

A COMPARATIVE ANALYSIS BETWEEN K-MEDDOIDS AND FUZZY C-MEANS CLUSTERING ALGORITHMS FOR STATISTICALLY DISTRIBUTED DATA POINTS

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ABSTRACT

Data clustering is a process of putting similar data into groups. A clustering algorithm partitions a data set into several groups such that the similarity within a group is larger than among groups. In the field of data mining, various clustering algorithms are proved for their clustering quality. This research work deals with, two of the most representative clustering algorithms namely centroid based K-Medoids and representative object based Fuzzy C-Means are described and analyzed based on their basic approach using the distance between two data points. For both the algorithms, a set of n data points are given in a two-dimensional space and an integer K (the number of clusters) and the problem is to determine a set of n points in the given space called centers, so as to minimize the mean squared distance from each data point to its nearest center. The performance of the algorithms is investigated during different execution of the program for the given input data points. Based on experimental results the algorithms are compared regarding their clustering quality and their performance, which depends on the time complexity between the various numbers of clusters chosen by the end user. The total elapsed time to cluster all the data points and Clustering time for each cluster are also calculated in milliseconds and the results compared with one another.

Key Words: *K-Medoids Algorithm, Fuzzy C-Means Algorithm, Cluster Analysis, Data Analysis.*

1. INTRODUCTION

Clustering is an important area of application for a variety of fields including data mining, knowledge discovery, statistical data analysis, data compression and vector quantization. Clustering has been formulated in various ways in machine learning, pattern recognition, optimization and statistics literature. Clustering is the most common form of unsupervised learning. According to the rule of the unsupervised learning, clustering does not require supervision. No supervision means that there is no human expert who has assigned documents to classes. In clustering, it is the distribution and makeup of the data that will determine cluster membership. The notion of what constitutes a good cluster depends on the application and there are many methods for finding clusters subject to various criteria. These include approaches based on splitting and merging such as ISODATA, randomized approaches such as CLARA, CLARANS, and methods based on neural nets, and methods designed to scale to large databases, including DBSCAN, BIRCH and ScaleKM [2][4][10]. Among clustering formulations that are based on minimizing a formal

objective function, perhaps the most widely used and studied is partition based algorithms like K-Means, K-Medoids and Fuzzy C-Means clustering. In a partitioned algorithm, given a set of n data points in real d -dimensional space, and an integer k , the problem is to determine a set of k points in R^d , called centers, so as to minimize the mean squared distance from each data point to its nearest center. This measure is often called the squared-error distortion and this type of clustering falls into the general category of variance based clustering [5][8][9].

A simple example of cluster is given in Fig. 1. It is visually clear that there are three distinct clusters of 50 data points. The key input to a clustering algorithm is the distance measure.

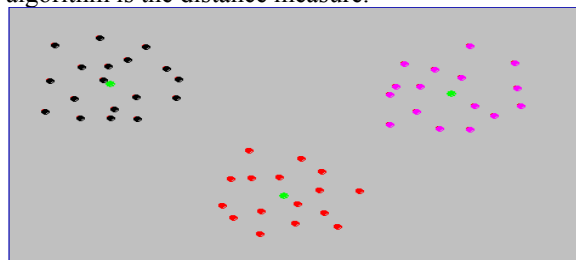


Fig. 1: Cluster Example



In Fig. 1, the distance measure is distance in the 2D plane. The cluster center is displayed in green color and the data points of each cluster are displayed in different colors. This measure suggests three different clusters in the figure. In most of the clustering approaches, the distance measure used is the Euclidean distance [6]. Different distance measures give rise to different clustering. Thus, the distance measure is an important means by which this research can influence the outcome of clustering.

2. METHODOLOGY

An important step in most clustering is to select a distance measure, which will determine how the similarity of two elements is calculated. This will influence the shape of the clusters, as some elements may be close to one another according to one distance and farther away according to another. For example, in a 2-dimensional space, the distance between the point $(x = 1, y = 0)$ and the origin $(x = 0, y = 0)$ is always 1 according to the usual norms, but the distance between the point $(x = 1, y = 1)$ and the origin can be 2, $\sqrt{2}$ or 1 if you take respectively the 1-norm, 2-norm or infinity-norm distance. The variety of common distance functions are as follows:

- The Euclidean distance. This type of distance is also called as the distance as the crow flies or 2-norm distance).
- The Manhattan distance (aka taxicab norm or 1-norm)
- The maximum norm (aka infinity norm)
- The Mahalanobis distance corrects data for different scales and correlations in the variables.
- The angle between two vectors can be used as a distance measure when clustering high dimensional data.
- The Hamming distance measures the minimum number of substitutions required to change one member into another.

