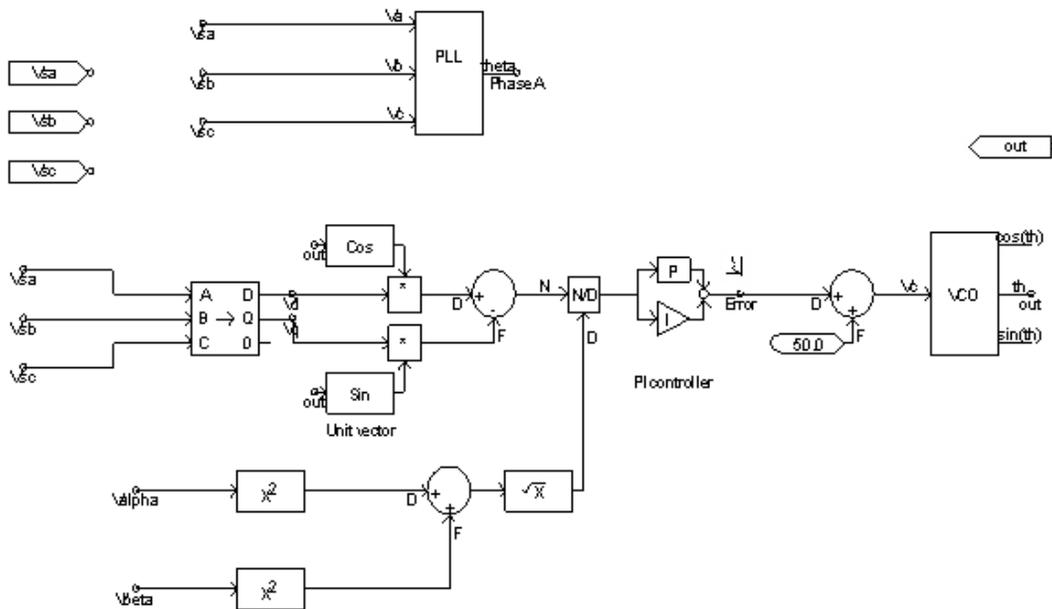


Fig. 4: Proposed dqPLL implemented in PSCAD

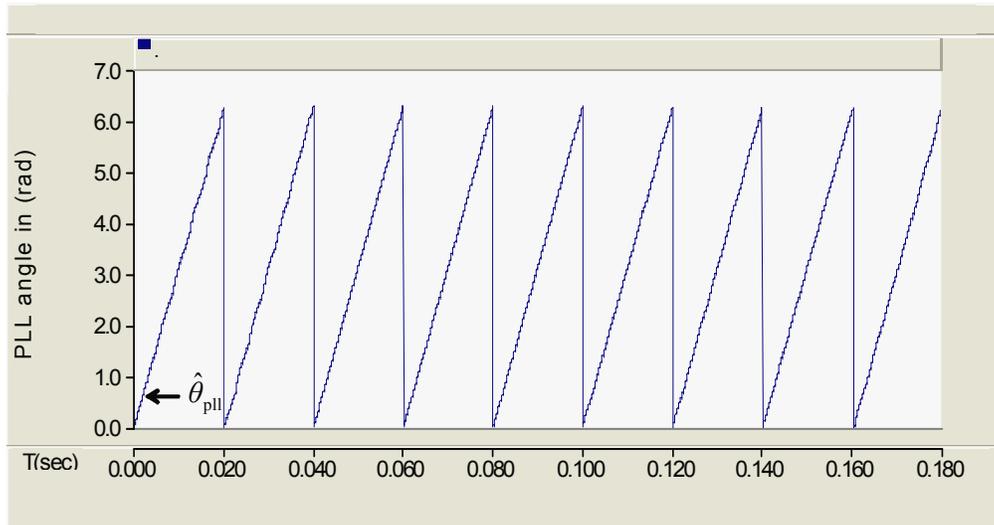


Fig. 5: Tracking of supply phase angle with dqPLL algorithm under distorted and unbalanced condition in PSCAD