Another important distinction is whether the clustering uses symmetric or asymmetric distances. Many of the distance functions listed above have the property that distances are symmetric (the distance from object A to B is the same as the distance from B to A). In other applications, this is not the case. (A true metric gives symmetric measures of distance.) The symmetric and 2-norm distance measure is used in this research work. In the Euclidean space \mathbf{R}^n , the distance between two points is usually given by the Euclidean distance (2-norm distance). The formula for 2-norm distance is

$$2\text{-norm distance} = \left(\sum_{i=1}^n |x_i - y_i|^2 \right)^{1/2}$$

The 2-norm distance is the Euclidean distance, a generalization of the Pythagorean Theorem to more than two coordinates. It is what would be obtained if the distance between two points were measured with a ruler: the "intuitive" idea of distance. Based on this idea of finding the distance between data points, the clustering qualities of the proposed algorithms are analyzed in this work.

Determining the quality of a clustering algorithm involves evaluating and assessing the quality of the clusters produced and is an important task in data mining. There are three approaches to measuring cluster quality, based on external, relative and internal criteria. The term external validity criteria are used when the results of the clustering algorithm can be compared with some pre-specified clustering structures (Halkidi et al., 2002). Relative validity criteria measure the quality of clustering results by comparing them with others generated by other clustering algorithms, or by the same algorithm using different parameters [6][17][18]. An internal validity criterion involve the development of functions that compute the distances between objects within each cluster, or the distance between the clusters themselves, and uses such distances to assess the clustering quality. To achieve a good clustering, these criteria are in the form of measures to assess the quality of a clustering. This work uses only the internal validity criteria in a random way. The Euclidean distance is used to find the distance between the input data points.

To create input data points in the applet window, the Box-Muller formula is used. For computer simulations, it is often useful to generate values that have a normal distribution. There are several methods and the most basic is to invert the standard normal cumulative distribution function. One of the efficient methods is the Box-Muller transform. A simple approximate approach that is easy to program is as follows. Simply sum 12 uniform (0, 1) deviates and subtract 6 (half of 12). This is quite usable in many applications. The sum over these 12 values has an Irwin-Hall distribution; 12 are chosen to give the sum a variance of exactly one. The resulting random deviates are limited to the range $(-6, 6)$ and have a density which is a 12-section eleventh-order polynomial approximation to the normal distribution. Box-Muller method is used for normal distribution coding to calculate the data points X and Y. This method says that, if two independent random



numbers U and V are uniformly distributed on $(0, 1]$, (e.g. the output from a random number generator), then two independent standard normally distributed random variables are X and Y , where

$$X = \sqrt{-2 \ln U} \cos(2\pi V) \quad (1)$$

$$Y = \sqrt{-2 \ln U} \sin(2\pi V) \quad (2)$$

This formulation arises because the chi-square distribution with two degrees of freedom is an easily-generated exponential random variable (which corresponds to the quantity of natural logarithm of U in these equations). Thus an angle is chosen uniformly around the circle via the random variable V , a radius is chosen to be exponential and then transformed to (normally distributed) x and y coordinates. The basic form of the Box-Muller method is as follows. Suppose U_1 and U_2 are independent random variables that are uniformly distributed in the interval $(0, 1]$. Let

$$Z_0 = R \cos(\theta) = \sqrt{-2 \ln U_1} \cos(2\pi U_2) \quad (3)$$

$$Z_1 = R \sin(\theta) = \sqrt{-2 \ln U_1} \sin(2\pi U_2) \quad (4)$$

Then Z_0 and Z_1 are independent random variables with a normal distribution of standard deviation 1. The derivation is based on the fact that, in a two-dimensional cartesian system where X and Y coordinates are described by two independent and normally distributed random variables, the random variables for R^2 and Θ in the corresponding polar coordinates are also independent and can be expressed as

$$R^2 = -2 \cdot \ln U_1 \text{ and } \theta = 2\pi U_2 \quad (5)$$

Because R^2 is the square of the norm of the standard bivariate normal variable (X, Y) , it has the chi-square distribution with two degrees of freedom. In the special case of two degrees of freedom, the chi-square distribution coincides with the exponential distribution, and the equation for R^2 above is a simple way of generating the required exponential variate. The next sections deal with the basic concepts of K-Medoids and Fuzzy C-Means algorithm followed by the experimental results.

3. K-MEDOIDS ALGORITHM

The very popular K-Means algorithm is sensitive to outliers since an object with an extremely large

value may substantially distort the distribution of data. How might the algorithm be modified to diminish such sensitivity? Instead of taking the mean value of the objects in a cluster as a reference point, a Medoid can be used, which is the most centrally located object in a cluster [14][15]. Thus the partitioning method can still be performed based on the principle of minimizing the sum of the dissimilarities between each object and its corresponding reference point. This forms the basis of the K-Medoids method (Han and Kamber, 2006; Jain, et al., 1999; Kaufman and Rousseeuw, 1990). The basic strategy of K-Medoids clustering algorithms is to find k clusters in n objects by first arbitrarily finding a representative object (the Medoids) for each cluster. Each remaining object is clustered with the medoid to which it is the most similar. K-Medoids method uses representative objects as reference points instead of taking the mean value of the objects in each cluster. The algorithm takes the input parameter k , the number of clusters to be partitioned among a set of n objects (Park, et al., 2009; Dunham, 2003; Han and Kamber, 2006). A typical K-Medoids algorithm for partitioning based on Medoid or central objects is as follows:

Input: k : The number of clusters
 D : A data set containing n objects
Output: A set of k clusters that minimizes the sum of the dissimilarities of all the objects to their nearest medoid.
Method: Arbitrarily choose k objects in D as the initial representative objects;
Repeat assign each remaining object to the cluster with the nearest medoid;
 randomly select a non medoid object O_{random} ;
 compute the total points S of swapping object O_j with O_{random} ;
 if $S < 0$ then swap O_j with O_{random} to form the new set of k medoid;
Until no change;

Similar to the above algorithm, a Partitioning Around Medoids (PAM) was one of the first k-Medoids algorithms introduced by researchers. It attempts to determine k partitions for n objects. After an initial random selection of k medoids, the algorithm repeatedly tries to make a better choice of medoids [16][21]. Therefore, the algorithm is often called as representative object based algorithm.



4. FUZZY C-MEANS ALGORITHM

Traditional clustering approaches generate partitions; in a partition, each pattern belongs to one and only one cluster. Fuzzy clustering extends this notion to associate each pattern with every cluster using a membership function [1][7]. The output of such algorithms is a clustering, but not a partition some times. Fuzzy clustering is a widely applied method for obtaining fuzzy models from data. It has been applied successfully in various fields including geographical surveying, finance or marketing. This method is frequently used in pattern recognition. It is based on minimization of the following objective function:

$$J_m = \sum_{i=1}^N \sum_{j=1}^C u_{ij}^m \|x_i - c_j\|^2, \quad 1 \leq m < \infty$$

where m is any real number greater than 1, u_{ij} is the degree of membership of x_i in the cluster j, x_i is the i^{th} of d-dimensional measured data, c_j is the d-dimension center of the cluster, and $\|*\|$ is any norm expressing the similarity between any measured data and the center (Al-Zoubi et al., 2007; Yong et al., 2004). Fuzzy partitioning is carried out through an iterative optimization of the objective function shown above, with the update of membership u_{ij} and the cluster centers c_j by:

$$u_{ij} = \frac{1}{\sum_{k=1}^c \left[\frac{\|x_i - c_j\|}{\|x_i - c_k\|} \right]^{2/m}}, \quad c_j = \frac{\sum_{i=1}^N u_{ij}^m \cdot x_i}{\sum_{i=1}^N u_{ij}^m}$$

This iteration will stop when $\max_{ij} \left\{ u_{ij}^{(k+1)} - u_{ij}^{(k)} \right\} < \xi$, where ξ is a termination criterion between 0 and 1, whereas k are the iteration steps. This procedure converges to a local minimum or a saddle point of J_m . The algorithm is composed of the following steps:

- Step 1:** Initialize $U=[u_{ij}]$ matrix, $U^{(0)}$
- Step 2:** At k-step: calculate the centers vectors $C^{(k)}=[c_j]$ with $U^{(k)}$
- Step 3:** Update $U^{(k)}$, $U^{(k+1)}$
- Step 4:** If $\|U^{(k+1)} - U^{(k)}\| < \xi$ then STOP; otherwise return to step 2.

In this algorithm, data are bound to each cluster by means of a Membership Function, which represents the fuzzy behavior of the algorithm. To

do that, the algorithm has to build an appropriate matrix named U whose factors are numbers between 0 and 1, and represent the degree of membership between data and centers of clusters (Moh'd Belal Al-Zoubi, ed al., 2007). FCM clustering techniques are based on fuzzy behavior and provide a natural technique for producing a clustering where membership weights have a natural (but not probabilistic) interpretation. This algorithm is similar in structure to the K-Means algorithm and also behaves in a similar way [12][23][24]. For the creation of input data points for both the algorithms, the Box-Muller formula is used [3]. With this discussion, the next part of this paper analyses the experimental results and discussion about the results.