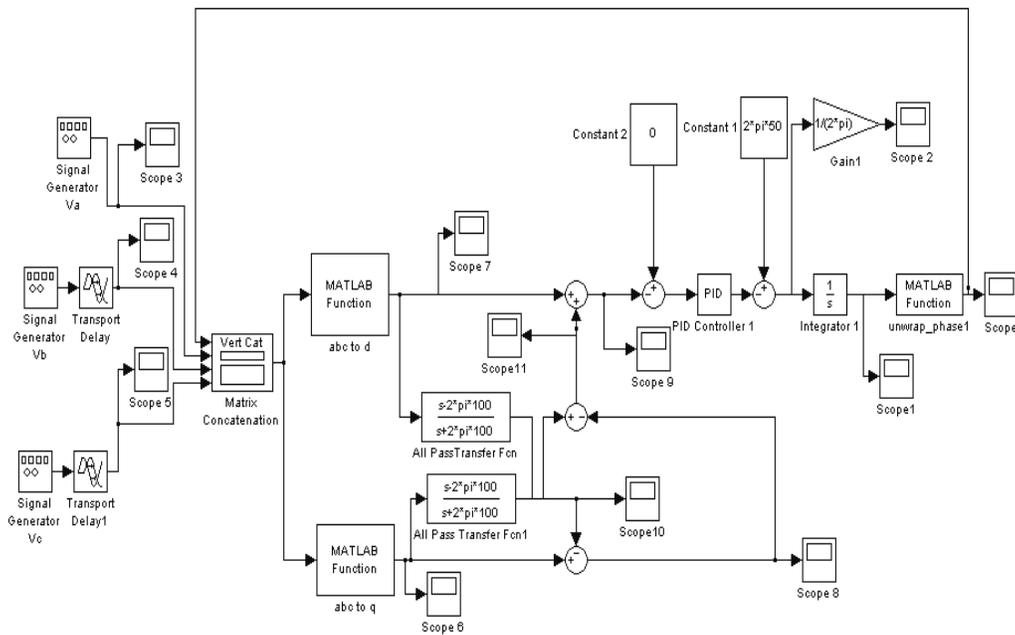


Fig. 6: Proposed dqPLL implemented in MATLAB.

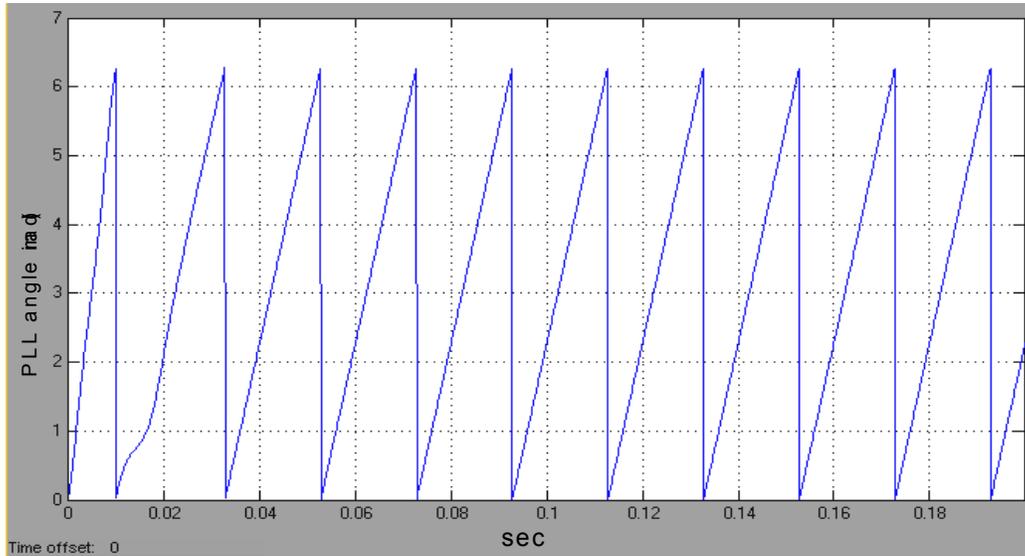


Fig. 7: Tracking of supply phase angle with dqPLL algorithm under distorted and unbalanced condition in SIMULINK