5. EXPERIMENTAL RESULTS

Having introduced the two clustering techniques and their basic mathematical foundations, now turn to the discussion of these techniques on the basis of a practical approach. This approach involves the implementation of the two techniques introduced previously, and performance of the algorithms is tested on statistical distributions of input data points via Normal and Uniform distributions. Therefore, the implementation plan consists of two parts; one for Normal distribution of input data points and the other for Uniform distribution. For both the types of distributions, the data points are created using Box-Muller formula as discussed [3]. The program is written in JAVA language. After the creation of data points, the user has to specify the number of clusters. In the output window, the data points in each cluster are displayed by different colors and the execution time is calculated in milliseconds [19][20][21]. Now, the discussion starts with the Normal distribution of input data points first followed by Uniform distribution. The resulting clusters of the Normal distribution for K-Medoids algorithm is given in Fig. 2. The number of data points and clusters given by end user as input during the execution of the program is 1000 and 5 ($k = 5$) respectively. The algorithm is repeated 1000 times (one iteration for each data point) to get efficient output. The cluster centers (centroids) are calculated for each cluster by its mean value and clusters are formed depending upon the distance between data points.

Different approaches of clustering yields different types of outcomes. In this work, for different input data points, the algorithm gives different types of outputs. The input data points are

generated in red color and the output of the algorithm is displayed in different colors as shown in Fig. 2. The center point of each cluster is displayed in white color. The total elapsed time and the execution time for each cluster to each run are calculated in milliseconds. The time taken for execution of the algorithm varies from one run to another run and also it differs from one computer to another computer. The number of data points is the size of the cluster. If the number of data points are 1000 then the algorithm is repeated the same one thousand times. For each data point, the algorithm executes once. The algorithm takes 4375 milliseconds for 1000 data points and 5 clusters. The same algorithm is executed 5 times and results are tabulated in table 1 (against the rows

‘Normal’). The total elapsed time for all clusters is given at the end of the row ‘Size’. The sum of the execution time for each cluster (individual execution time for each cluster) is given at the end of the row ICT (Individual Cluster Time). The difference between these two is available in the last column. For the same one thousand uniformly distributed data points, the algorithm is executed 5 times and the results are listed in table 1 (against the rows ‘Uniform’). Next, one of the outcomes for 1000 uniformly distributed data points and 10 clusters is shown in Fig. 3. In this case, the algorithm takes 7344 milliseconds for 10 clusters. But the sum of the individual clustering time is 7313 milliseconds. The difference time between these two is 31 milliseconds.

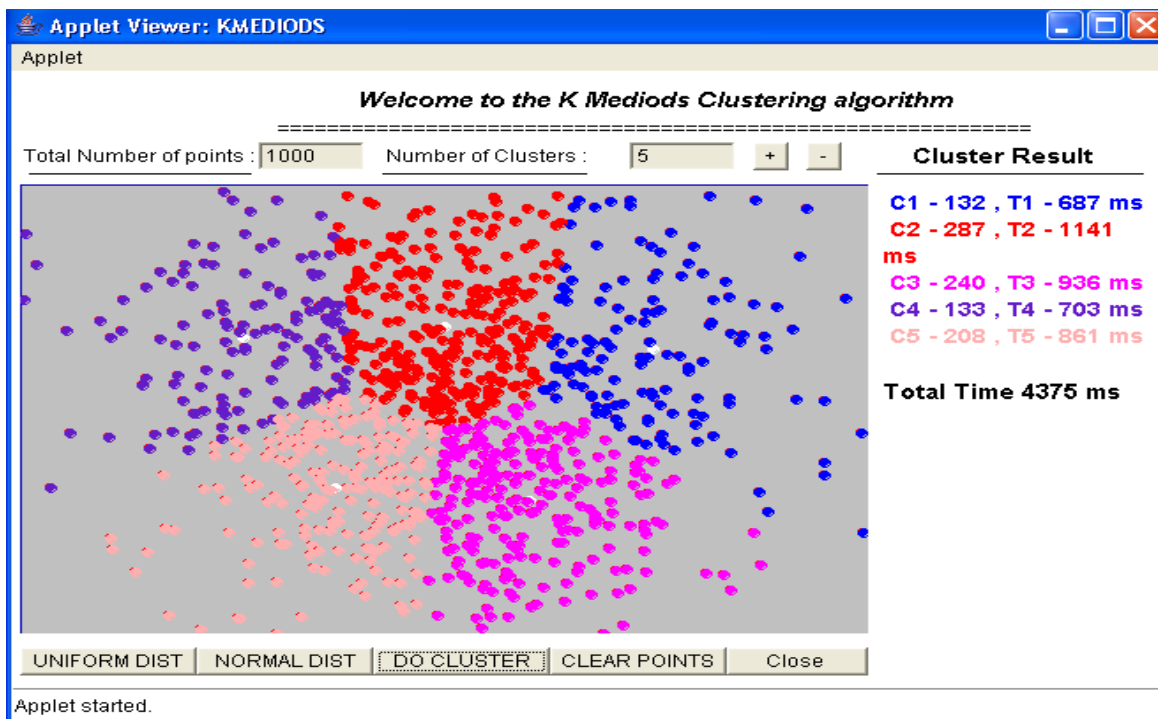


Fig. 2: Normal Distribution Output- K-Medoids

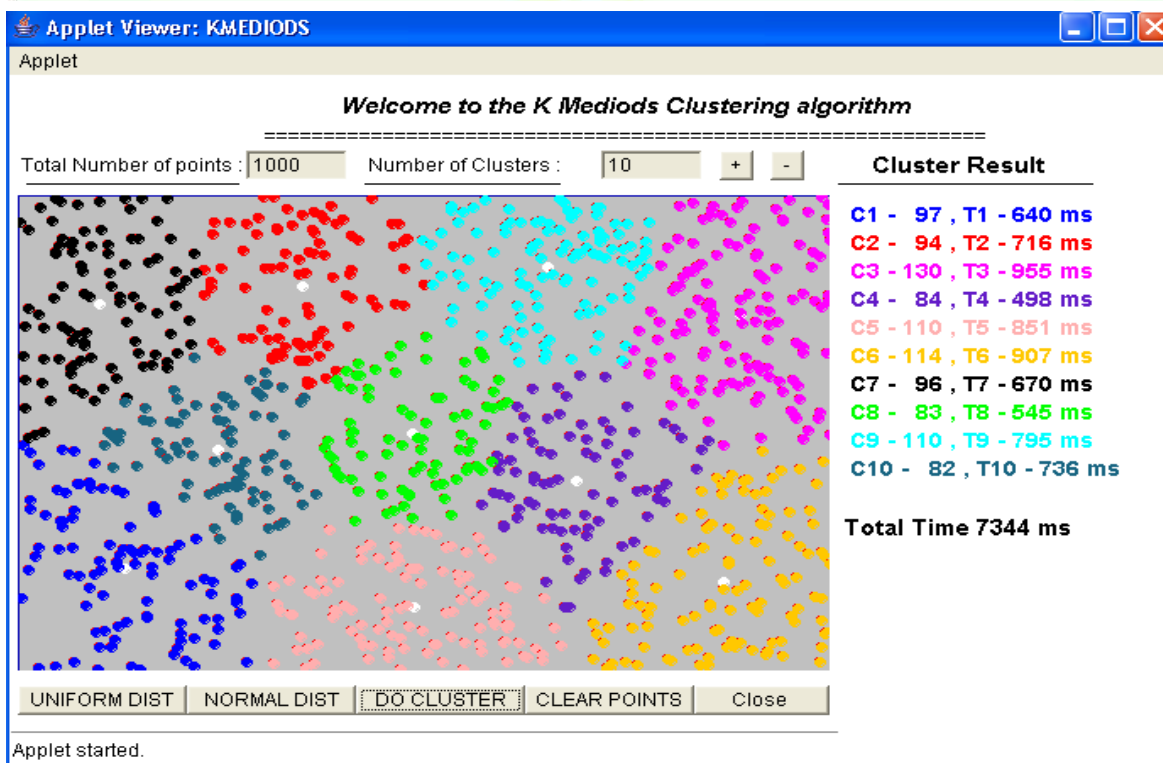


Fig. 3: Uniform Distribution Output-K-Medoids

Next, the FCM algorithm is executed by taking 1000 Normal distribution of data points as input. The number of clusters chosen by the user is 5. The execution time taken by the system is 3953 milliseconds. Like, the algorithm is executed for one thousand uniformly distributed data points. Now the algorithm takes 3797 milliseconds for execution. Five times the algorithm is executed and the results are given in table 2 for both the types of inputs. Here also the difference time between total elapsed time and the sum of the execution time for all clusters is given in the last row. Next, both the algorithms are executed 5 times by considering the number of clusters is 10 and the results are given in the table 3. This table contains only the execution time for each cluster and the total elapsed time. The third column is the type of the distribution. Clustering time for Normal distribution is listed against the rows 'N' and for the Uniform distribution is listed against the rows 'U'. The execution time for each cluster is given in the table from the columns 1 to 10 for ten clusters. The sum of each cluster individual time is available in the column ICT (Individual Cluster Time). The total elapsed time is indicated in the column TET (Total

Elapsed Time). The difference time (DT) between ICT and TET is calculated and is given in the last column. Fig. 4 is the output for 1000 normally distributed data points with 15 clusters of FCM algorithm. For the same algorithm, the number of clusters chosen by the user is 20 and the result of 1000 uniformly distributed data points is shown in Fig. 5. Table 4 shows that the performance results comparison for all the types of data distributed for the experiments for 5 and 10 clusters. Also the table contains the best and worst execution times for all the categories. From the table, it is clear that the best times (BT) are derived from the result of uniform distribution and the worst times (WT) are from normal distribution. The average times of ICT and TET are given in the same table for both the algorithms for the normal and uniform distributions of input data points. The difference time between ICT and TET are calculated and is given in the columns DT1 and DT2 for 5 and 10 clusters respectively. Next, both the algorithms are executed by choosing the number of clusters 15, 20 and the average times are listed in the table 5. Here ICT and TET times alone taken for discussion.