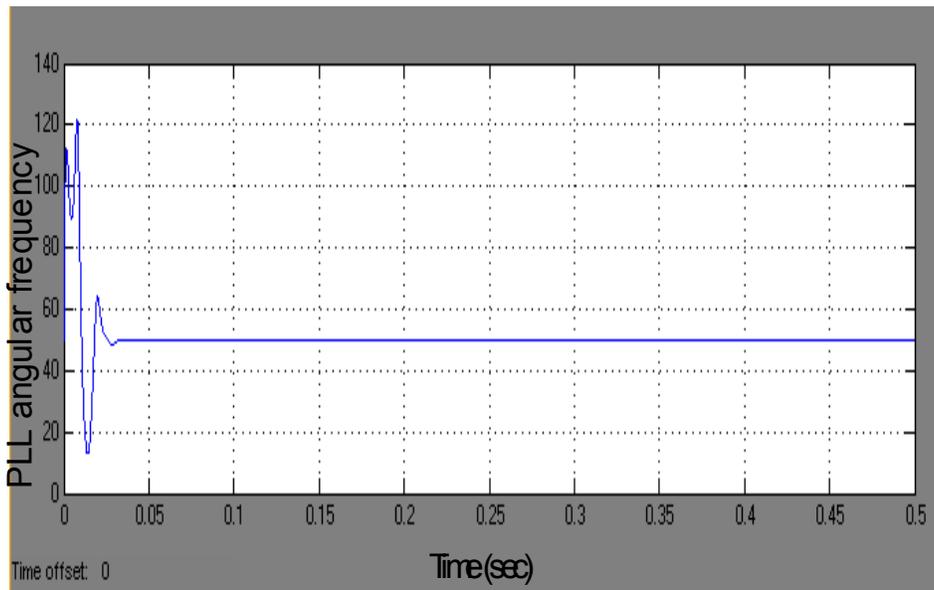


Fig. 8: Elimination of error and double frequency ripples result.