Table 1: Cluster Results for K-Medoids

Run	Distribution	Cluster	1	2	3	4	5	T.Time	Diff.Time
1	Normal	Size	132	287	240	133	208	4375	47
		ICT	687	1141	936	703	861	4328	
	Uniform	Size	198	230	199	200	173	4062	24
		ICT	889	759	835	815	740	4038	
2	Normal	Size	237	217	163	204	179	4203	30
		ICT	902	870	750	865	786	4173	
	Uniform	Size	162	158	254	189	237	3891	16
		ICT	687	656	866	737	929	3875	
3	Normal	Size	167	248	241	127	217	4090	42
		ICT	753	887	998	649	761	4048	
	Uniform	Size	216	165	171	190	258	4172	15
		ICT	841	654	717	861	1084	4157	
4	Normal	Size	200	252	195	219	134	4059	44
		ICT	896	943	700	787	689	4015	
	Uniform	Size	187	179	201	212	221	3994	24
		ICT	803	710	790	856	811	3970	
5	Normal	Size	133	202	194	217	254	4210	33
		ICT	720	856	798	813	990	4177	
	Uniform	Size	172	174	239	215	200	3944	27
		ICT	785	781	811	790	750	3917	

The programs of K-Medoids and FCM are executed many times and the results are analyzed based on the number of data points and the number of clusters. The behavior of the algorithms is analyzed by observations. The performance of the algorithms have also been analyzed for several executions by considering different data points (for which the results are not shown) as input (1500 data points, 2000 data points etc.) and the number of clusters are from 15 and 20 (for which also the results are not shown), the outcomes are found to be highly satisfactory [20][21]. According to the results obtained from the proposed two data clustering

algorithms, the results are compared based on their performance and clustering quality. A table of the achieved results by giving average times for each of the two techniques is presented in Table 5 and the graphical format is shown in Fig. 6. By comparing the average times of both the algorithms, it can easily observe that the FCM algorithm takes less time than the K-Medoids algorithm. For example, the average time for 15 clusters for normal distribution of data points is 10415.6 milliseconds, but for the FCM algorithm it is found to be 10305.6 milliseconds. This same type of results repeats for uniform distribution also.

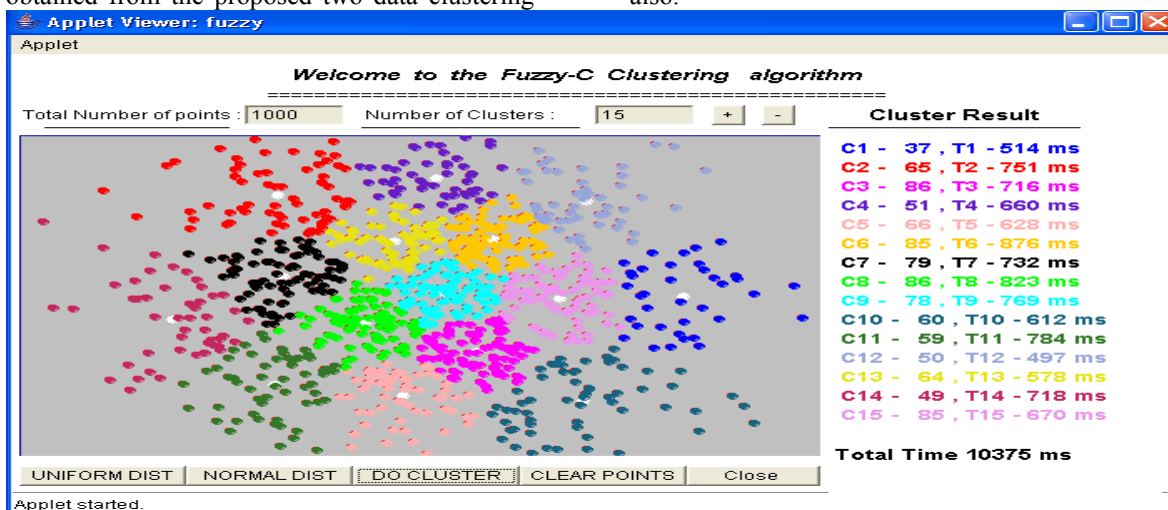


Fig. 4: Normal Distribution Output- Fuzzy C-Means

Table 2: Cluster results for FCM

Run	Distribution	Cluster	1	2	3	4	5	T.Time	Diff.Time
1	Normal	Size	269	207	152	235	137	3953	16
		ICT	951	858	768	769	591	3937	
	Uniform	Size	169	213	252	179	187	3797	
		ICT	767	737	905	653	719	3781	
2	Normal	Size	160	162	201	211	266	4015	28
		ICT	723	705	781	845	933	3987	
	Uniform	Size	218	189	199	192	202	3818	
		ICT	840	689	810	702	762	3803	
3	Normal	Size	197	223	216	186	178	3943	31
		ICT	742	842	748	791	789	3912	
	Uniform	Size	216	236	206	169	173	3931	
		ICT	821	872	755	655	810	3913	
4	Normal	Size	214	237	162	176	211	4244	25
		ICT	838	970	813	704	894	4219	
	Uniform	Size	228	193	178	172	229	4024	
		ICT	852	775	750	740	884	4001	
5	Normal	Size	213	157	178	200	252	4125	26
		ICT	889	712	788	809	901	4099	
	Uniform	Size	199	163	244	194	200	4022	
		ICT	815	775	885	710	813	3998	