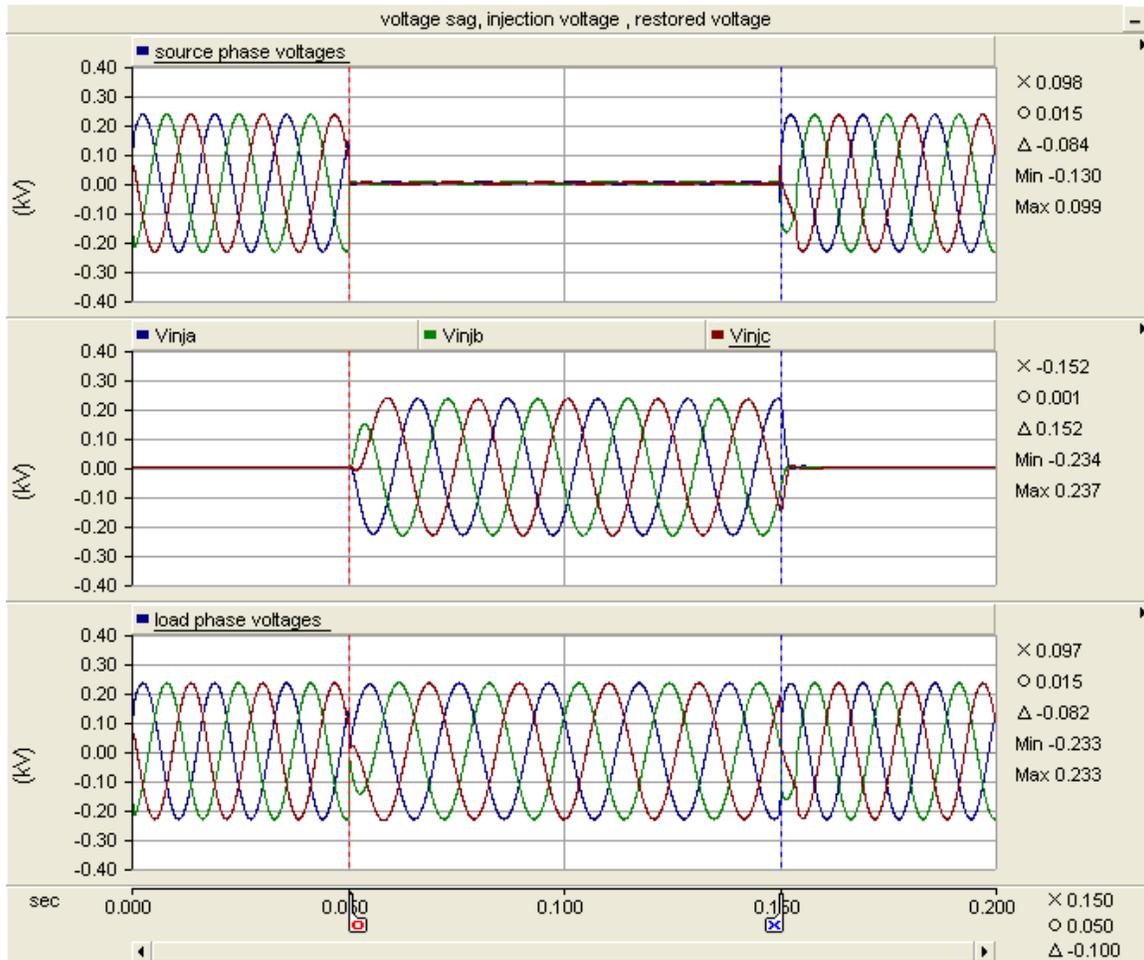


Fig. 9: Three-phase fault

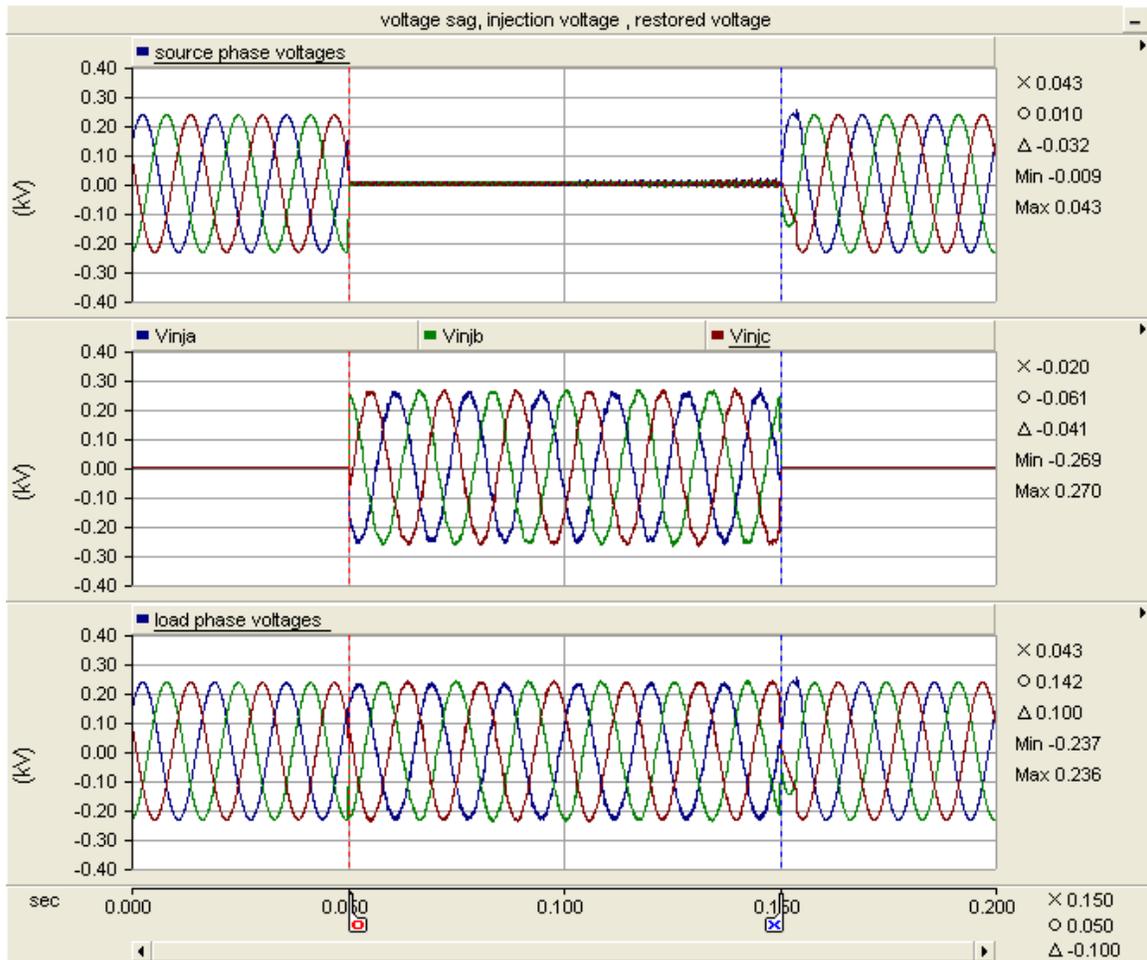


Fig. 10: Three-phase fault with voltage harmonics compensation