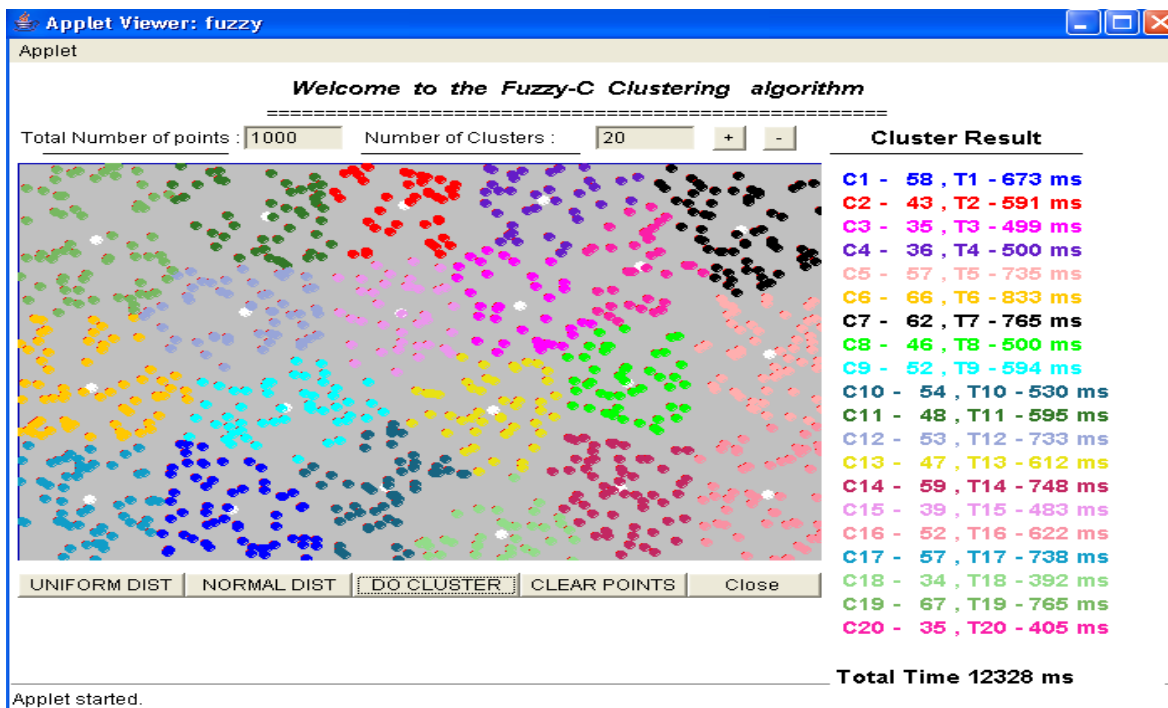


Fig. 5: Uniform Distribution Output- Fuzzy C-Means



Table 3: Cluster Results for 10 Clusters

Algorithm	R	Dist\Clr	1	2	3	4	5	6	7	8	9	10	ICT	TE T	D T
K-Medoids	1	N	73 5	86 5	65 5	63 6	670	64 0	53 1	892	952	891	746 7	750 1	34
		U	64 0	71 6	95 5	49 8	851	90 7	67 0	545	795	736	731 3	734 4	31
	2	N	69 3	62 5	87 6	65 5	889	84 3	70 3	645	655	691	727 5	732 1	46
		U	93 0	71 8	78 8	81 5	656	76 8	68 2	548	795	565	726 5	728 9	24
	3	N	69 9	95 5	59 8	68 7	749	60 2	71 8	891	689	755	734 3	737 8	35
		U	84 4	58 9	67 6	56 2	100 4	57 9	95 4	613	698	626	714 5	717 7	32
	4	N	81 7	65 6	74 8	73 1	861	73 4	73 5	889	656	563	739 0	742 2	32
		U	69 1	86 2	70 4	78 2	578	68 4	89 9	733	592	569	709 4	713 2	38
	5	N	72 3	62 4	71 7	85 5	718	80 7	57 9	619	627	107 1	734 0	736 8	28
		U	67 4	70 5	83 2	85 7	685	66 8	93 5	723	532	676	728 7	731 3	26
FCM	1	N	71 8	57 6	58 0	80 2	466	76 6	95 0	750	100 0	846	745 4	750 0	46
		U	90 6	54 5	65 6	67 2	924	84 4	57 7	685	656	722	718 7	720 8	21
	2	N	75 4	72 1	54 5	80 8	566	77 8	73 2	767	656	860	718 7	720 2	15
		U	59 5	79 7	84 2	67 4	907	56 5	56 1	700	595	858	709 4	712 5	31
	3	N	67 1	65 2	71 4	56 5	794	97 5	86 7	722	621	661	724 2	726 5	23
		U	78 7	64 3	77 8	76 1	689	68 8	64 3	783	747	562	708 1	710 1	20
	4	N	64 0	80 5	51 3	63 0	857	54 8	64 4	103 0	653	893	721 3	724 3	30
		U	78 9	59 6	71 4	70 5	760	67 6	61 1	673	699	887	711 0	713 5	25
	5	N	64 8	70 0	70 4	73 3	608	62 6	68 8	876	657	816	705 6	707 7	21
		U	51 4	76 4	70 6	63 9	828	67 2	62 3	610	724	982	706 2	708 5	23

Table 4: Results Comparison (5 and 10 Clusters)

Algorithm	Distribution	5 Clusters					10 Clusters				
		BT	WT	ICT	TET	DT1	BT	WT	ICT	TET	DT2
K-Medoids	Normal	4059	4375	4148.2	4187.4	39.2	7145	7501	7363	7398	35
	Uniform	3891	4172	3991.4	4012.6	21.2	7015	7342	7220.8	7251	30.2
FCM	Normal	3943	4244	4030.8	4056	25.2	7195	7500	7230.4	7257.4	27
	Uniform	3797	4024	3899.2	3918.4	19.2	7085	7250	7106.8	7130.8	24

Table 5: Performance Results Comparison

Algorithm	Dist.	5 Clusters		10 Clusters		15 Clusters		20 Clusters	
		ICT	TET	ICT	TET	ICT	TET	ICT	TET
K-Medoids	Normal	4148.2	4187.4	7363	7398	10385.6	10415.6	12770.4	12795.6
	Uniform	3991.4	4012.6	7220.8	7251	10289.3	10314.2	12635.5	12656.6
FCM	Normal	4030.8	4056	7230.4	7257.4	10276.2	10305.6	12625.2	12652.8
	Uniform	3899.2	3918.4	7106.8	7130.8	10184.1	10208.2	12510	12538.8

From Fig. 6, it is easy to identify the difference between the execution times for both the algorithms. Here, the total execution time alone taken for comparison. The individual clustering time is not taken. Since the partitioning based clustering algorithms behave in a similar way, the difference between the execution time is less significant.

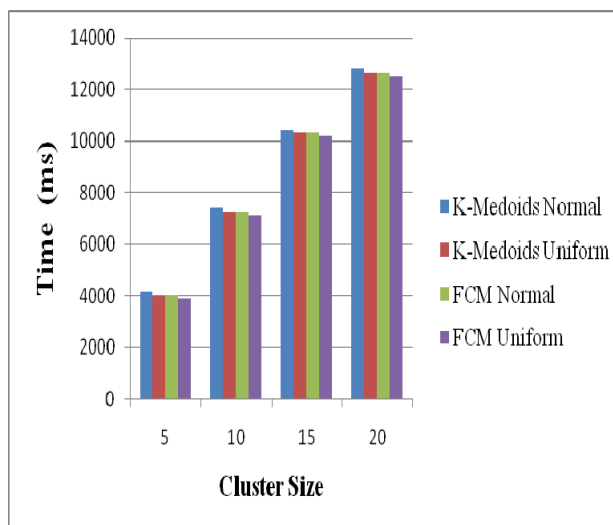


Fig. 6: Cluster Results

6. CONCLUSION

Cluster analysis is sensitive to both the distance metric selected and the criterion for determining the

order of clustering. Different approaches may yield different results. The choice of clustering algorithm depends on both the type of data available and on the particular purpose and application. It is very evident from table 5 that the performance of the FCM algorithm is relatively better than that of K-Medoids algorithm. Thus, for the data points generated using statistical distributions (via Normal and Uniform distributions), the FCM algorithm seems to be superior to K-Medoids. However, between the distributions Uniform distribution yields the best results. Generally, when the number of clusters increases, in turn will increase the execution time for both the algorithms. Hence, the time taken for execution depends on the number of clusters and the number of data points chosen by the user.

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